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TA435 .U58 V138:1982 C.1 NBS-PUB-C 1974



NBS BUILDING SCIENCE SERIES 138

Prediction of Pore Water Pressure Buildup and Liquefaction of Sands During Earthquakes by the Cyclic Strain Method

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Prediction of Pore Water Pressure Buildup and Liquefaction of Sands During Earthquakes by the Cyclic Strain Method

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Issued July 1982

Library of Congress Catalog Card Number: 82-600561

National Bureau of Standards Building Science Series 138

Nat. Bur. Stand. (U.S.), Bldg. Sci. Ser. 138, 168 pages (July 1982)

CODEN: BSSNBV

U.S. GOVERNMENT PRINTING OFFICE
WASHINGTON: 1982

For sale by the Superintendent of Documents, Government Printing Office, Washington, DC 20402
Price
(Add 25 percent for other than U.S. mailing.)

PREDICTION OF PORE WATER PRESSURE BUILDUP AND LIQUEFACTION OF SANDS
DURING EARTHQUAKES BY THE CYCLIC STRAIN METHOD

ABSTRACT

A cyclic strain approach for evaluating the buildup of excess pore water pressures and the potential for liquefaction of level sandy sites during earthquakes is proposed in this report. This strain approach is based on the premise that, for undrained loading of sand, there is a predictable correlation between cyclic shear strain and excess pore water pressure; also, that there is a threshold shear strain below which there is no sliding at the contacts between sand particles and no pore water pressure buildup can occur. As the result, a sand deposit will not develop excess pore pressures if the induced seismic shear strain is less than the threshold strain. Both theoretical evidence and experimental verification supporting the cyclic strain approach and the existence of the threshold, are presented in the report. Based on all these findings, a specific design method is proposed for predicting if excess pore pressures will develop at a specific site during a design earthquake.

Key words: cyclic strain; damping ratio; earthquake engineering; laboratory testing; liquefaction; particulate mechanics; particulate model; pore water pressure; sand; seismic loading; shear modulus; shear strain; site stability.

COVER: *A railroad embankment which was totally destroyed during an earthquake in Japan by liquefaction of the underlying loose saturated sands.*

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NOTATION

A	Normalized shear modulus parameter
a	Radius of contact area between two spheres
a_p	Horizontal peak acceleration at the ground surface
$(a_p)_t$	Threshold peak ground surface acceleration
c	Propagation velocity of the relevant seismic waves
C_r	Correction factor relating the cyclic shear strength obtained in a triaxial test to that anticipated under typical field conditions
D_r	Relative density
e	Void ratio
E	Young's modulus
f	Friction coefficient
G	Secant or effective shear modulus of soil
G_{max}	Shear modulus of soil at small strains ($\gamma_c \approx 10^{-4}$ percent)
g	Acceleration of gravity
K	Lateral earth pressure coefficient
K_0	Coefficient of lateral earth pressure at rest
K_2	Normalized stiffness parameter = $G/(\sigma'_3)^{1/2}$
M	Magnitude of earthquake, Richter Scale
N	Normal force
N	Standard penetration resistance
N', N_1	Corrected or modified standard penetration resistance for the effect of overburden pressure

NOTATIONS

n	Number of cycles of a sinusoidal (cyclic) shear stress or strain of uniform magnitude applied to the the test specimen
R	Radius of a sphere
$R(=\sigma_{dc}/2\sigma_3)$	Cyclic shear stress ratio in stress-controlled cyclic triaxial test
$r_d, r_d(z)$	Stress reduction factor varying from a value of one at z (depth) = 0 to values below 0.7 at $z = 100$ ft.
T	Tangential force
u	Initial pore water pressure
V	Seismic ground particle velocity
V_s	Shear wave velocity
ΔW	Area enclosed by $\tau - \gamma$ hysteresis loop
z	Depth of soil element below the ground surface
z_w	Depth of groundwater table
γ	Shear strain, cyclic shear strain
γ_c	Seismic (Cyclic) shear strain
γ_t	Threshold cyclic shear strain
δ	Tangential displacement between centers of spheres
Δe	Change of void ratio
$\Delta u, \Delta u(t)$	Excess pore water pressure; excess peak pore water pressure
Δu_r	Residual pore water pressure
ϵ_v	Axial strain corresponding to the first compression excursion (i.e., $n = 1/4$ cycle).
λ	Damping ratio
ν	Poisson's ratio

NOTATION

ρ	Mass density of soil
σ_c	Normal contact stress
σ_v	Initial vertical pressure
σ_o	Initial vertical pressure
σ'_o	Initial effective vertical pressure
σ_3	Initial total confining pressure; in triaxial testing, $\sigma_3 = \sigma_2 =$ confining pressure in the chamber.
σ'_3	Initial effective confining pressure
σ'_m	Average effective stress = $1/3 (\sigma'_1 + \sigma'_2 + \sigma'_3)$
σ_{dc}	Cyclic deviator stress
σ_{dp}	Peak cyclic deviator stress
$\tau, \tau(t)$	Cyclic shear stress
τ_c	Uniform magnitude of a sinusoidal (cyclic) shear stress applied to the test specimen, usually taken as a fraction of the peak value, τ_p .
τ_p	Peak seismic shear stress associated with peak ground acceleration
τ_{D_r}	Cyclic shear strength for a given relative density, D_r .
OCR	Overconsolidation ratio
$(\frac{\sigma_{dc}}{2\sigma'_o})_{50}$	Cyclic shear stress ratio causing liquefaction in the laboratory, for D_r of 50 percent.
$(\frac{G}{G_{max}})_\gamma$	Modulus reduction factor of the soil at shear strain γ

FACING PAGE: *This partial failure of the lower San Fernando Dam, which occurred during the February 1971 earthquake was the result of liquefaction of the hydraulically-filled embankment material. Eighty thousand people had to be temporarily evacuated and could have lost their lives in a total embankment collapse.*



1. INTRODUCTION

The liquefaction of saturated cohesionless soils during earthquakes is one of the most important problems facing earthquake engineers. There has scarcely been a major earthquake without at least some reported cases of liquefaction. Sand boils, flotation to the ground surface of buried concrete tanks, cracking of pavements, settlement and tilting of buildings and bridge supports, collapse of waterfront structures, lateral spreading and cracking of slopes and embankments, and flow failures of natural slopes and earth dams have been some of its manifestations.

Kuribayashi and Tasuoka, 1975 [42]^{1/} list 44 Japanese earthquakes between 1872 and 1968 for which liquefaction of sandy sites occurred. Of these, the best

¹ Numbers in brackets refer to literature references in section 9.

known is the Niigata earthquake of 1964, where tilting and failure of multistory buildings due to liquefaction of the foundation sand was widespread (see fig. 1.1) (Kishida, 1966 [36]; Koizumi, 1966 [38]; Ohsaki, 1966 [56]; Seed and Idriss, 1967 [76]). A more recent Japanese earthquake which also caused extensive liquefaction occurred on June 12, 1978 in Miyagi-Ken-Oki (Kobayashi et al., 1978 [37]; Yamamura et al., 1979 [89]).

Table 1.1 is a partial list of 14 other earthquakes outside Japan which have occurred during this century and which induced liquefaction.

The high incidence of liquefaction during earthquakes, together with its potential for damage, has made the phenomenon a prime subject of concern in earthquake engineering. The seismic design of nuclear power plants and other critical facilities routinely includes evaluation of the liquefaction potential of saturated sandy or silty cohesionless soil layers. The design of new and the inspection of old earth dams in seismic areas is carried out considering the possibility of liquefaction of the dam and/or its foundation when sandy or silty cohesionless soils are involved. Due to its complexity, the mechanism of the liquefaction phenomenon is not yet completely understood and a large amount of liquefaction research is still being done, especially in the U.S. and Japan. The recent upsurge in the construction of fixed offshore oil platforms throughout the world, where potential failure of the foundation due to ocean wave induced liquefaction of the ocean bottom must be considered in the design, has reinforced the interest in clarifying the liquefaction phenomenon.

Most research on liquefaction has taken place in the last 10 to 15 years. Some significant publications, including recent summaries and discussions of the state-of-the-art, are: Lee and Seed, 1967 [47]; Seed, 1968 [72]; Seed and Idriss, 1971 [78]; Castro, 1975 [9]; Youd, 1975 [93]; Seed et al., 1975 [80]; Castro and Poulos, 1977 [10]; Seed, 1979 [74]; and Peck, 1979 [61]. Some of these papers were presented at the ASCE Specialty Session on "Liquefaction Problems in Geotechnical Engineering" (ASCE, 1976 [4]).

In the last few years, two aspects of the liquefaction problem have generated a great deal of discussion and motivated significant research. The first aspect relates to the conditions necessary to produce unlimited flow of the liquefied soil in the field under the action of gravity loads such as those occurring in a slope or beneath a structure. There is now general consensus that, while loose or very loose cohesionless soils can experience unlimited flow, dense soils at usual confining pressures cannot, because of their dilative behavior at large shear strains (Castro and Poulos, 1977 [10]; Seed, 1979 [74]).

The second aspect of the problem is related to the importance of relative density on the rate at which excess pore water pressure builds up during an earthquake. Early work suggested that relative density is the key soil parameter controlling pore water pressure increases (Seed and Idriss, 1971 [78]). Many engineering decisions have been based on the assumption that relative density is the key parameter, and pore water pressures measured on reconstituted samples in cyclic laboratory tests have been taken to be representative of pore

Table 1.1 Some Modern Non-Japanese Earthquakes Which Have Induced Liquefaction

<u>Earthquake</u>	<u>Year</u>	<u>Reference</u>
San Francisco, California	1906	Lawson et al., 1908 [46] Youd and Hoose, 1976 [97]
Bihar-Nepal, India	1934	Geological Survey of India, 1939 [25]
El Centro, California	1940	Ross, 1968 [67]
San Francisco, California	1957	Ross, 1968 [67]
Coatzacoalcas, Mexico	1959	Diaz de Cossio, 1960 [17]
Southern Chile	1960	BSSA, 1963 [7]
Alaska	1964	Ross et al., 1969 [68]
Caracas, Venezuela	1967	Cluff et al., 1973 [13]
Borrego Mountain, California	1968	Youd and Castle, 1970 [96]
San Fernando, California	1971	Dixon and Burke, 1973 [18] Seed et al, 1975 [80]
Haicheng, China	1974	Xie Junfei, 1979 [88]
Guatemala	1976	Hoose, 1976 [32] cited by Youd, 1977 [94]
Tangshan, China	1976	Xie Junfei, 1979 [88]
San Juan, Argentina	1977	Bruschi, 1978 [6]

water pressures in the field during earthquakes. However, more recent research has conclusively demonstrated that relative density is only one of several factors involved (Seed, 1976 [73], 1979 [74]). Based on these findings, Peck, (1979 [61]) has questioned the validity of laboratory cyclic tests as presently performed for predicting liquefaction potential, and has instead suggested reliance on empirical methods based on field exploration by standard penetration tests.

This report addresses the problem of pore water pressure buildup and liquefaction during earthquakes at level sites. It is generally agreed that the cause of pore water pressure buildup in saturated sands or cohesionless silts is the cyclic loading of the soil associated with the passage of seismic waves. Both loose and dense dry sands compact and settle when subject to cyclic shear loading, as illustrated in figure 1.2 (Silver and Seed, 1971 [83]). If the soil is saturated and the loading takes place in an undrained condition, the relative incompressibility of the pore water makes the rapid compaction of the sand impossible. Instead, an excess pore water pressure develops whose value increases with the duration of cyclic loading, and in many fine sands and silts these pressures only start dissipating after the ground shaking has ended. Some manifestations of liquefaction in the field, such as the occurrence of sand boils, and the differential settlement of structures due to uneven post-earthquake compaction of the foundation soil, can be explained by the presence of excess pore water pressures and associated water flow. Other manifestations of seismically-induced liquefaction, which are associated with large or unlimited shear straining of the soil, can be explained by the decrease in shear strength associated with these excess pore water pressures. This shear strength decrease, while obviously a very important aspect of the liquefaction problem, is outside the scope of this work. This report focuses on the pore water pressure buildup common to all manifestations of liquefaction at level sites during earthquakes.

The approach to the liquefaction problem presented in this report is based on the premise that pore water pressure buildup during cyclic shear loading of sand is controlled mainly by the magnitude of the cyclic shear strain. This premise leads to the conclusion that shear modulus, rather than relative density, is the main parameter controlling pore water pressure buildup in the field. An important practical consequence is that measurements of in situ modulus at small strains, which can be obtained from geophysical measurements of shear wave velocity, should be used for predicting pore pressures. This is in contrast with the present use of in situ relative density which: a) is not a clearly valid concept when applied to natural sand deposits because of their stratification (Castro, 1975 [9]); and b) cannot be measured directly in the field, but instead must be inferred from penetration tests. Therefore, the proposed strain approach, based on seismic shear strains, in situ measurements of shear modulus, and cyclic strain-controlled tests, is different from current practice, which is based on seismic shear stresses, in situ penetration measurements for relative density determinations, and stress-controlled tests.

Chapter 3 of this report describes the main features of the present state-of-the-art and discusses the need for the new cyclic strain approach. Chapters 4, 5 and 6 present results of studies performed to develop the cyclic

strain method, including a theoretical analysis using a particulate model of the sand, laboratory measurements, additional studies of the most important parameters used in the method, and a proposed engineering procedure to eliminate the potential for liquefaction at level sites during earthquakes.



Figure 1.1 Tilted Niigata buildings after earthquake

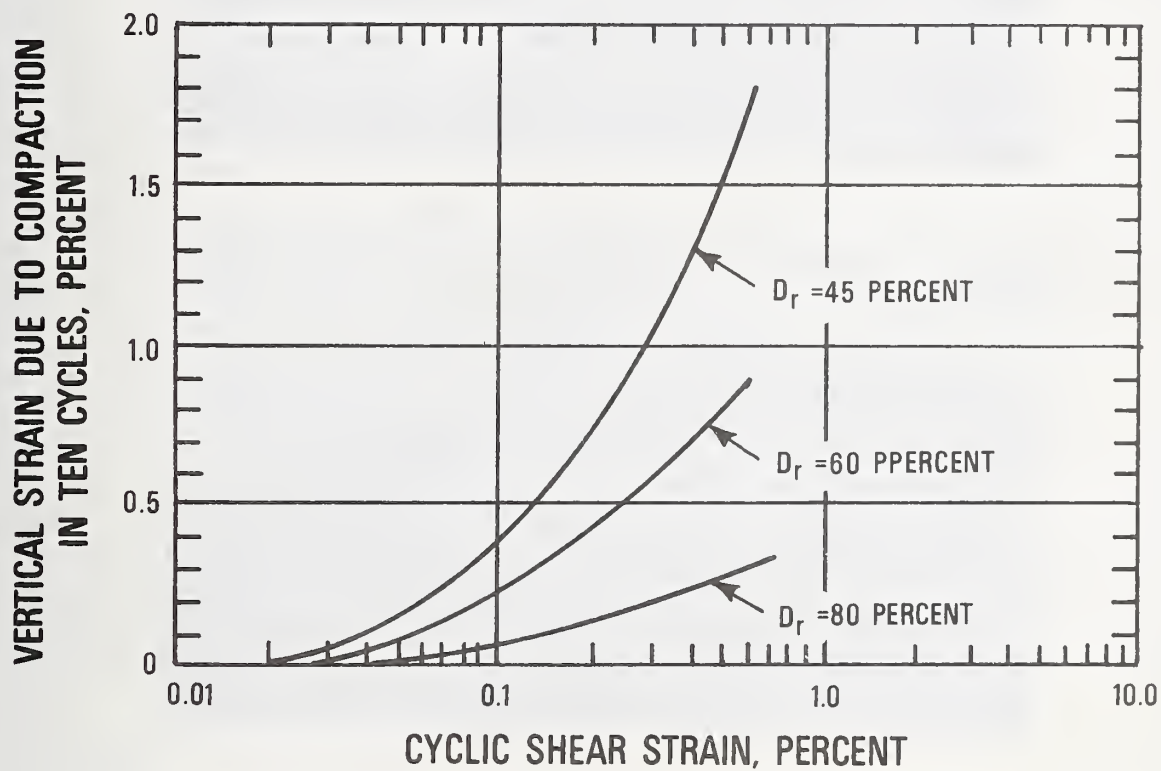


Figure 1.2 Settlement of a dry sand in cyclic strain controlled simple shear tests (Silver and Seed, 1971)

FACING PAGE: Detailed view of the fissures induced by liquefaction of the hydraulic fill in the San Fernando Dam during the February 1971 earthquake. The remaining embankment downstream of the failure had only a 4-ft. freeboard of highly fractured soil which was on the verge of failure and could have failed if the earthquake had lasted a few more seconds.



2. SCOPE

This report contains:

- (1) A review of present cyclic stress methods for predicting liquefaction potential of level sandy sites;
- (2) A proposed new approach to predicting liquefaction potential based on the correlation between cyclic strain and excess pore water pressure buildup;
- (3) The documentation for the existence of a threshold cyclic shear strain (γ_t), below which there is no excess pore water pressure buildup, and an explanation for the existence of γ_t by a particulate soil model;

- (4) The results of 12 undrained strain-controlled cyclic triaxial tests on Monterey No. 0 sand which are aimed at developing the basic parameters needed for the proposed strain approach to liquefaction, and a comparison of these results with measurements performed by others; and
- (5) A proposed design method for predicting the threshold peak ground surface acceleration, $(a_p)_t$, below which a site does not build up pore pressures and cannot liquefy.

Chapter 3 contains a review of the existing stress approach and a discussion of problems associated with its application. It also discusses the rationale for the proposed strain approach, as well as experimental evidence from prior work documenting the existence of the cyclic threshold strain, γ_t , and of a consistent correlation between cyclic strain and excess pore water pressure.

Chapter 4 contains a particulate model where the sand is represented by a simple cubic array of quartz spheres, and which predicts values of γ_t close to those observed experimentally.

Chapter 5 contains the results of 12 undrained strain controlled cyclic triaxial tests on Monterey No. 0 sand, performed under the direction of the second author of this report (Ladd). The tests include measurements at very small cyclic strains ($\gamma \approx 10^{-3}$ percent) and precise measurements of the threshold strain. Comparisons are also presented between the results of these tests and measurements performed by others.

Chapter 6 contains the derivation of a proposed design method based on the threshold strain, and on the derived concept of a "threshold peak ground surface acceleration," $(a_p)_t$, needed to start pore pressure buildup at a given site and saturated sand layer.

FACING PAGE: *Liquefaction-induced fissures and embankment failure observed after the Miyagi-ken-oki June 1978 earthquake.*



3. GENERAL APPROACH

3.1 STATE-OF-THE-ART (CYCLIC STRESS) APPROACH

3.1.1 General

The current state-of-the-art method to predict pore water pressure buildup and liquefaction potential during earthquakes in level sites has been developed to a large extent by Seed and his coworkers (Seed and Idriss, 1971 [78]; Seed et al., 1975 [80]; Seed, 1979 [74]). The following two main assumptions are made in this method:

- 1) The pore pressure developed at any saturated cohesionless soil element such as the one shown in figure 3.1(a) is caused by the cyclic shear stress, τ . This shear stress acts in the horizontal and vertical planes and is caused

by the passage of vertically propagating seismic shear waves. Figure 3.1(b) shows a typical variation of τ with time, $\tau(t)$, during ground shaking.

- 2) The loading of the soil by $\tau(t)$ is undrained (the pore water pressure dissipation and redistribution within the soil mass are disregarded within the time frame of the event). Therefore, the pore water pressure in the element in excess of the hydrostatic pressure, $\Delta u(t)$, increases with duration of shaking and is a maximum at the end of the shaking ($t=30$ seconds in figure 3.1(b)). Thus, the minimum value of the effective overburden pressure occurs also at the end of the shaking, and is $\sigma'_0 - \Delta u(30)$ where σ'_0 = initial effective overburden pressure. If $\Delta u(30) = \sigma'_0$, there is no effective stress in the soil and, by definition, "initial liquefaction" of the soil has occurred. If $\Delta u(30) < \sigma'_0$ "initial liquefaction" did not occur during the shaking.

Initial liquefaction has been extensively used as a criterion defining failure. Other criteria, based on the strain developed during stress-controlled tests, have also been used; however, the discussion herein is mainly restricted to the initial liquefaction concept. The ideal way to obtain the value of $\Delta u(30)$ would be: (i) to retrieve a perfectly undisturbed soil sample from the given depth, (ii) to consolidate a specimen in the laboratory to the effective field static pressures, σ'_0 and $K_0 \sigma'_0$, and (iii) to subject the saturated specimen to the seismic shear stress history, $\tau(t)$, in undrained condition, and monitor the development of the excess pore water pressure, $\Delta u(t)$. In practice this 3-step method cannot be implemented, and is replaced instead by the following, more manageable procedure:

- a) $\tau(t)$ is replaced by n cycles of a sinusoidal shear stress of uniform amplitude, τ_c . This cyclic stress, τ_c is taken as a fraction of the peak value, τ_p of $\tau(t)$. Usually, $\tau_c = 0.65 \tau_p$ is used. Therefore, $\tau(t)$ is replaced by n cycles of τ_c , and the value of n is selected so that Δu at the end of the n cycles is approximately equal to Δu at the end of $\tau(t)$.
- b) A disturbed soil sample is retrieved from the depth of interest, and is reconstituted in the laboratory to the same relative density, D_r , it had in the field. Field D_r is usually estimated from the measured standard penetration resistance, N , using available correlations between N , σ'_0 , and D_r such as that of Gibbs and Holtz, (1957 [26]).
- c) The reconstituted sample is consolidated under stresses approximating the free field effective pressures (usually this means isotropic consolidation under σ'_0).

Then, an undrained stress controlled test is performed where n cycles of the uniform cyclic shear stress, τ_c , are applied to the sample in an undrained condition, while monitoring the excess pore water pressure buildup, Δu . If $\Delta u = \sigma'_0$ at the end of the n cycles, the sample has experienced initial liquefaction. This result is then used to predict the occurrence of the initial liquefaction in the field.

Usually, several stress-controlled, cyclic laboratory tests such as described in (c) are performed on identical reconstituted samples having equal D_r and consolidated under the same σ'_0 . The cyclic stress, τ_c , is varied between tests, and the number of cycles, n , needed to produce initial liquefaction is obtained from each test. The curve of τ_c versus n is used for the prediction of liquefaction in the field. Figure 3.2 shows an example of such a curve obtained from cyclic simple shear tests. The value of τ_c from the curve for a given n (also called the cyclic strength of the soil) is compared with the average τ_c developed by the earthquake, and the liquefaction potential in the field is evaluated from this comparison. This comparison is illustrated in figure 3.3.

The shear stress history, $\tau(t)$, and the derived τ_c value shown in figure 3.1(b) are sometimes obtained from site response analyses. In those analyses, assumed ground motions are input at rock or at some depth within the soil, and a shear beam model of the soil profile is used for the computations of seismic shear stresses, strains and accelerations at different depths within the soil (i.e., Schnabel et al., 1972 [71]). In this case, the calculated $\tau(t)$ is a function of the input motions and of the geometry and stress-strain properties of the soil model.

3.1.2 The Simplified (Seed and Idriss) Procedure

A further simplification of the cyclic stress approach described in section 3.1.1 has been proposed by Seed and Idriss (1971 [78]). This simplified procedure is widely used in engineering practice. It has the advantage of using a limited number of parameters which are usually available, and not requiring the use of a computer.

In this simplified procedure, the liquefaction potential of a soil element at a depth z is evaluated in three steps as follows:

Step 1. Determination of τ_c and n . This is done by computing the stress ratio, τ_c/σ'_0 caused by earthquake by means of equation 3.1:

$$\frac{\tau_c}{\sigma'_0} = 0.65 \frac{a_p}{g} \frac{\sigma_0}{\sigma'_0} r_d \quad 3.1$$

where:

- a_p = horizontal peak acceleration at the ground surface
- g = acceleration of gravity = 32.2 ft/sec²
- σ_0, σ'_0 = total and effective overburden pressures at depth z
- $r_d = r_d(z)$ = stress reduction factor varying from a value of one at $z=0$ to values below 0.7 at $z=100$ ft. (see fig. 3.4)

The earthquake is assumed to induce in the soil n cycles of uniform cyclic stress, τ_c . The value of n is related to the magnitude, M of the earthquake, and is equal to about 10 cycles for $M=7$. Figure 3.5 presents the most recent relationship between M and n proposed by Seed et al., (1975a [81]).

Step 2. Determination of $(\tau)_{Dr}$ causing initial liquefaction (cyclic strength of soil). The value of uniform cyclic stress causing initial liquefaction in n cycles, $(\tau)_{Dr}$ is assumed to be a function of n , and of the relative density and grain size of the soil. $(\tau)_{Dr}$ is obtained from equation 3.2:

$$\frac{(\tau)_{Dr}}{\sigma'_o} = \frac{\sigma_{dc}}{2\sigma'_o} \cdot \frac{1}{50} \cdot C_r \cdot \frac{D_r}{50} \quad 3.2$$

where: $(\tau)_{Dr}/\sigma'_o$ = the cyclic shear strength ratio for a given relative density, D_r

σ_{dc} = the cyclic deviator stress

50 = signifies a relative density of 50 percent

D_r = field relative density in percent

$\left(\frac{\sigma_{dc}}{2\sigma'_o}\right)_{50}$ = the shear stress ratio causing liquefaction in the laboratory in a stress-controlled cyclic triaxial test, for $D_r = 50$ percent

C_r = a correction factor relating the cyclic shear strength obtained in a triaxial test to that anticipated under typical field conditions.

$(\sigma_{dc}/2\sigma'_o)_{50}$ and C_r are obtained from appropriate charts once n , D_r , and the grain size of the sand are known. D_r is obtained from the standard penetration resistance, N , using the Gibbs and Holtz correlation.

Step 3. Comparison between τ_c and $(\tau)_{Dr}$. The values of τ_c and $(\tau)_{Dr}$ obtained from equations 3.1 and 3.2 are compared. If $\tau_c > (\tau)_{Dr}$ liquefaction at depth z is predicted by the method. If $\tau_c < (\tau)_{Dr}$ no liquefaction is predicted.

The simplified procedure has all the main features of the general stress approach discussed in section 3.1.1. Note the importance given to the relative density of the soil in this method.

3.1.3 Empirical Charts and Correlations

After the 1964 Niigata earthquake, it was observed that the occurrence and degree of damage caused by liquefaction were well correlated with measurements of the standard penetration resistance, N , performed before the earthquake (Kishida, 1966 [36]; Ohsaki, 1966 [56]). Based on this observation, some empirical correlations were obtained which are summarized in figure 3.6. Figure 3.6 is directly applicable to a site having subsoil conditions similar to those in Niigata and experiencing a ground shaking similar to that which occurred in Niigata in 1964. More general correlations and charts, applicable to wider ranges of soil and shaking conditions, have been proposed by Whitman, 1971 [86]; Seed and Idriss, 1971, [78]; Castro, 1975 [9]; Christian and Swiger, 1975 [12]; Yegian and Whitman, 1978 [91]; and Seed, 1979 [74]. In all cases, these authors have calibrated their proposed correlations with documented case histories where liquefaction has (or has not) occurred. Tables containing the values of N and of other basic parameters of up to 50 case histories have been presented by Seed and Idriss, 1971 [77]; Seed et al., 1975 [80]; and Yegian, 1976 [90].

Figures 3.7 through 3.9 present some of these empirical correlations. In all of these figures, the stress ratio caused by the earthquake is obtained from the peak ground surface acceleration using an expression such as equation 3.1. Other parameters needed to use the charts are N , σ'_0 , and the earthquake magnitude, M (for fig. 3.9). In these three figures, the measured value of N must be corrected for the effect of overburden pressure. In figure 3.7 the corrected value, N' , defined in the figure, is used. The corrected N_1 value used in figures 3.8 and 3.9 is calculated using equation 3.3.

$$N_1 = \left(1 - 1.25 \log \frac{\sigma'_0}{2000} \right) N \quad 3.3$$

where σ'_0 is in psf.

It must be noted that the corrections used to calculate N' and N_1 in figures 3.7 through 3.9 are very similar except for a constant factor. For a wide range of pressures, $500 \text{ psf} < \sigma'_0 < 4,000 \text{ psf}$, $N_1 \approx 0.5 N'$.

The original use of N as a basis for the development of empirical liquefaction correlations was based on two assumptions: (i) the paramount importance attributed to relative density in controlling the rate of development of excess pore water pressures in the field, and (ii) the belief that N measures relative density in the field. As discussed in section 3.1.1 of this report, both assumptions (i) and (ii) have been challenged; however, this challenge does not affect the proven success of N and of the empirical correlations as tools to organize liquefaction case histories and to evaluate liquefaction potential. Therefore, what is needed is an improved and more basic understanding of standard penetration test (SPT) measurements in cohesionless soils, and of the relation between these measurements and the factors controlling liquefaction. The results of recent research on the SPT along these lines by Kovacs, 1975 [40], and Kovacs et al., 1981 [41]; Schmertmann, 1977 [69] and Schmertmann and Palacios, 1979 [70] represent a very promising start towards this objective.

3.2 PROPOSED CYCLIC STRAIN APPROACH

3.2.1 Problems with the Stress Approach

The current cyclic stress approach to liquefaction described above is based on the premise that the pore water pressure buildup in a saturated sand, subjected to a given cyclic shear stress history, is mainly a function of the relative density D_r and the initial effective stresses acting on the sand. The influence of the density on cyclic strength of reconstituted sand was first observed in 1965 (see fig. 3.10). Therefore, this parameter was incorporated by specifying that the cyclic tests should be done on reconstituted samples compacted to the estimated field density. The assumption that cyclic strength is mainly a function of relative density, is also used in the simplified procedure described in section 3.1.2.

However, cyclic tests performed in the last few years have revealed that a number of other factors besides D_r also influence significantly the results of

stress-controlled tests. Some of these factors, which were recently discussed in detail by Seed, 1979 [74], are listed in table 3.1.

Experimental results showing the significance of the last four factors of table 3.1 on the cyclic strength of reconstituted sands are plotted in figures 3.11 through 3.14. These figures show that the effect of these factors can be even more significant than that caused by large variations in density. Most of the evidence showing the influence of time under pressure, overconsolidation, prestraining and fabric on cyclic strength is from laboratory tests. However, some limited evidence from the field suggest that the geological age of the soil deposit influences liquefaction potential and should be considered (Ohsaki, 1969 [57]; Youd et al., 1978 [98]; Finn, 1979 [24]). Seed, 1976 [73] has pointed out that "...the liquefaction characteristics of in situ sand deposits are determined by a number of complex factors, of which relative density is only one, and careful evaluation of all these factors is required in selecting soil characteristics for use in design."

The influence of all these factors on the cyclic strength of sands certainly complicates the state-of-the-art and makes its practical use more difficult. Efforts can be made to simulate as closely as possible the geological and seismic history of the soil when testing reconsolidated samples in the laboratory. The specimens can be reconsolidated, prestrained, and aged under pressure prior to cyclic loading. However, this complicates the tests and requires information that may not be available. Besides, there are limits to what can be done on a reconstituted sample. Laboratory aging under pressure cannot possibly simulate the hundreds or thousands of years of history of many soil deposits. The fabric effect introduces an additional and serious problem, since there is yet no reliable method to measure sand fabric in the field.

Testing undisturbed samples of cohesionless soils and performing the cyclic tests on them rather than using reconstituted specimens would solve this dilemma. Unfortunately, the factors included in table 3.1 appear to be very sensitive to sampling and handling of sands prior to testing (Seed, 1979 [74]).

Peck, 1979 [61], has tentatively concluded that: "(1) unless the cyclic loading tests used to evaluate liquefaction potential can be performed on absolutely undisturbed samples, which is manifestly impossible, the results will probably indicate too great a likelihood of liquefaction; and (2) in many instances the resistance to liquefaction in the field may be appreciably, even spectacularly, greater than that determined on the basis of conventional cyclic laboratory tests on reconstituted or even "undisturbed" samples if no allowances are made for various possible beneficial effects such as time, repeated small shearing forces, and stress history." Based on these conclusions, Peck proposes at this time to rely more on empirical correlations based on field standard penetration measurements, rather than using cyclic laboratory tests.

Table 3.1. Some Factors Influencing the Cyclic Strength of Sands

- Relative Density
- Method of Sample Preparation (Fabric Effect)
- Prior Seismic Straining (Prestraining or Preshaking Effect)
- Lateral Earth Pressure Coefficient (K_o) and Overconsolidation Ratio (OCR)
- Increased Time Under Pressure (Aging Effect)

3.2.2 Why a Strain Approach?

The main premise of this report is that a cyclic strain approach to the problem of predicting pore water pressure buildup and liquefaction of saturated cohesionless soils would have significant advantages over the current cyclic stress approach. Evidence substantiating this statement, which was available at the outset of this research, is discussed in this and the following sections.

Silver and Seed, 1971 [83] showed experimentally that cyclic shear strain, $\gamma_c = \tau_c/G$ (G = secant shear modulus) rather than cyclic shear stress, τ_c , controls the densification of dry sands. Strain-controlled cyclic simple shear tests were performed by Silver and Seed on Dry Crystal Silica No. 20 sand using a range of relative densities, D_r , of overburden pressures, σ'_0 , and of cyclic shear strains, γ_c . It was found that the rate of settlement with number of cycles depended on D_r and γ_c , but was independent of σ'_0 , and did not correlate with τ_c and G taken independently. Some results of these tests are summarized in figure 1.2. Based on the Seed and Silver results, Martin et al., 1975 [49] successfully developed a cyclic strain, effective-stress model to predict pore water pressure buildup in saturated sands during undrained stress-controlled tests. All of these findings strongly suggest that γ_c , rather than τ_c , controls both densification and liquefaction in sands.

Based on cyclic test results on dry sands, Drnevich and Richart, 1970 [23] Youd, 1972 [92] and Pyke, 1973 [64] concluded that there is a threshold cyclic shear, γ_t , of the order of 10^{-2} percent, below which no densification occurs (see fig. 3.15). A value of γ_t of about 10^{-2} percent is also consistent with the experimental results for dry sand shown in figure 1.2, and with strain-controlled tests results on saturated sands reported by Park and Silver, 1975 [59], and Dobry and Ladd, 1980 [20], and will be discussed in more detail in section 3.2.3. A theoretical study of a simple granular model of a quartz sand, originally proposed by Dobry and Swiger, 1979 [21], and presented in detail in chapter 4, predicts a range of values for this threshold strain, 1×10^{-2} percent $< \gamma_t < 4 \times 10^{-2}$ percent for effective confining pressure between 500 psf and 4,000 psf (24 and 192 kPa). The existence of a threshold level at which pore water pressure buildup starts is obviously very important for liquefaction prediction. The fact that this threshold has a more stable value when expressed as a strain than when expressed in terms of stress is another argument in favor of a strain approach to liquefaction.

The adoption of a cyclic strain approach should considerably simplify the interpretation of cyclic laboratory tests on saturated sands. There is experimental evidence indicating that the factors presented in table 3.1 which increase the cyclic strength of sands in stress-controlled tests, also increase the shear modulus of sands (Seed and Idriss, 1971 [78]; Drnevich and Richart, 1970 [23]; Hardin and Drnevich, 1972 [29]; Pyke, et al., 1974 [65]; Anderson and Stokoe, 1977 [3]; Dobry and Ladd, 1980 [20]). This evidence suggests that, if both τ (cyclic shear strength) and G are similarly affected by the factors listed in table 3.1, the ratio $\gamma = \tau/G$ should be less affected by these same factors. Therefore, the pore water pressure buildup in strain-controlled tests should be less sensitive to those factors than in stress-controlled tests. A more detailed discussion of this premise is presented in section 3.2.3.

The advantage gained by adopting a strain approach to liquefaction would be the total or partial replacement of the parameters listed in table 3.1 by the shear modulus, G . Unlike relative density or sand fabric, the shear modulus at small strains, G_{max} , can be directly measured in the field by means of the shear wave propagation velocity. Field measurements of G_{max} would automatically incorporate many of the characteristics of the soil deposits which are important for pore water pressure buildup and liquefaction during earthquakes. This approach should, therefore, decrease the need for a detailed knowledge of the geological and seismic history of the site which is presently required in the stress approach.

There is still another argument in favor of the strain approach, which relates to the advantages of running cyclic strain - instead of stress-controlled tests of dense (dilative) sands. Castro (1975 [9]) has shown that, for cyclic triaxial stress-controlled tests on these soils, there is a substantial redistribution of water content within the specimen, most of which probably occurs near the end of the test, when the cyclic strain becomes large. This redistribution affects the cyclic behavior of the dense sand specimen in such a way that it ceases to represent the field situation; in particular, the "strains measured in the laboratory in such a case are so conservatively large as to make the test unusable as a design tool," Castro and Poulos, 1980 [11]. Strain-controlled tests of dense sands, performed at smaller cyclic strains, which are more representative of those in situ, should decrease the redistribution problem. Although more research is needed on the subject, it seems reasonable to expect that running strain-controlled tests of dense sands, at those smaller representative strains will: (a) cause less water content redistribution before initial liquefaction occurs, and (b) provide more realistic predictions of in situ pore pressures than those obtained from stress-controlled tests (see also Peck, 1980 [62]).

3.2.3 Analysis of Available Cyclic Test Results

This section analyzes and discusses some available stress- and strain-controlled cyclic triaxial test results on saturated sands from the viewpoint of the proposed cyclic strain approach. These results relate mainly to the fabric effect listed in table 3.1, and were obtained from the files of one of the authors of this report (Ladd) and from Park and Silver, 1975 [59].

The first data set was obtained from Ladd's files. It corresponds to stress-controlled tests on a saturated sand compacted to $D_r \approx 83$ percent by different sample preparation methods. The sand used is the same as the soil called "Sand No. 2" by Ladd, 1977 [43], and its grain size distribution is shown in figure 3.16. The cyclic triaxial strength data for initial liquefaction are plotted in the usual way (i.e., cyclic stress ratio versus n) in figure 3.17 for the two sample preparation methods used: Moist Vibration and Dry Tamping (see Ladd, 1977 [43] for a description of the two methods). Figure 3.17 shows again in a very dramatic way the effect of sand fabric, which was already illustrated in figure 3.11. The moist vibration specimens have much larger cyclic strengths than the dry tamping specimens. The explanation for this is that the sand compacted by moist vibration was stiffer, and therefore developed smaller cyclic strains than that compacted by dry tamping. This is

illustrated by the data in figure 3.18, which correspond to the same stress-controlled tests of figure 3.17. Figure 3.18 shows the maximum amplitudes of cyclic axial stress and strain, corresponding to the first compression and extension excursions, for both moist vibration and dry tamping tests. Two conclusions can be drawn from figure 3.18: (a) the specimens are stiffer in compression than in extension for both compaction methods, and (b) moist vibration specimens are stiffer than dry tamping specimens, with the difference being much larger in extension. For example, the two dry tamping tests corresponding to cyclic stress ratios, $R = 0.36$ and 0.37 , developed in their first extension excursion axial strains of almost one percent and failed in only 8 to 12 cycles (see fig. 3.17); on the other hand, a moist vibration specimen tested at a similar stress, $R = 0.41$, developed in its first extension excursion a lower strain (≈ 0.4 percent) and failed in 24 cycles. In figure 3.19, the same results of figure 3.17 have been replotted using the axial strain in the first extension excursion, ϵ_v , as a parameter, instead of the cyclic stress ratio of the test, R . The difference between dry tamping and moist vibration data points is much less in figure 3.19 than in figure 3.17. Although there is still considerable scatter in figure 3.19, it was possible to define a single curve representing all the data points. Therefore, an important reason for the lower cyclic strength exhibited in figure 3.17 by the dry tamping specimens is that they were less stiff, especially in extension, and were thus subjected to larger cyclic strains starting from the very beginning of cyclic loading.

Figures 3.20 through 3.23 present results from stress-controlled and strain-controlled cyclic triaxial tests on saturated Crystal Silica No. 20 sand, performed by Park and Silver, 1975 [59]. The grain size distribution of the sand used is shown in figure 3.16. All tests were conducted on specimens compacted at $D_r = 60$ percent using two preparation methods: Dry Vibration and Wet Rodding. The effective confining pressure in all tests was $\sigma'_3 = 2,000$ psf (96 kPa).

The cyclic strength results from the stress-controlled tests are presented in the usual way in figure 3.20. Again, the effect of fabric is apparent with the Dry Vibration specimens being significantly weaker. For a given stress ratio, the Wet Rodding specimens needed 15 to 20 times more cycles to fail than the Dry Vibration specimens (e.g., at $R = 0.30$, $n = 30$ cycles and 2 cycles, respectively). Figure 3.21 gives additional information on pore water pressure buildup during the same stress-controlled tests. Figure 3.21 again shows that the rate at which pore water pressure built up was much slower for the Wet Rodding specimens.

The reason for the differences in stress-controlled test results shown in figures 3.20 and 3.21 is, again, that Wet Rodding specimens were stiffer, and therefore developed smaller cyclic strains than the Dry Vibration specimens.

This difference is illustrated by the comparison of the stress-strain curves in the first cycle plotted in figure 3.22. For this case, no information was available to plot separately the first compression and extension excursions, as was done in figure 3.18 for sand No. 2. The difference between the curves in figure 3.22 is similar to that between the curves in figure 3.18.

Therefore, for both Crystal Silica sand and sand No. 2, the effect of fabric on cyclic strength, as measured in stress-controlled tests, seems to be largely a stiffness effect. A stiffer fabric, which develops lower cyclic strains from the beginning of cyclic loading, also develops less pore water pressures and, thus, liquefies in a larger number of cycles.

The results of strain-controlled cyclic triaxial tests, performed by Park and Silver on the same Crystal Silica sand, compacted to the same relative density, using the same specimen preparation procedures and under the same confining pressures as those used for the above-mentioned stress-controlled tests are shown in figure 3.23. This figure shows the rate of pore water pressure buildup at different cyclic axial strains, ϵ_v , during the strain-controlled tests, and here also, the effect of fabric is minor and has been reduced to a scatter measured by the width of the hatched areas in the figure. Figure 3.23 demonstrates quite clearly that the rate of pore water pressure buildup with number of loading cycles is essentially the same for both Dry Vibration and Wet Rodding specimens, provided that the same cyclic strains are used. A comparison between figures 3.21 and 3.23 shows again that the fabric effect on pore pressure buildup is very pronounced for stress-controlled tests (figure 3.21), while it is practically nonexistent if strain-controlled tests are performed (figure 3.23).

The lowest value of cyclic axial strain, ϵ_v , used by Park and Silver in their strain-controlled tests was 3×10^{-2} percent. Using a Poisson's Ratio for the saturated sand, $\nu = 0.5$, it yields a cyclic shear strain, γ_c of:

$$\gamma_c = 1.5 \epsilon_v \quad 3.4$$

or, the lowest shear strain was $\gamma_c = 4.5 \times 10^{-2}$ percent. For this value of cyclic shear strain, the rate of pore water pressure buildup was very slow. As shown in figure 3.23, for $\epsilon_v = 3 \times 10^{-2}$ percent, $\Delta u/\sigma'_3 \leq 0.20$ even after 100 cycles. This, added to the shapes of the curves in figure 3.23, again suggests the existence of a threshold strain, γ_t near 10^{-2} percent as discussed in section 3.2.2.

All results presented in figures 3.20 through 3.23 were performed by Park and Silver on fresh specimens, i.e., each cyclic test was conducted on a new sample. They also performed strain-controlled staged tests on specimens compacted using the Dry Vibration procedure. In each stage, 300 cycles of a given cyclic strain were applied undrained, with the pore water pressure buildup being monitored. After this cyclic loading, the drainage valves were opened and the sample was reconsolidated under the same confining pressure, $\sigma'_3 = 2,000$ psf (96 kPa). The valves were then closed, and in this new undrained stage, 300 cycles of a larger cyclic strain were applied. The process was repeated at several cyclic strains. A comparison between the results of the staged tests and those on fresh specimens indicates that the pore water pressure buildup versus number of cycles, n , was essentially identical if pore pressure in the previous stages had been kept small, $\Delta u/\sigma'_3 \leq 0.4$. Therefore, the values of $\Delta u/\sigma'_3$ after $n = 10$ cycles for fresh specimens obtained from figure 3.23 have been plotted in figure 3.24, together with those from staged specimens for which $\Delta u/\sigma'_3 \leq 0.4$. In figure 3.24, shear strain γ_c rather than axial strain, ϵ_v , has been plotted, with

equation 3.4 used to compute γ_c . Similar results from staged strain-controlled cyclic triaxial tests on sand No. 1, obtained from the files of one of the authors of this report (Ladd) have also been superimposed on figure 3.24. The grain size distribution of sand No. 1 is shown in figure 3.16. The specimens of sand No. 1 were compacted to $D_r \approx 60$ percent using the Moist Tamping technique, and isotropically consolidated to effective confining pressures of $\sigma'_3 = 10$ psi (69 kPa) and $\sigma'_3 = 20$ psi (138 kPa). Figure 3.24 includes results of strain-controlled tests on sand No. 1 using cyclic shear strains, $\gamma_c < 10^{-2}$ percent. These small strain measurements were done by the use of the technique described in section 5.1.2 of this report. At these small strains, $\Delta u/\sigma'_3 = 0$ after $n = 10$ cycles, and figure 3.24 again suggests a threshold, $\gamma_t \approx 10^{-2}$ percent.

Figure 3.24, which was included in a recent publication by Dobry and Ladd, 1980 [20], is remarkably consistent. Although it includes results of cyclic tests conducted on two different sands, on normally consolidated specimens prepared at two different laboratories using different techniques, and for a range of confining pressures between 1,400 and 2,800 psf (69 to 138 kPa), one single curve fits all results reasonably well. The threshold strain, $\gamma_t \approx 10^{-2}$ percent is one important feature of this curve. The clear and consistent picture of pore water pressure buildup provided by figure 3.24 is simpler than data that can be obtained from stress-controlled tests on the same sands. Figure 3.24 gives a clear indication of the potential usefulness of the cyclic strain method.

3.2.4 Proposed Cyclic Strain Method

Instead of using the seismic (cyclic) shear stress, τ_c (or the stress ratio τ_c/σ'_0), it is suggested to use the seismic (cyclic) shear strain, γ_c , for the purpose of evaluating liquefaction potential. There seems to be three possible ways of obtaining γ_c at a given depth z of a soil profile and for a given seismic excitation:

- a) From the equation $\gamma_c = \tau_c/G$. This equation assumes that the seismic shear stress τ_c at depth z is known. The value of τ_c can be computed from an expression such as equation 3.1 if the ground surface acceleration is known.
- b) From site response studies where a model of the soil is subjected to an input earthquake motion, and the strains, stresses and motions within the model are calculated (e.g., Schnabel et al., 1972 [71]).
- c) From the ground particle velocity, V , and using the expression $\gamma = V/c$, where c is the propagation velocity of the relevant seismic wave, and which is often (although not always) taken as $c = (G/\rho)^{1/2}$ (ρ = mass density of the soil). This method has been used extensively to predict ground shear distortions near pipelines during earthquakes (e.g., see Newmark, 1967 [55]).

A common feature of procedures (a) through (c) is that they all explicitly include the stress-strain or stiffness properties of the soil in the calculation. This is in contrast with the cyclic stress approach to liquefaction, where the stiffness of the soil is not explicitly considered. Generally speaking, a stiffer soil having a larger value of G will experience a smaller cyclic strain and will develop less pore pressures.

The present report will focus on procedure (a) to calculate γ_c . The use of procedure (a) permits the formulation of a cyclic strain method for evaluating liquefaction potential along the lines of the original Seed and Idriss (stress) method, described in section 3.1.2. The steps of the proposed strain method to evaluate the liquefaction potential of a sand layer at a depth z are the following:

Step 1. Determination of γ_c and n . γ_c is calculated using equation 3.5

$$\gamma_c = 0.65 \frac{a_p}{g} \frac{\sigma_o r_d}{G_{\max} (G/G_{\max}) \gamma_c} \quad 3.5$$

Equation 3.5 is similar to equation 3.1, however; equation 3.5 considers the stiffness of the soil, G , while equation 3.1 does not.

The meaning of each symbol in equation 3.5 is given below:

- a_p = peak horizontal acceleration at the ground surface
- g = acceleration of gravity
- σ_o = total overburden pressure at depth z
- r_d = $r_d(z)$ = stress reduction factor with depth plotted in figure 3.4
- G_{\max} = shear modulus of the soil at very small cyclic strain, $\gamma_c \approx 10^{-4}$ percent
- $(G/G_{\max}) \gamma_c$ = effective modulus reduction factor of the soil corresponding to the cyclic strain, γ_c .

The equivalent number of cycles n is obtained from the magnitude of the earthquake, M .

Step 2. Comparison between γ_c and the threshold strain of the soil, γ_t . If $\gamma_c < \gamma_t$, neither pore pressure buildup nor liquefaction will occur and the evaluation ends here.

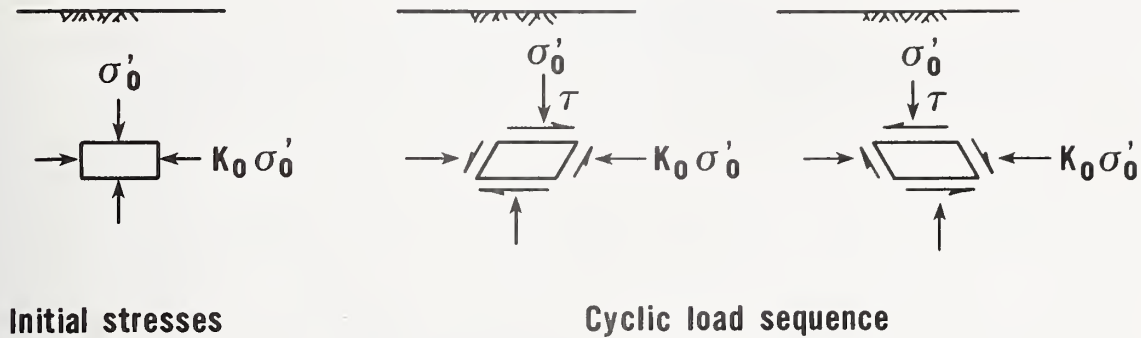
Step 3. If $\gamma_c > \gamma_t$, the values of γ_c and n should be used in conjunction with experimental curves similar to that shown in figure 3.24, to estimate the value of the pore pressure buildup at the end of the earthquake, $\Delta u/\sigma'_0$, where σ'_0 = initial effective overburden pressure at depth z .

Step 4. The value of $\Delta u/\sigma'_0$ estimated in step 3 is used to decide if the site will experience initial liquefaction ($\Delta u/\sigma'_0 = 1.0$) or not ($\Delta u/\sigma'_0 < 1.0$).

For the case of $\gamma_c > \gamma_t$ in steps 3 and 4 above, $(G/G_{\max}) \gamma_c$ in equation 3.5 is a function of both γ_c and the current pore pressure buildup, $\Delta u/\sigma'_0$. Therefore, the relation $(G/G_{\max}) \gamma_c$ and γ_c keeps changing during the earthquake. Obviously, some additional research is needed to develop definite rules for computing γ_c , as well as to refine other aspects of the proposed cyclic strain method, for the case of $\gamma_c > \gamma_t$.

The rest of this report presents results of studies and laboratory tests conducted to develop the necessary information for the use of the proposed cyclic strain method.

a. IDEALIZED FIELD LOADING CONDITIONS



b. SHEAR STRESS VARIATION DETERMINED BY RESPONSE ANALYSIS

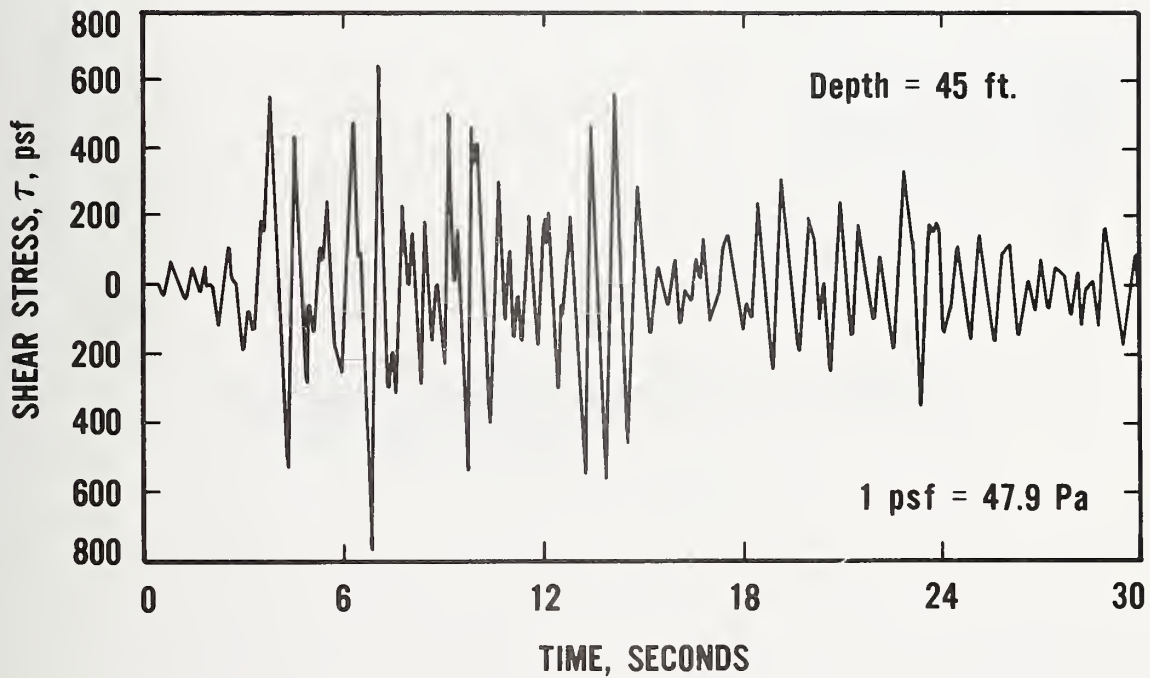


Figure 3.1 Cyclic shear stresses on a soil element during ground shaking (Seed et al., 1975)

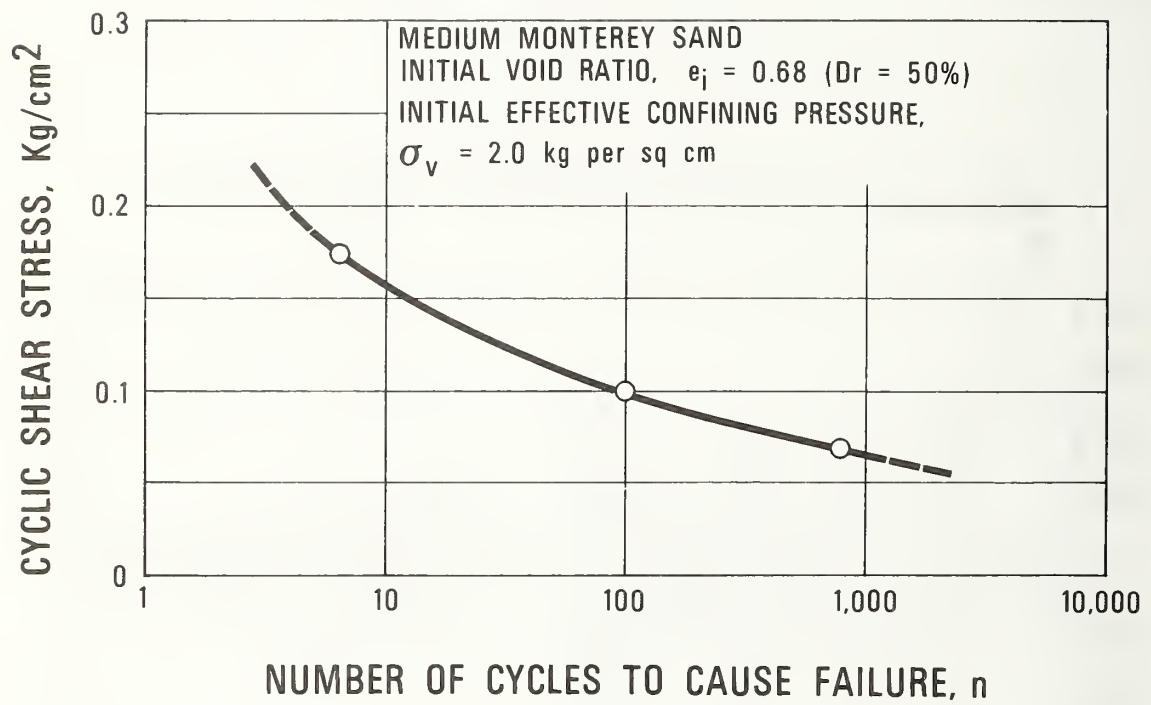


Figure 3.2 Typical form of the relationship between pulsating shear stress and the number of cycles to cause failure - simple shear conditions (Peacock and Seed, 1967)

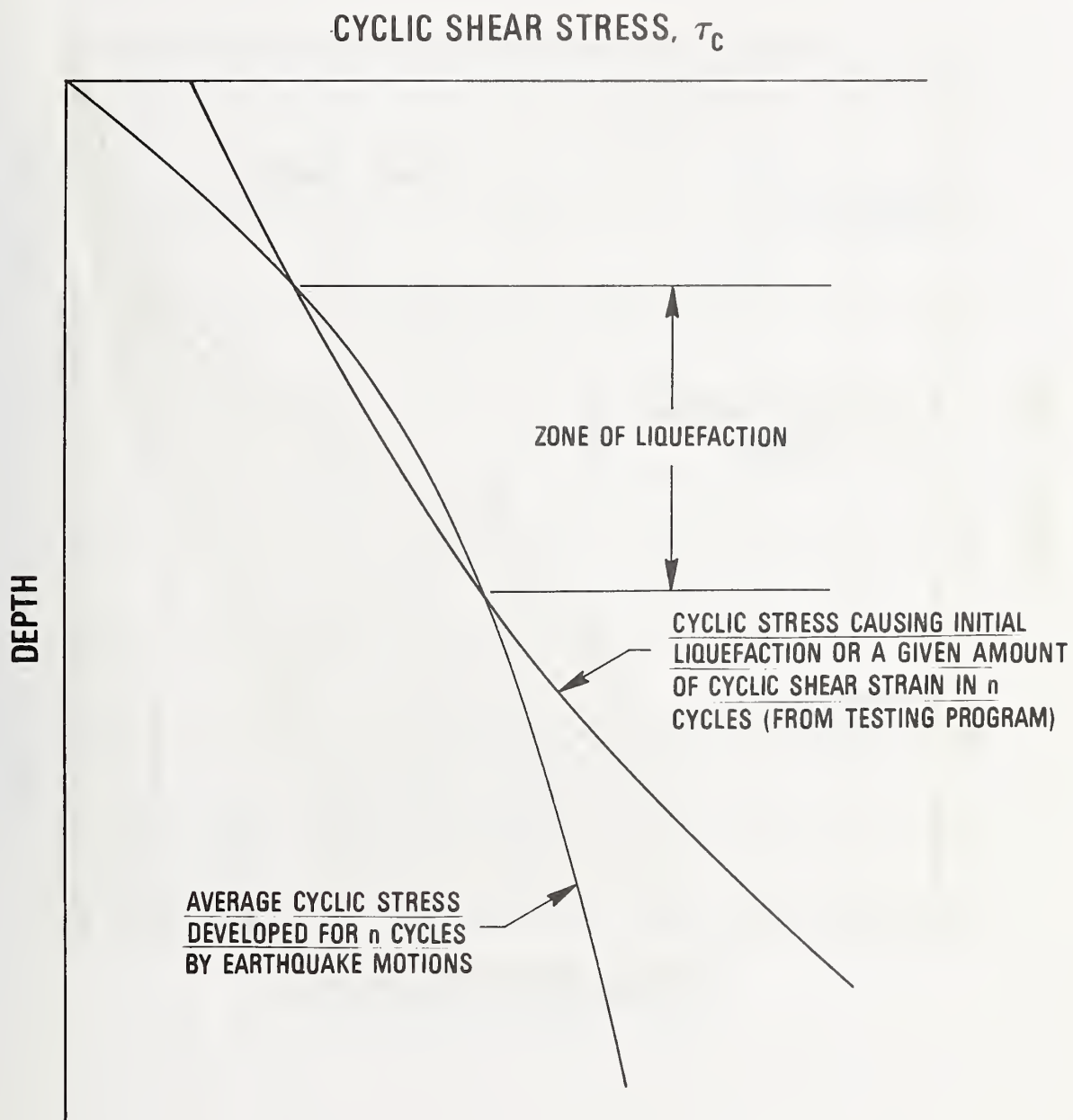


Figure 3.3 Cyclic stress method for evaluating liquefaction potential (Seed et al., 1975)

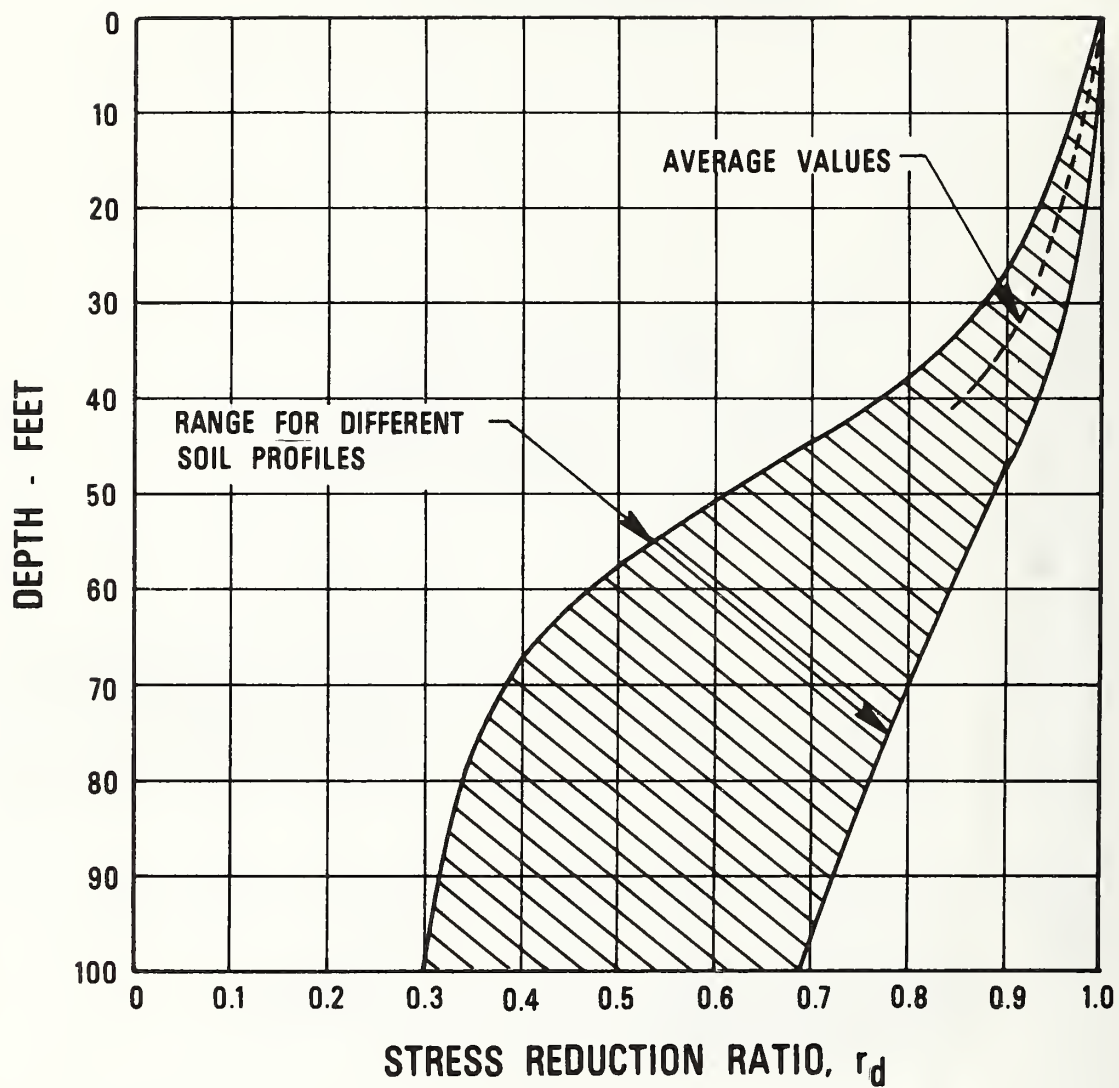


Figure 3.4 Range of values of stress reduction ratio, r_d , for different soil profiles (Seed and Idriss, 1971)

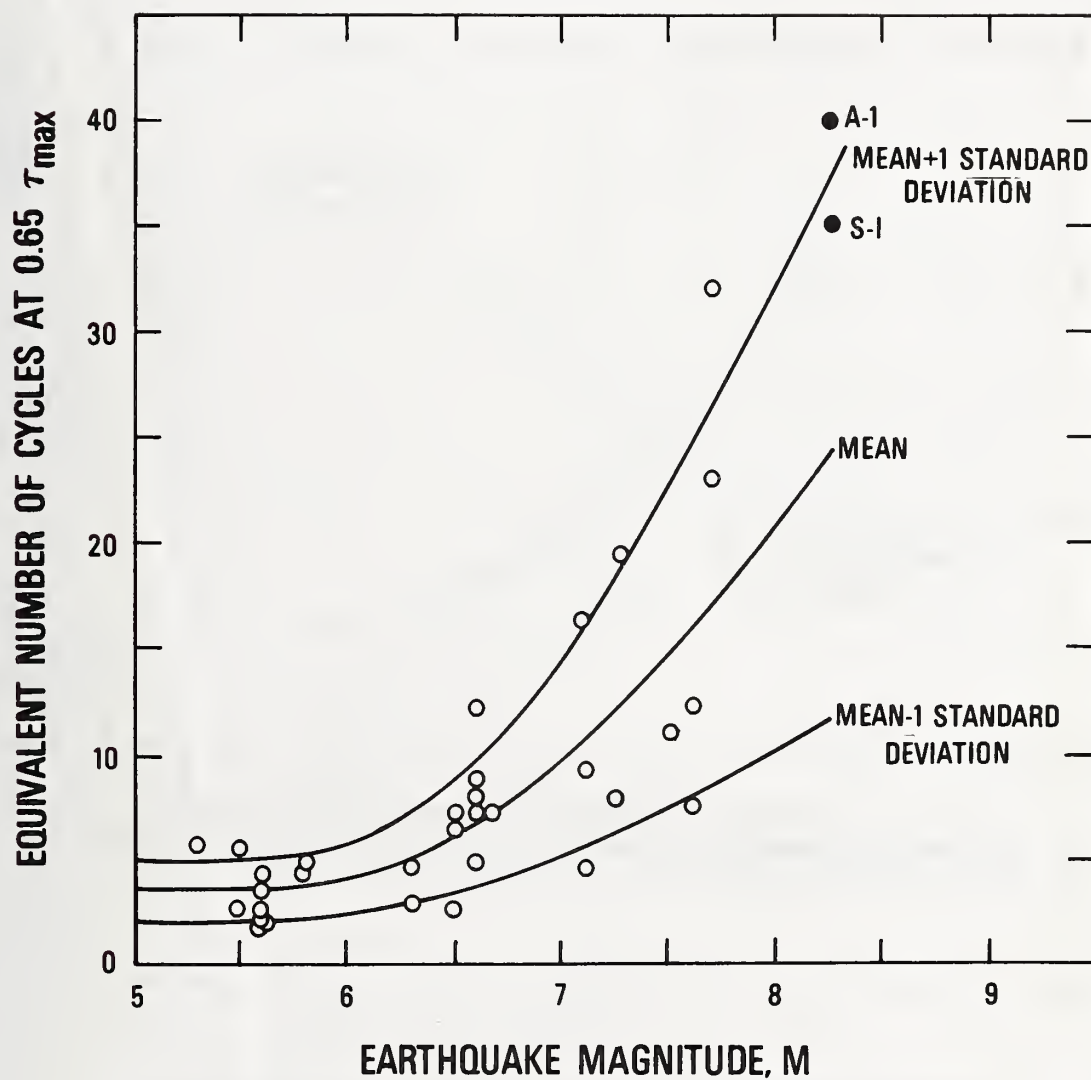


Figure 3.5 Equivalent numbers of uniform stress cycles based on strongest components of ground motion (Seed et al., 1975a)

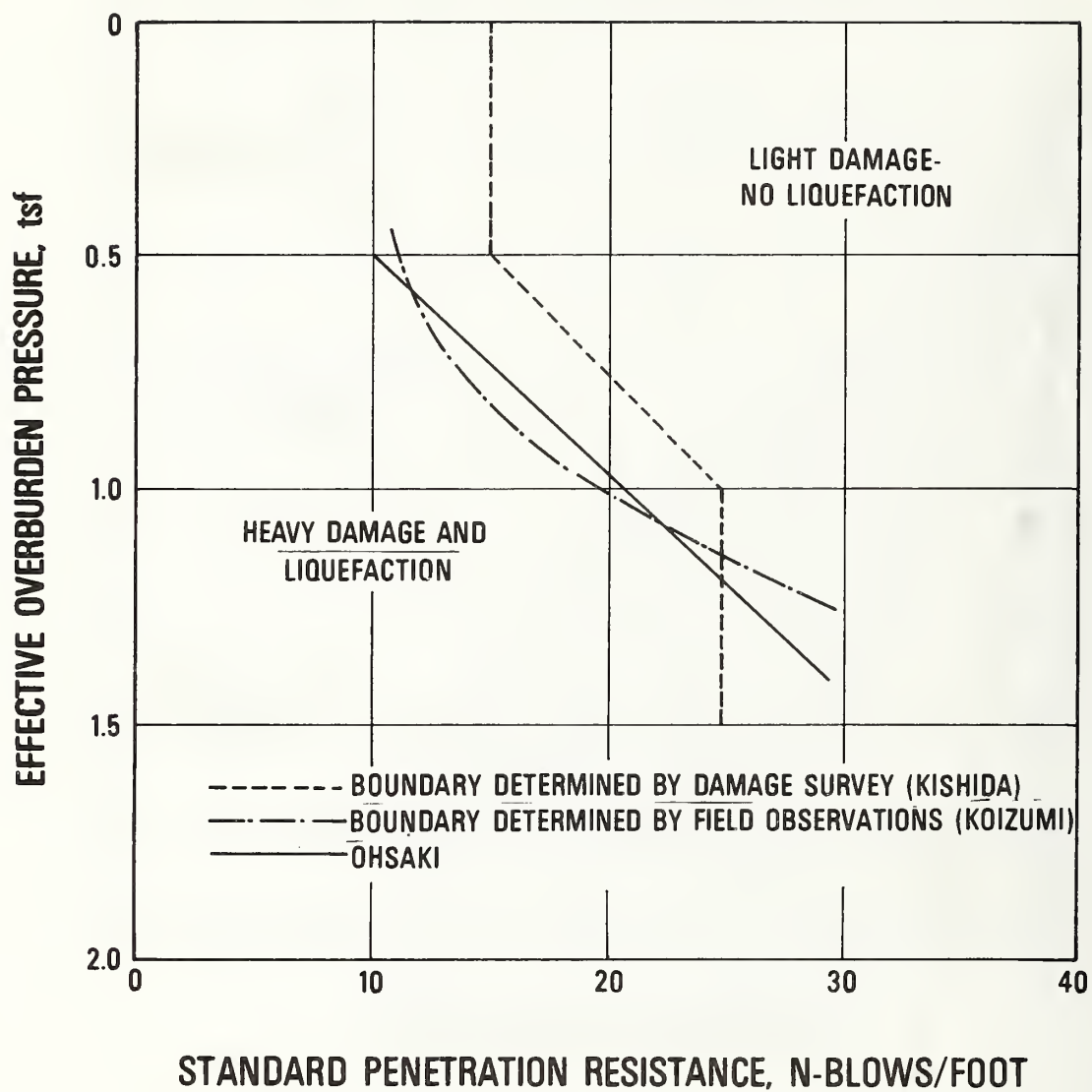


Figure 3.6 Analysis of liquefaction potential at Niigata for earthquake of June 16, 1964 (Seed et al., 1975)

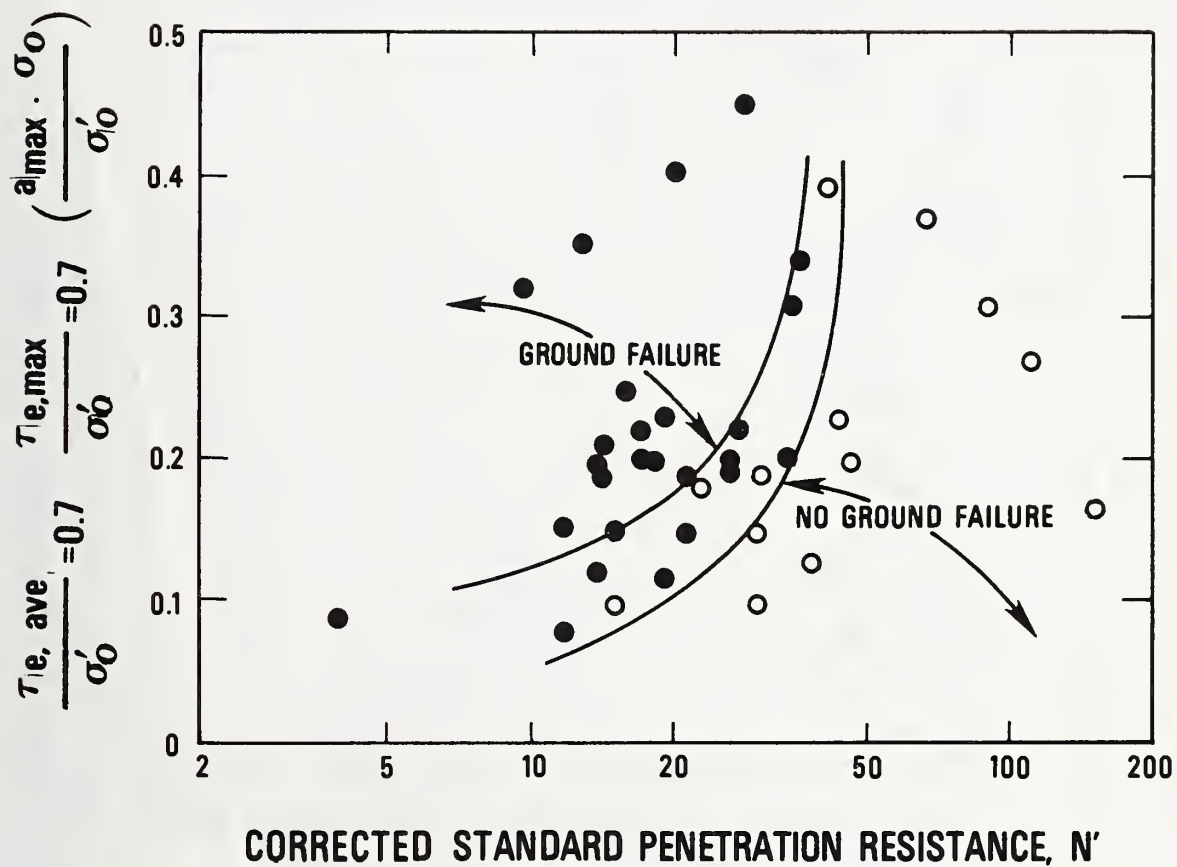


Figure 3.7 Performance of saturated sands at earthquake sites (Castro, 1975)

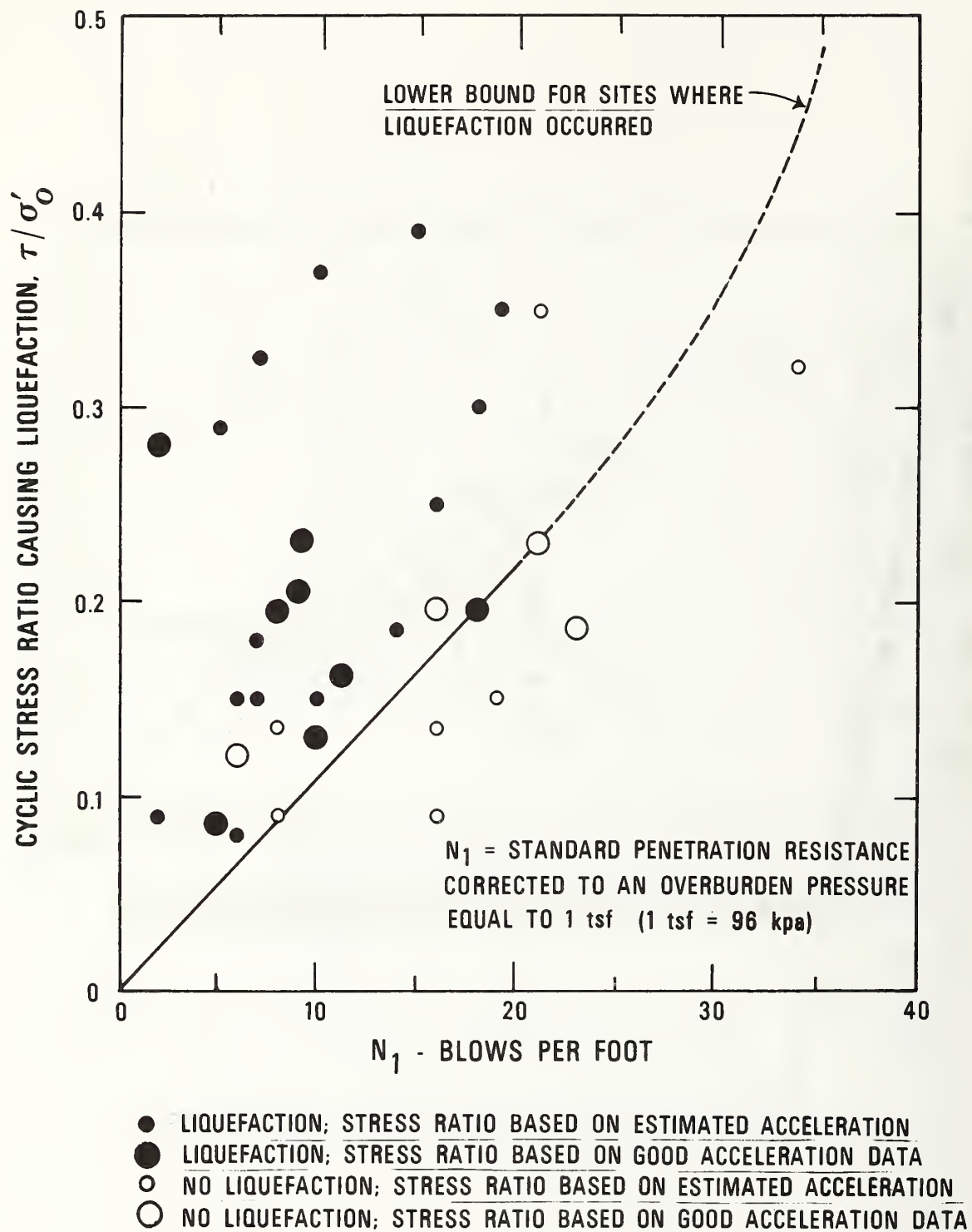


Figure 3.8 Correlation between stress ratio causing liquefaction in the field and modified penetration resistance of sand, N_1 , (Seed et al., 1975)

CYCLIC STRESS RATIO τ/σ'_0 CAUSING PEAK CYCLIC PORE PRESSURE RATIO OF 100% WITH LIMITED SHEAR STRAIN POTENTIAL FOR $\sigma'_0 \approx 1$ tsf

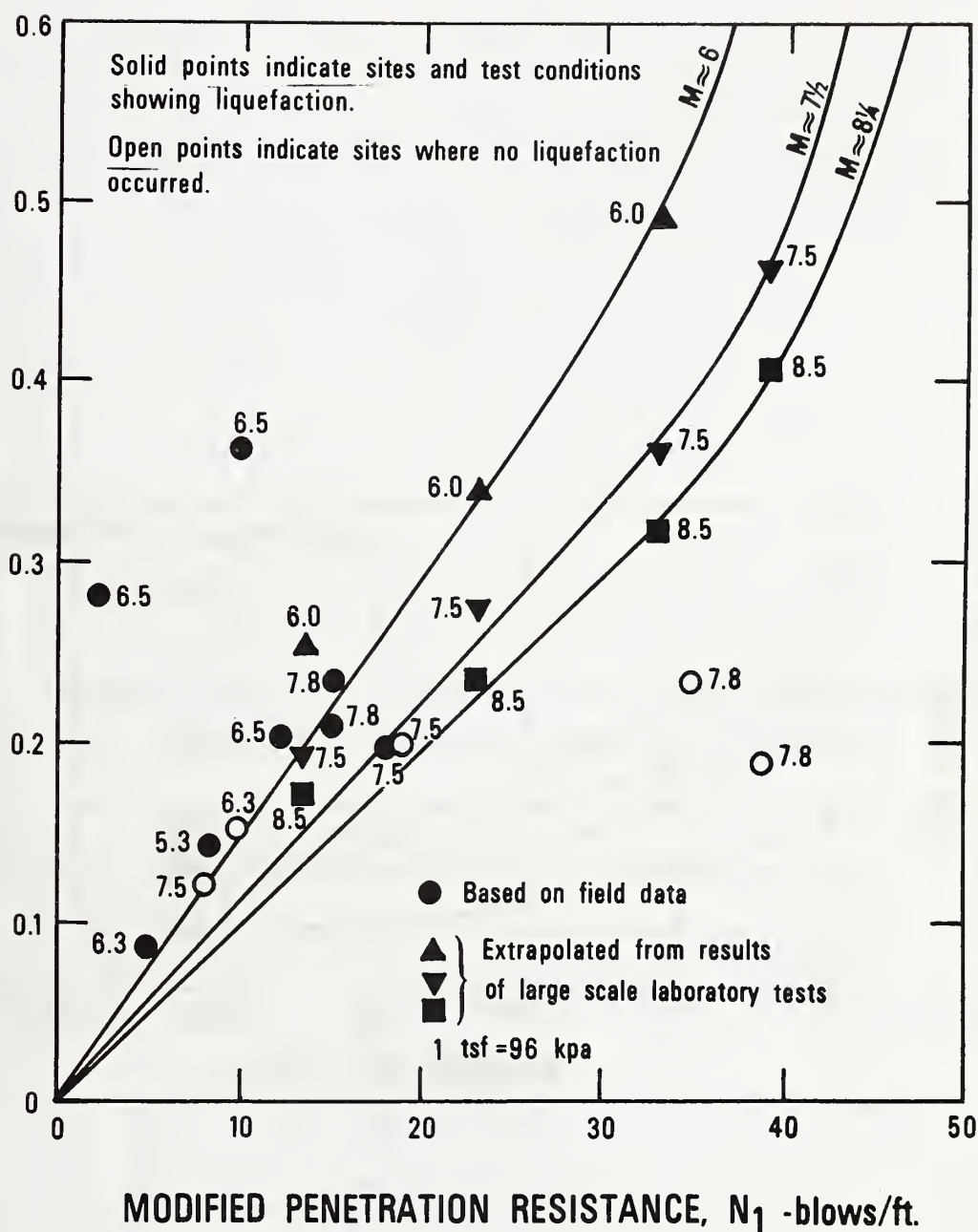


Figure 3.9 Correlation between field liquefaction behavior of sands for level ground conditions and modified penetration resistance (supplemented by data from large scale tests) (Seed, 1979)

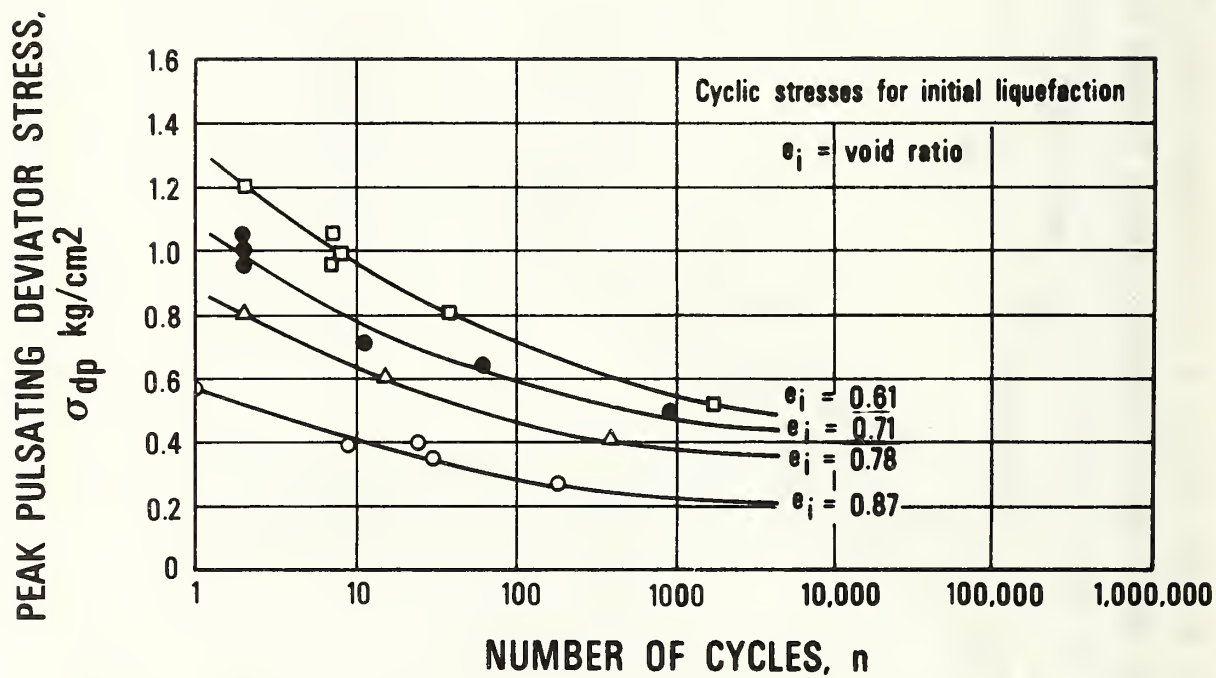
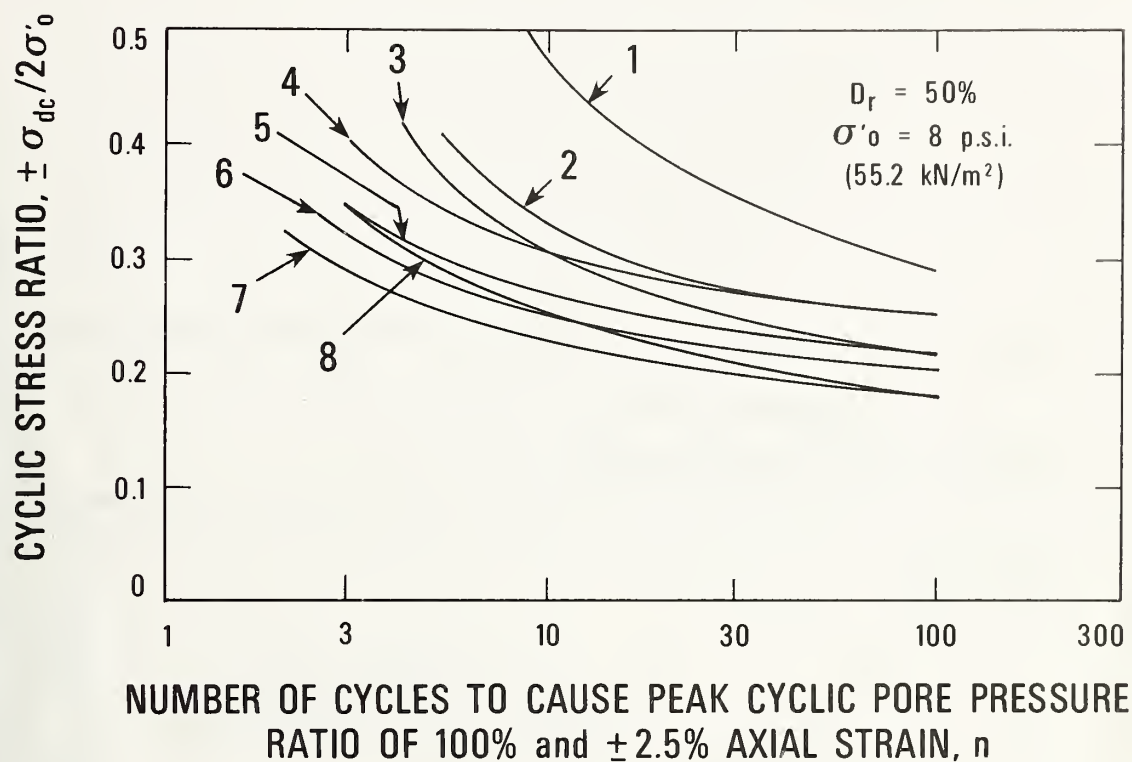


Figure 3.10 Cyclic stresses required to cause liquefaction and 20 percent strain in Sacramento River sand at different densities - $\sigma'_3 = 1.0$ kg per sq cm (Seed and Lee, 1965)



Curve No.	Method of Compaction
1	High frequency vibrations on moist samples
2	Moist tamping
3	Moist rodding
4	Low frequency vibrations on dry samples
5	High frequency vibrations on dry samples
6	Pluviated-water
7	Pluviated-air
8	Dry rodding

Figure 3.11 Cyclic stress ratio versus number of cycles for different compaction procedures (after Mililis et al, 1975)

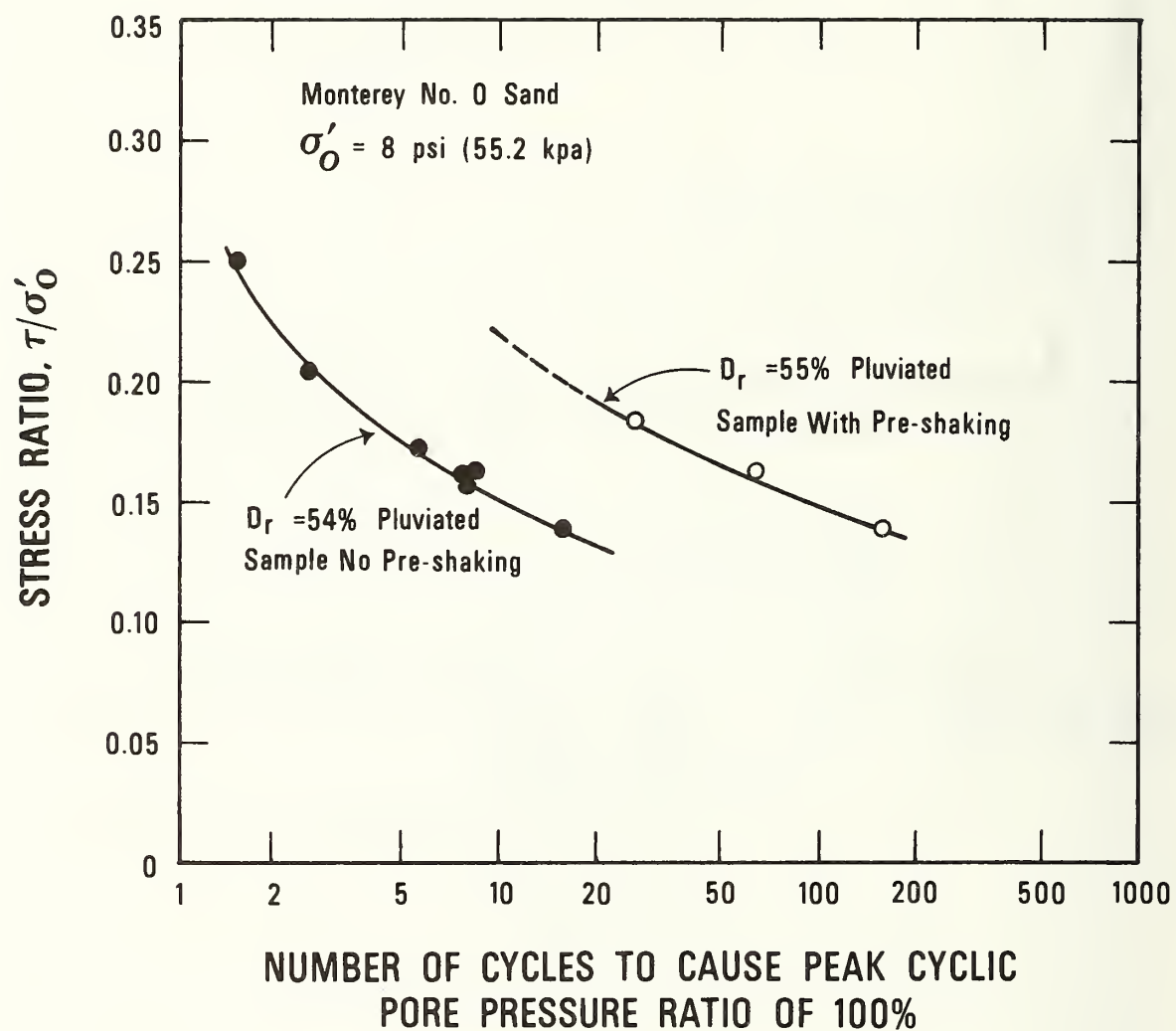


Figure 3.12 Effect of seismic history on cyclic strength of sand (Seed, 1979)

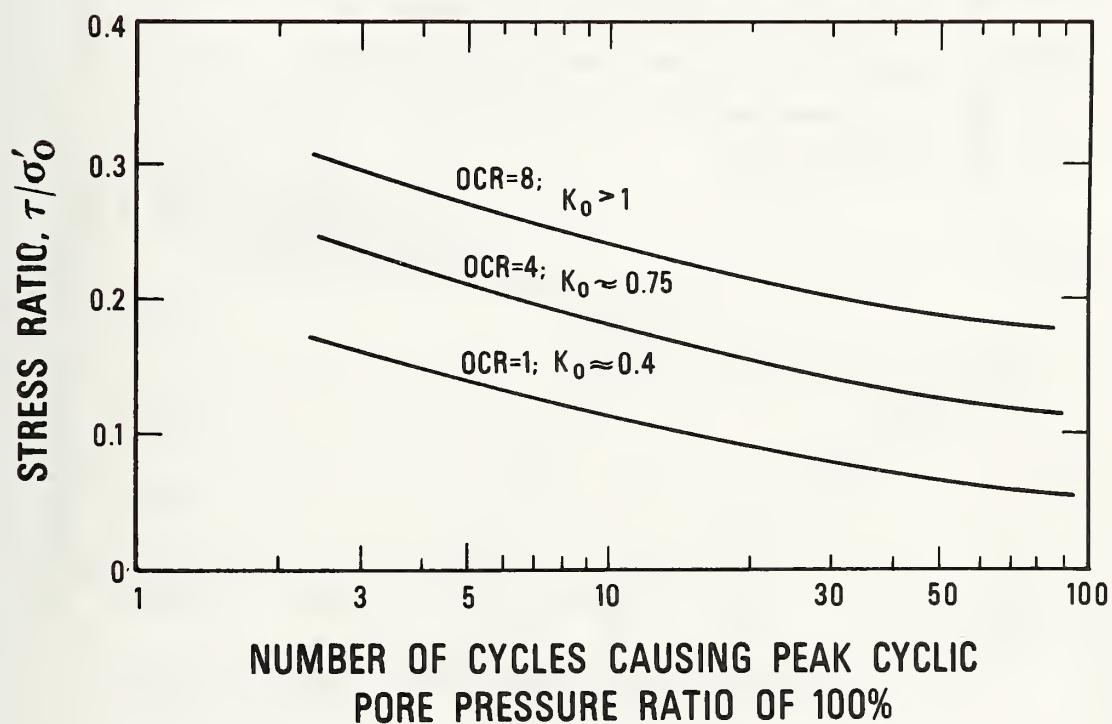


Figure 3.13 Influence of overconsolidation on stress causing pore water pressure ratio of 100 percent in simple shear tests (Seed, 1979)

STRENGTH OF SAND AFTER PERIOD OF SUSTAINED PRESSURE
STRENGTH OF FRESHLY DEPOSITED LABORATORY SAMPLE

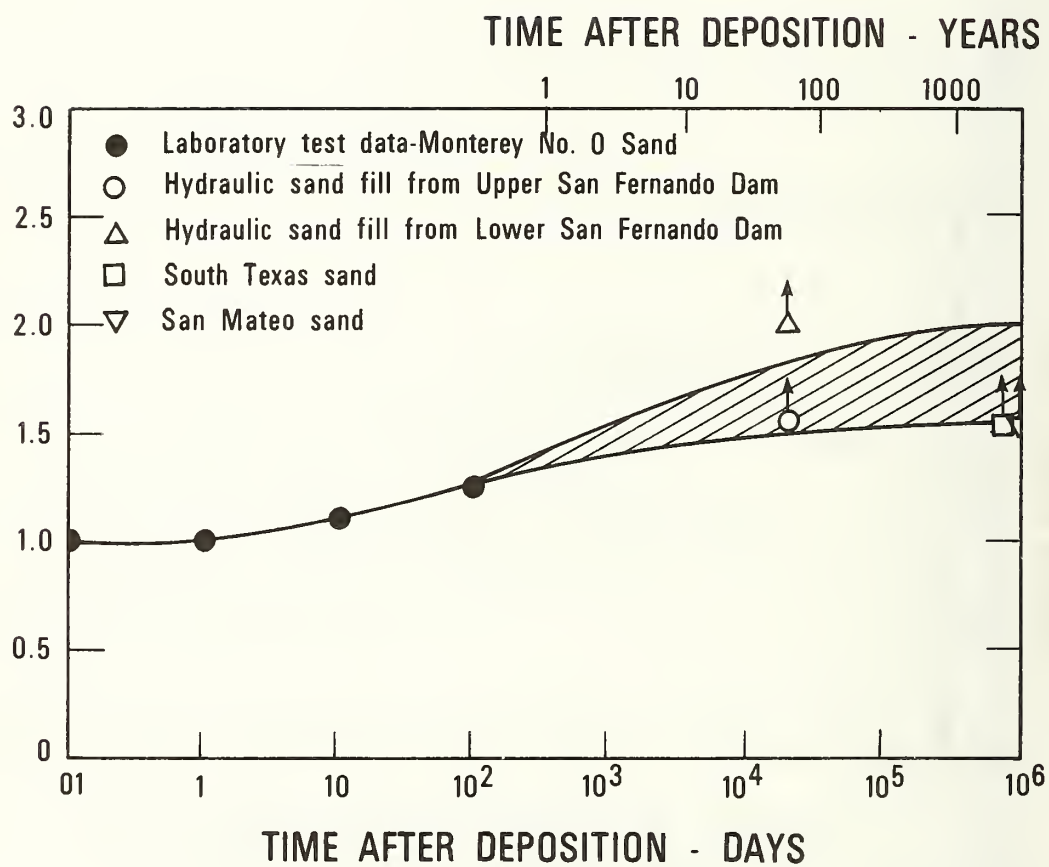


Figure 3.14 Influence of period of sustained pressure on stress causing peak cyclic pore pressure ratio of 100 percent (Seed, 1979)

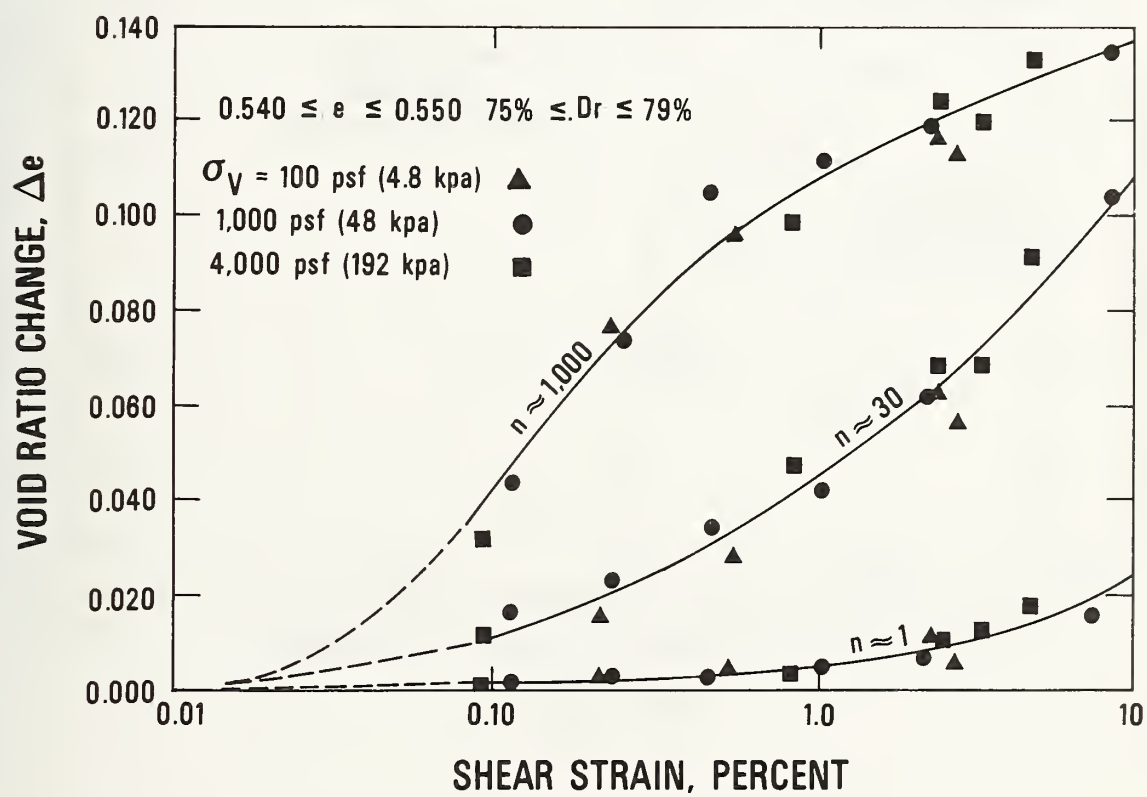


Figure 3.15 Void ratio change for a sand as a function of cyclic shear strain and number of cycles (Youd, 1972)

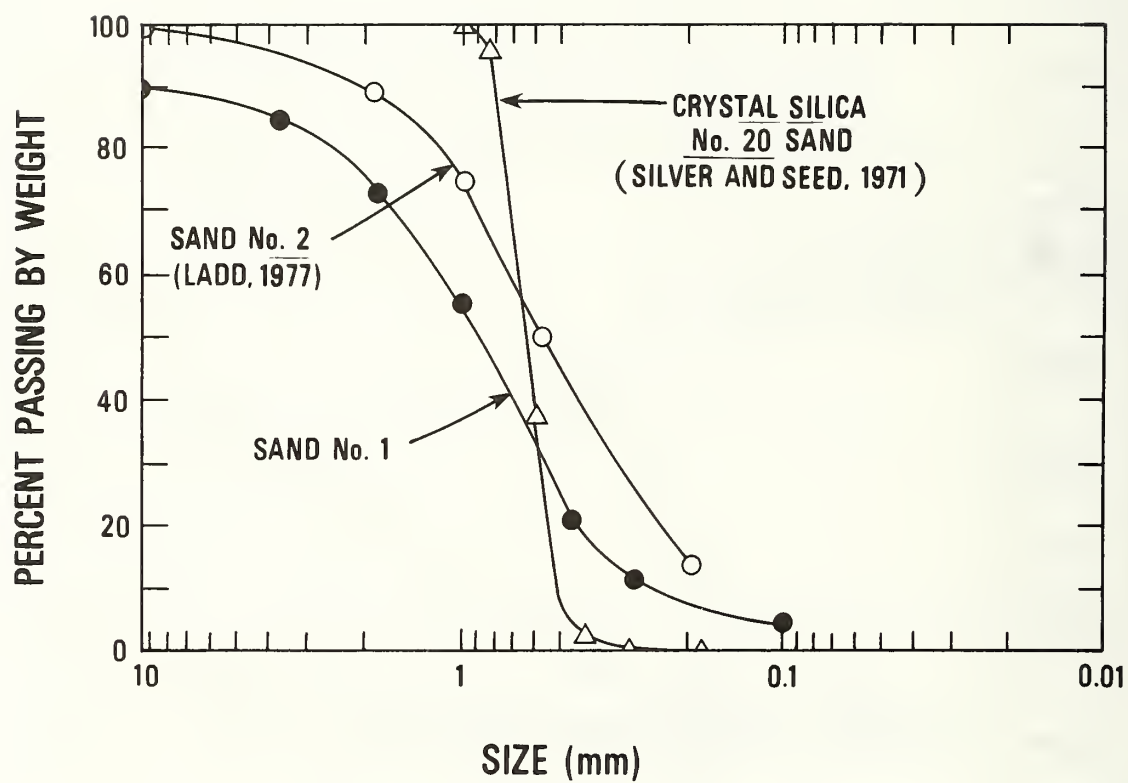


Figure 3.16 Grain size curves of sands used in testing

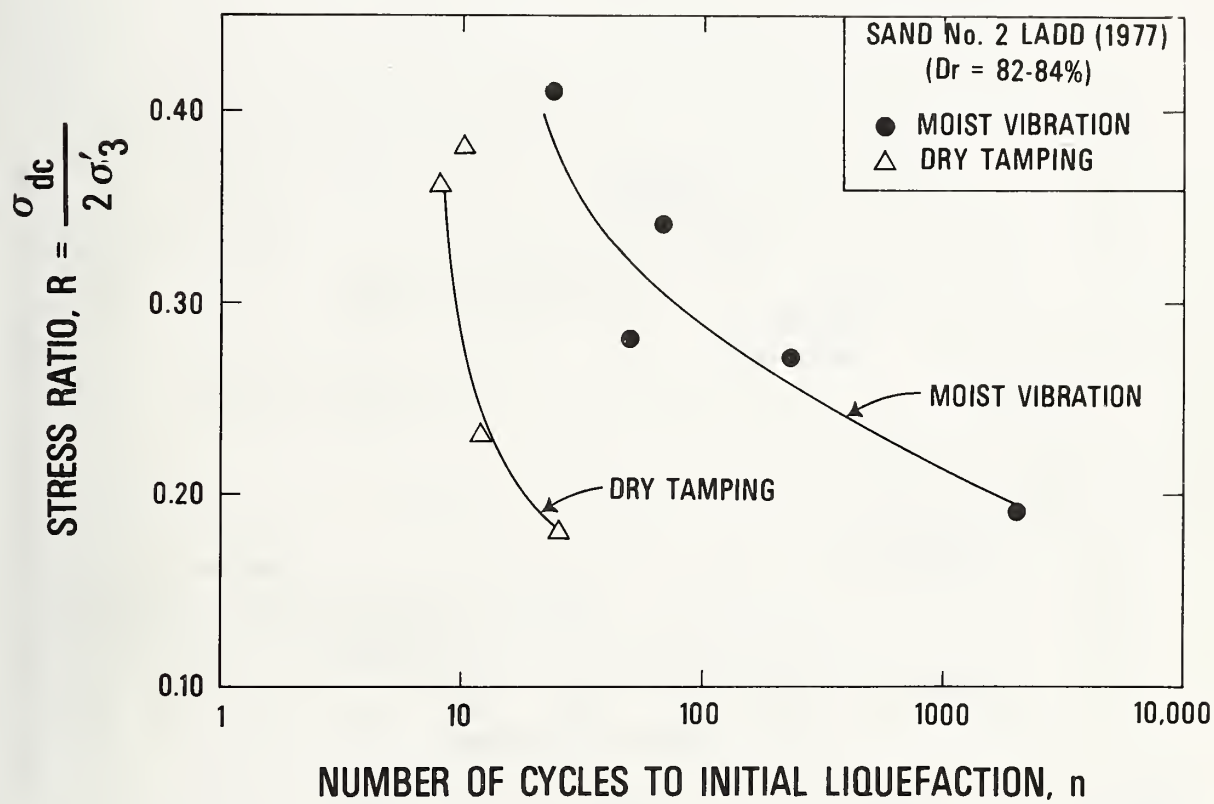


Figure 3.17 Effect of fabric on cyclic strength, stress-controlled tests (Ladd, 1977)

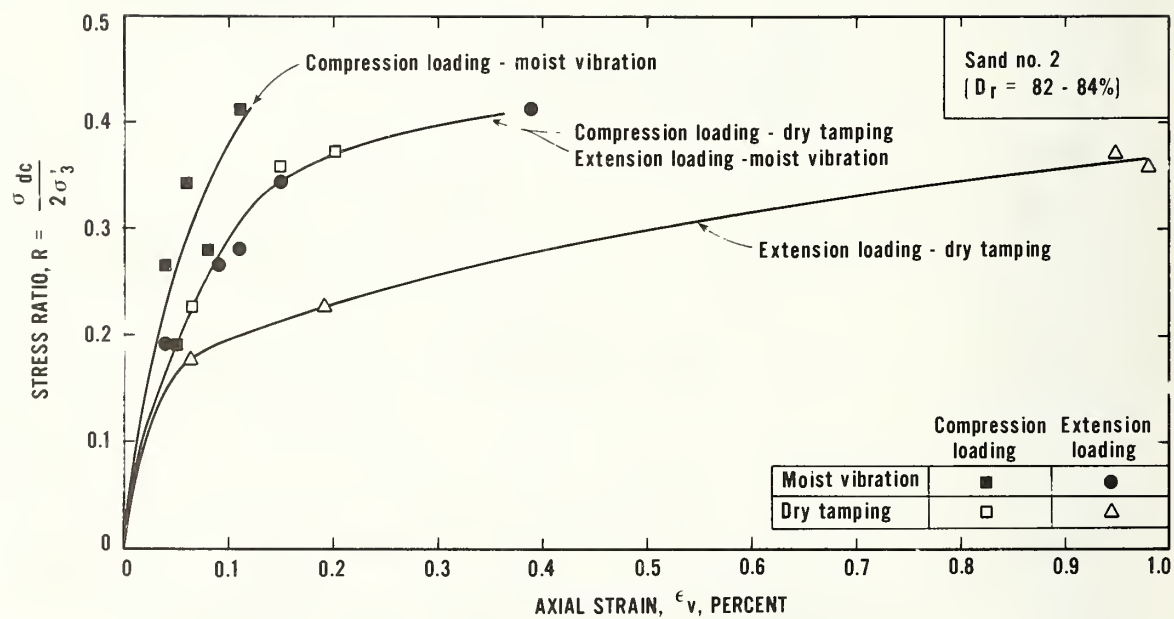


Figure 3.18 Stress-strain curves for first compression and extension excursions, stress-controlled cyclic triaxial tests, Sand No. 2 (modified after Ladd, 1977)

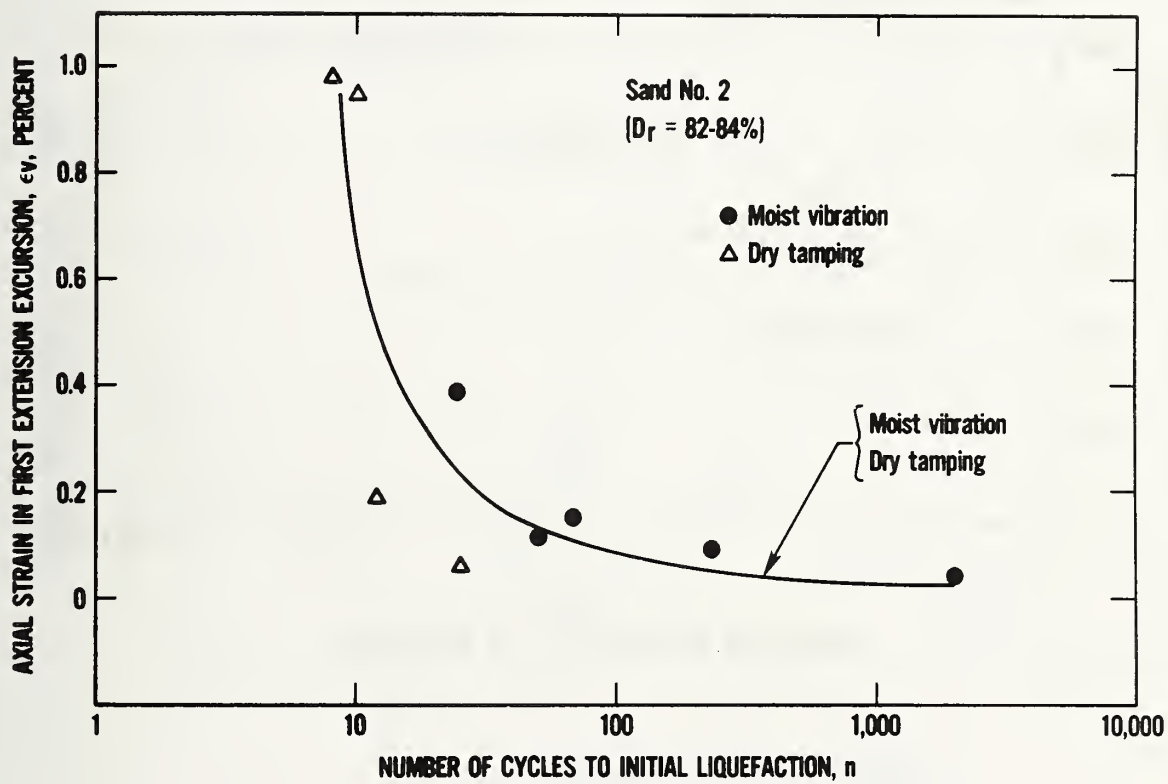


Figure 3.19 Effect of fabric on cyclic strength after accounting for sample stiffness, stress-controlled tests (modified after Ladd, 1977)

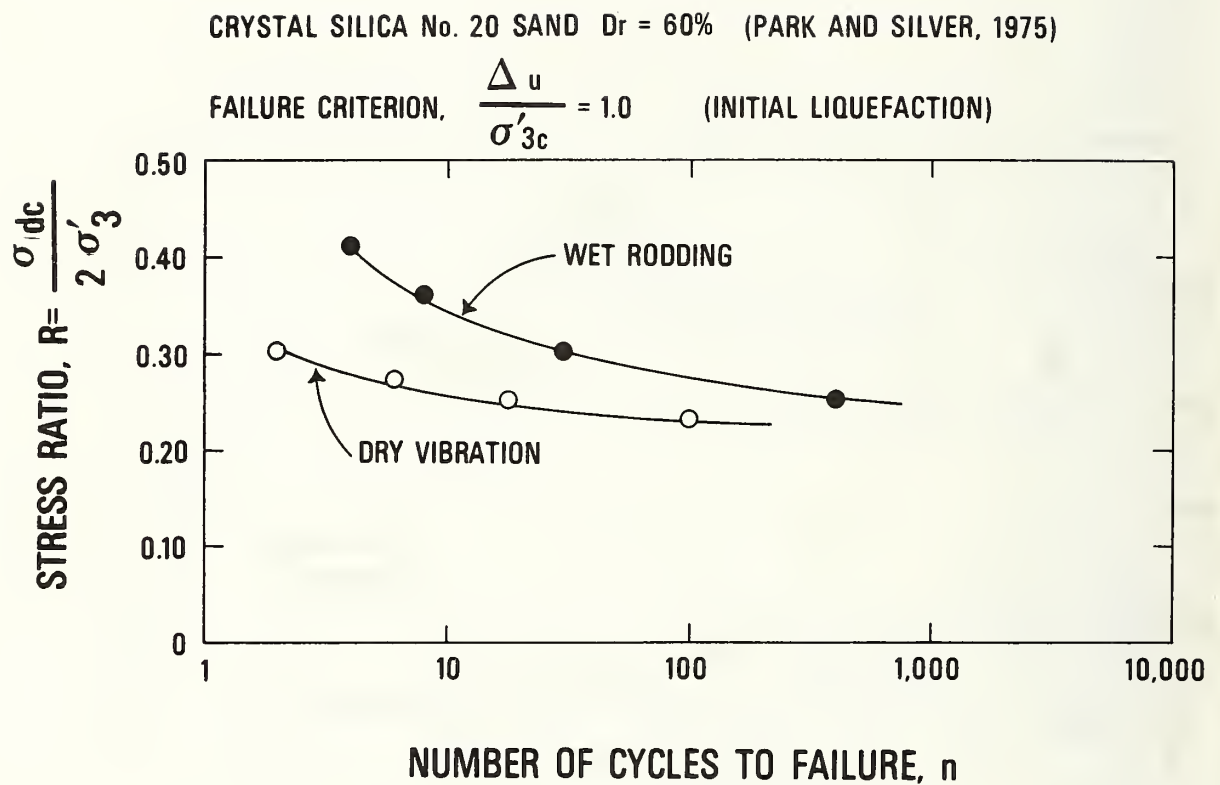


Figure 3.20 Effect of fabric on cyclic strength, stress-controlled tests (Park and Silver, 1975)

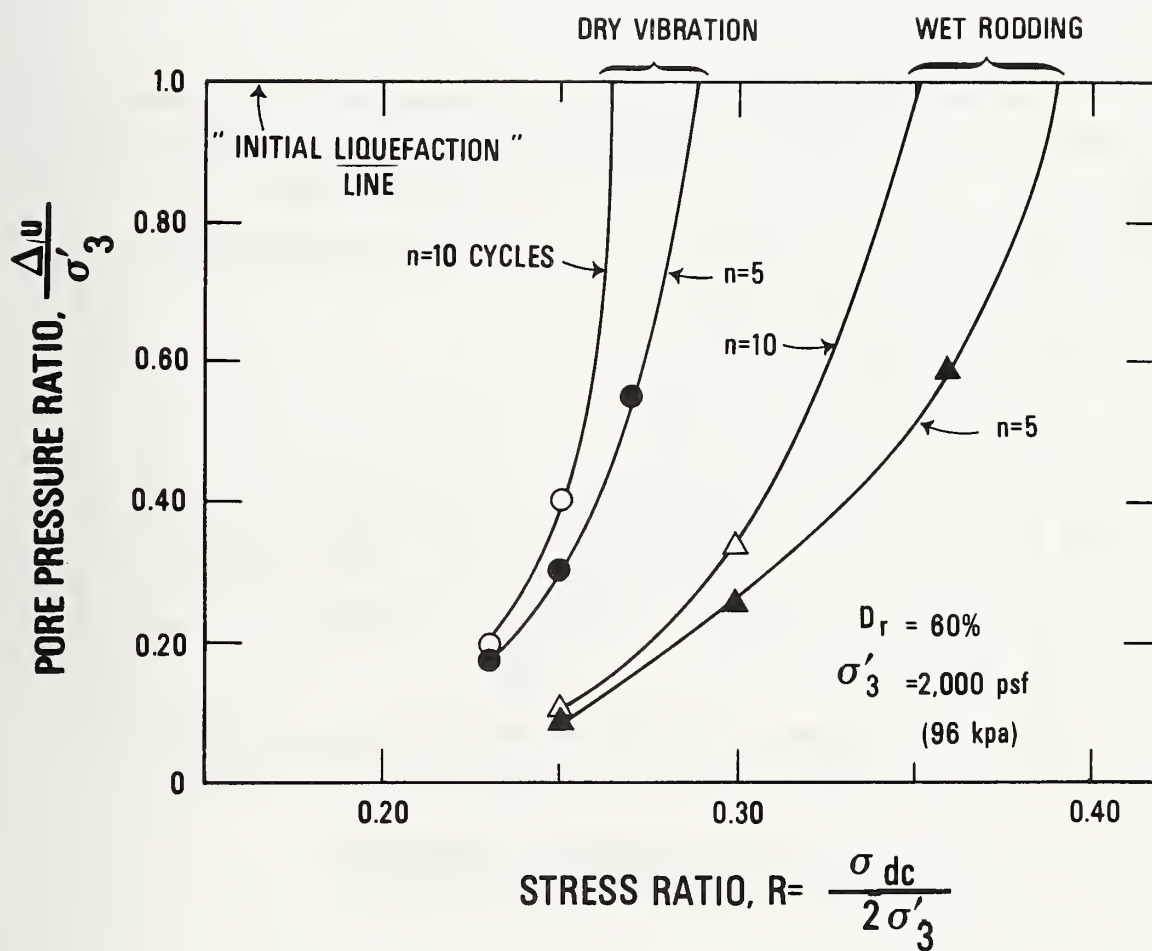


Figure 3.21 Stress-controlled cyclic triaxial tests of saturated Crystal Silica sand (modified after Park and Silver, 1975)

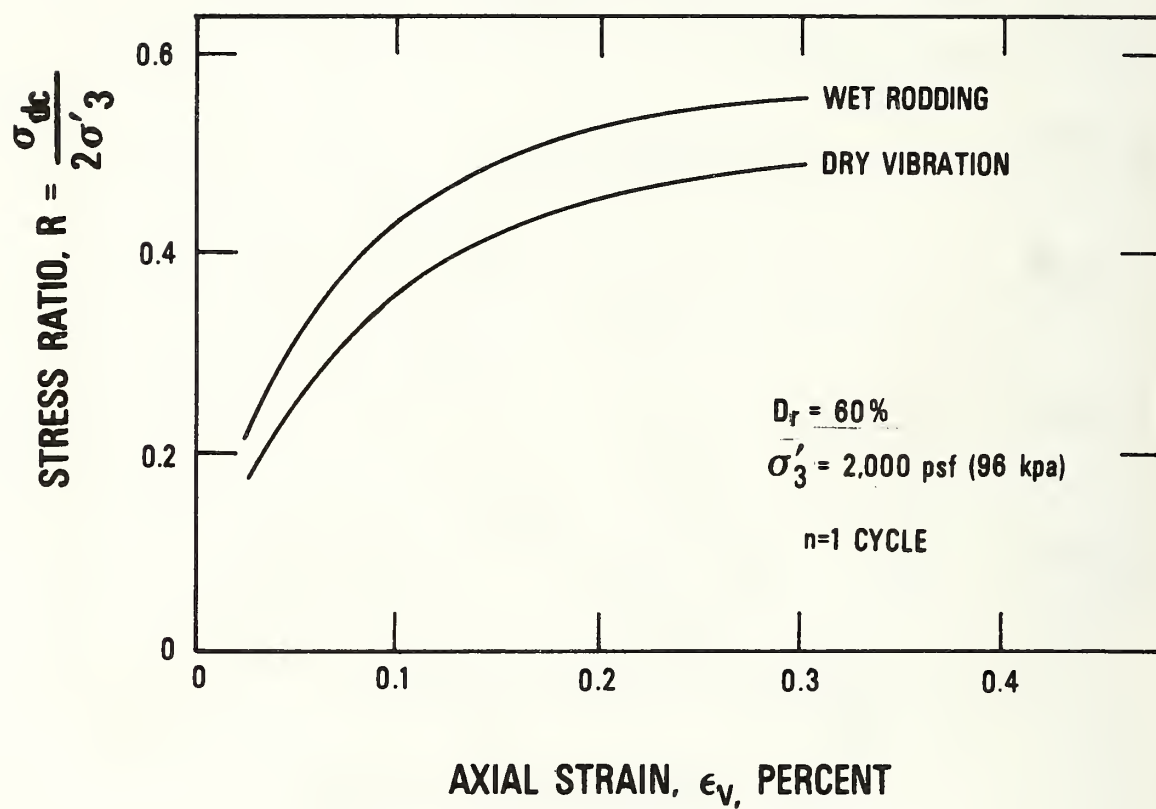


Figure 3.22 Stress-strain curve for first cycle, cyclic triaxial tests of saturated Crystal Silica sand (modified after Park and Silver, 1975)

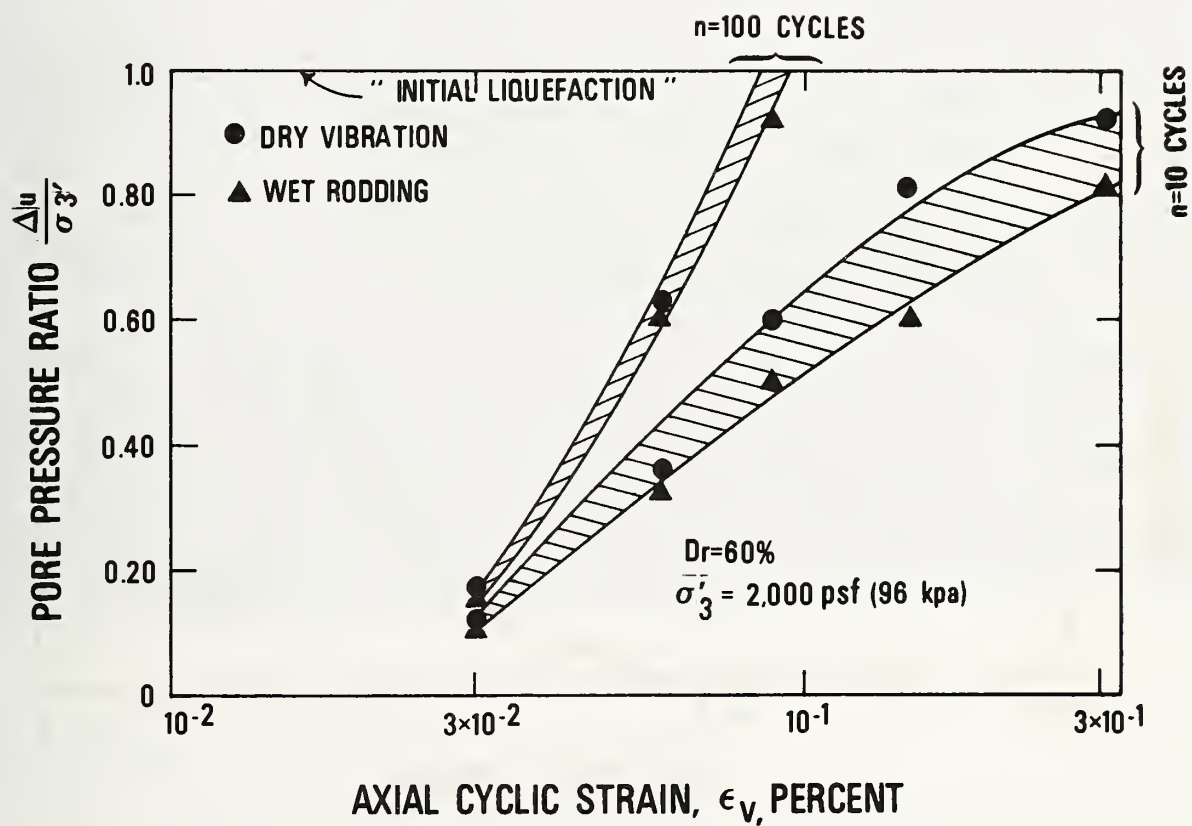


Figure 3.23 Strain-controlled cyclic triaxial tests of saturated Crystal Silica sand (modified after Park and Silver, 1975)

FACING PAGE: Sand boils observed after the Imperial Valley, CA, October 1979 earthquake. Liquified fine sands were pushed up through the ground surface of dry coarse soils by excess pore water pressure.

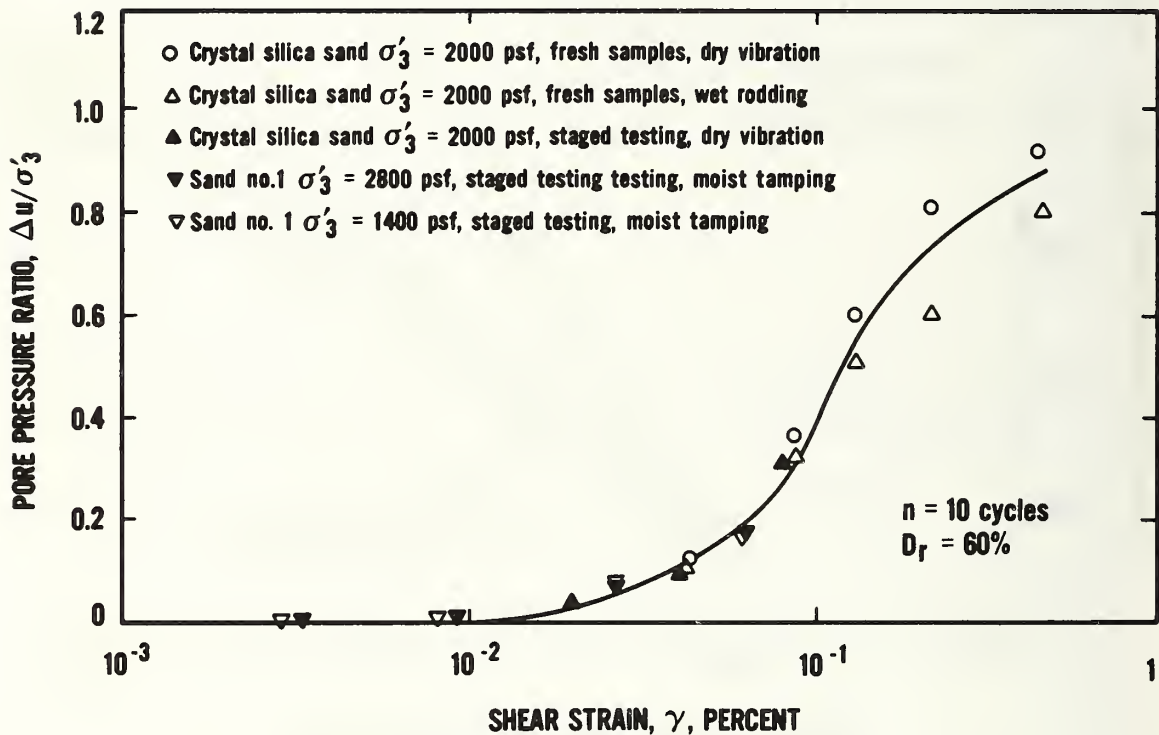


Figure 3.24 Measured pore water pressure in saturated sands after ten loading cycles, strain-controlled cyclic triaxial tests (Dobry and Ladd, 1980)



4. A MODEL OF SPHERES FOR THE THRESHOLD STRAIN

4.1 GENERAL

An important aspect of the relationship between cyclic strain and excess pore water pressure buildup is the existence of a threshold shear strain, γ_t , in sands, below which no densification and, therefore, no excess pore water pressure buildup occurs. Section 3.2.2 summarized experimental evidence suggesting that in sands this parameter seems to have a remarkably constant value, of the order of 10^{-2} percent. The origin of γ_t and the parameters controlling it are investigated in this section by means of a theoretical model of spheres.

The model selected is that of a simple cubic array of identical quartz spheres. Some of the results using this model have been presented elsewhere (Dobry and Swiger, 1979 [21]). Even though the simple cubic array is a very simplified

model of a real sand, it is shown in the rest of this chapter that the study of this model provides: (a) an explanation of the physical origin of γ_t ; (b) a reasonably good prediction of the value $\gamma_t \approx 10^{-2}$ percent which has been measured in actual sands; (c) insight into the influence of parameters such as confining pressure and grain size on γ_t ; and (d) a reasonable prediction of the measured cyclic stress-strain behavior of actual sands at strains below the threshold, $\gamma < \gamma_t$.

Figure 4.1 shows the model. The simple cubic array of elastic quartz spheres is subjected first to an isotropic confining pressure, σ , and then to a cyclic shear stress, $\pm \tau$ (only the stresses corresponding to the positive τ are shown in the figure). Associated with the cyclic stress there is a cyclic strain of the array, $\pm \gamma$. It is assumed that γ is smaller or at most equal to the threshold value, $\gamma \leq \gamma_t$. It will be seen that this is equivalent to assuming that no sliding occurs at any of the contact points between the spheres. The following elastic constants and friction coefficient for the quartz spheres were obtained from Lambe and Whitman (1969 [45]) and are used for the calculations:

Young's Modulus	$E = 11 \times 10^6$ psi
Poisson's Ratio	$\nu = 0.31$
Friction Coefficient	$f = 0.50$

Section 4.2 presents a study of the shear force-displacement relation at the contact points between the spheres, using the results of the Mindlin-Deresiewicz theory. In section 4.3 this information is used to calculate the value of γ_t . In section 4.4 the stress-strain behavior calculated for the model at small strains, $\gamma < \gamma_t$, is compared with that of actual sands.

4.2 CONTACT BETWEEN ELASTIC SPHERES

Figure 4.2 shows the situation at any one of the four contact points around the representative central sphere of figure 4.1. A normal force N and a tangential force T must be transmitted through the contact. The relations between these forces and the overall stresses σ and τ acting on the array shown in figure 4.1 are:

$$\sigma = \frac{N}{4R^2} \quad 4.1$$

$$\tau = \frac{T}{4R^2} \quad 4.2$$

The normal force N produces an elastic shortening of the distance between the centers of the neighboring spheres. This shortening, which translates into normal and volumetric strains for the whole array, is of no interest for the present calculations. On the other hand, the tangential force, T , produces a tangential displacement, δ , between the centers of the spheres. This tangential displacement is the direct cause of the shear strain of the whole array:

$$\gamma = \frac{\delta}{2R} + \frac{\delta}{2R} = \frac{\delta}{R} \quad 4.3$$

where the two terms represent, respectively, the contributions to γ of the two spheres at left and right of, and above and below of, the representative central sphere of figure 4.1.

Therefore, an understanding of the physical origin of δ and a calculating of its value are the key to understanding and calculating γ and γ_t .

The following calculation of δ is based on the work by Mindlin (1949 [51]), Mindlin et al., (1951 [52]) and Mindlin and Deresiewicz (1953 [53]), as summarized in a previous report by Dobry and Grivas (1978 [19]).

The contact point between the spheres in figure 4.2 is really a small circular area of radius $a \ll R$. The value of a is:

$$a = \left(\frac{3}{4} \frac{1-\nu^2}{E} N R \right)^{1/3} \quad 4.4$$

The normal force, N , is distributed over this circular area. The corresponding normal contact stress, σ_c , has the parabolic distribution shown in figure 4.3, where σ_c is a maximum at the center of the contact area and zero at the edge of the area.

The distribution of the tangential force, T , over the same contact area is of special interest. If the tangential force has been monotonically increased while keeping N constant, the elastic solution for the shear stresses, τ_c , within the contact area gives $\tau_c = \infty$ at the edge of the contact area.

If the solid friction condition, $\tau_c \leq f\sigma_c$, is imposed at all points within the contact area, it is found that there is an annulus of inside radius c and outside radius a (see fig. 4.3), where $\tau_c = f\sigma_c$ and where slip occurs between the two surfaces and energy is lost by friction. As T increases, c decreases, until, for $T = f N$, $c = 0$, the condition $\tau_c = f\sigma_c$ prevails over the entire contact area, and there is gross sliding of the two spheres along their contact. If δ = horizontal displacement between the centers of the spheres, the force-displacement curve, T vs. δ , is of the yielding type, as shown by curve OP in figure 4.4.

If the tangential load T is cycled between two fixed values, T^* and $-T^*$, ($T^* < f N$), while maintaining N constant, a hysteresis loop is formed, as shown in figure 4.4. This hysteresis loop is similar to the experimental loops measured in sands subjected to cyclic shear loading (e.g., see Seed and Idriss, 1970 [77]). The area enclosed by the loop measures the energy spent by friction in the annulus of slip, and for the case considered here ($T^* < f N$), the loop is stable (i.e., it repeats itself cycle after cycle).

Mindlin et al., (1951 [52]), Johnson (1955 [34] and 1961 [35]) and Goodman and Brown (1962 [27]) verified experimentally the predictions of the Mindlin-

Deresiewicz theory, by pressing together glass and metallic bodies and then applying cyclic tangential forces at the contact between them. All predictions were verified, including the existence of the annulus of slip, as well as the location of the tangential force-displacement curves for monotonic (curve OP in fig. 4.4) and cyclic (hysteretic loops in figs. 4.4 and 4.5) loadings.

4.3 THRESHOLD STRAIN OF ARRAY OF QUARTZ SPHERES

The equation of the monotonic "backbone" curve (OP in fig. 4.4) predicted by the Mindlin-Deresiewicz theory is:

$$\frac{\delta}{\delta_1} = 1 - \left(1 - \frac{T}{fN}\right)^{2/3} \quad 4.5$$

where

$$\delta_1 = \frac{3(2-\nu)(1+\nu)fN}{4Ea} \quad 4.6$$

Equation 4.5 has been plotted in figure 4.6. When the tangential displacement $\delta = \delta_1$, the tangential force $T = fN$ and gross sliding of the contact occurs. Therefore, δ_1 is the threshold displacement at which there is a tendency for an overall change of the geometric arrangement of the spheres to occur. The threshold strain, γ_t , is related to δ_1 by equation 4.3:

$$\gamma_t = \frac{\delta_1}{R} \quad 4.7$$

If the value of δ_1 from equation 4.6 is substituted into equation 4.7, and the resultant expression is combined with equations 4.1 and 4.4, the following equation is obtained for γ_t :

$$\gamma_t = 2.08 \frac{(2-\nu)(1+\nu)f}{(1-\nu^2)^{1/2}(E)^{2/3}} (\sigma)^{2/3} \quad 4.8$$

Finally, if the numerical values of the constants for quartz listed in section 4.1 are used, the following simple expression is derived,

$$\gamma_t(\%) = 1.75 \times 10^{-4} (\sigma)^{2/3}, \quad \sigma \text{ in psf} \quad 4.9$$

Equation 4.9 gives the threshold strain, γ_t , as a function of the confining pressure, σ for a simple cubic array of quartz spheres. This equation is plotted in figure 4.7. The result is extremely interesting. It suggests that: (a) for the range of confining pressures of most practical interest (500 psf $< \sigma < 4,000$ psf), γ_t is in the range between about 1×10^{-2} percent and 4×10^{-2} percent, which is close to the experimental values reported for actual sands; and (b) γ_t is independent of grain size (the radius of the spheres, R is not present in equations 4.8 and 4.9. Finally, equation 4.8 offers a means to study the influence of the material constants E , ν , and f for sands other than quartz sands.

4.4 CYCLIC STRESS-STRAIN BEHAVIOR AT VERY SMALL STRAINS

The simple cubic model of quartz spheres can also be used to predict the cyclic stress-strain behavior of sands at very small strains, $\gamma < \gamma_t$. Measurements during cyclic shear loading of sands have produced experimental hysteresis loops such as those shown in figure 4.4, except that, for actual sands, stress (τ) is plotted versus strain (γ), instead of T versus δ used in the figure. However, the curves in figures 4.4 and 4.6 can be readily converted into $\tau - \gamma$ plots valid for the simple cubic array and loading system of figure 4.1. Specifically, equation 4.5, representing the backbone curve in figures 4.4 and 4.6, becomes:

$$\frac{\gamma}{\gamma_t} = 1 - \left(1 - \frac{\tau}{f\sigma}\right)^{2/3} \quad 4.10$$

It is of interest to compute two normalized parameters for the simple cubic array of quartz spheres at very small strains, $\gamma < \gamma_t$, and to compare these parameters with the values measured in actual sands. These parameters are: (a) the modulus reduction curve, G/G_{\max} versus γ , and b) the damping ratio, λ versus the shear strain γ .

The expression of G/G_{\max} versus γ can be obtained directly from equation 4.10 as follows:

$$\tau = f\sigma \left[1 - \left(1 - \frac{\gamma}{\gamma_t}\right)^{3/2}\right] \quad 4.11$$

$$G = G_{\sec} = \frac{\tau}{\gamma} = \frac{f\sigma}{\gamma} \left[1 - \left(1 - \frac{\gamma}{\gamma_t}\right)^{3/2}\right] \quad 4.12$$

$$G_{\max} = \left(\frac{d\tau}{d\gamma}\right)_{\gamma=0} = \frac{3}{2} \frac{f\sigma}{\gamma_t}$$

$$\frac{G}{G_{\max}} = \frac{2}{3} \frac{1 - \left(1 - \frac{\gamma}{\gamma_t}\right)^{3/2}}{\gamma/\gamma_t} \quad 4.13$$

Equation 4.13 has been plotted as a dashed curve in figure 4.8 for a representative value $\gamma_t = 1.5 \times 10^{-2}$ percent. The experimental range for sands presented by Seed and Idriss (1970 [77]) is superimposed in the figure for comparison. The theoretical line generally coincides with the upper bound of the experimental range.

A similar calculation was performed for the hysteretic damping ratio, λ . The usual definition of λ is:

$$\lambda = \frac{1}{2\pi} \frac{\Delta W}{\tau\gamma} \quad 4.14$$

where ΔW = area enclosed by a $\tau - \gamma$ hysteresis loop. For the simple cubic array λ can be calculated using equation 4.14, or alternatively directly from the theoretical $T - \delta$ hysteretic loop shown in figure 4.4. If this last procedure is used, the damping ratio is:

$$\lambda = \frac{1}{2\pi} \frac{(\Delta W)_{\text{contact}}}{T^* \delta^*} \quad 4.15$$

where $(\Delta W)_{\text{contact}}$ is the area of the loop in figure 4.4 (energy dissipated at one contact during one loading cycle), and T^* and δ^* are the maximum values of the tangential load and displacement, respectively, during the cycle. Equations 4.14 or 4.15 give identical results and equation 4.15 is used here for convenience.

Goodman and Brown (1962 [27]) calculated the value of $(\Delta W)_{\text{contact}}$:

$$\begin{aligned} (\Delta W)_{\text{contact}} = \frac{18}{5} \frac{(2-\nu)(1+\nu)(fN)^2}{Ea} \left\{ 1 - \left(1 - \frac{T^*}{fN} \right)^{5/3} \right. \\ \left. - \frac{5}{6} \frac{T^*}{fN} \left[1 + \left(1 - \frac{T^*}{fN} \right)^{2/3} \right] \right\} \end{aligned} \quad 4.16$$

By combining equations 4.5, 4.3 and 4.7, equation 4.17 is obtained:

$$\frac{T^*}{fN} = 1 - \left(1 - \frac{\delta^*}{\delta_1} \right)^{3/2} = 1 - \left(1 - \frac{\gamma}{\gamma_t} \right)^{3/2} \quad 4.17$$

where γ = maximum shear strain during the loading cycle.

By substituting equation 4.17 into equation 4.16, the following expression is obtained for $(\Delta W)_{\text{contact}}$:

$$\begin{aligned} (\Delta W)_{\text{contact}} = \frac{18}{5} \frac{(2-\nu)(1+\nu)(fN)^2}{Ea} \left\{ 1 - \left(1 - \gamma/\gamma_t \right)^{5/2} \right. \\ \left. - \frac{5}{6} \left(2 - \frac{\gamma}{\gamma_t} \right) \left[1 - \left(1 - \gamma/\gamma_t \right)^{3/2} \right] \right\} \end{aligned} \quad 4.18$$

Equation 4.18 provides the value of $(\Delta W)_{\text{contact}}$ needed to calculate λ in equation 4.15. The product $T^* \delta^*$ for equation 4.15 is obtained as follows:

From equation 4.17:

$$T^* = fN \left[1 - \left(1 - \frac{\gamma}{\gamma_t} \right)^{3/2} \right] \quad 4.19$$

From equations 4.6 and 4.17:

$$\delta^* = \delta_1 \frac{\gamma}{\gamma_t} = \frac{3(2-\nu)(1+\nu)fN}{4Ea} \frac{\gamma}{\gamma_t} \quad 4.20$$

Finally, if equations 4.18, 4.19 and 4.20 are combined with equation 4.15, the following expression is obtained for λ :

$$\lambda = \frac{12}{5\pi} \left\{ 1 - \frac{(1 - \gamma/\gamma_t)^{5/2}}{(\gamma/\gamma_t)[1-(1-\gamma/\gamma_t)^{3/2}]} - \frac{5}{6} \frac{(2 - \gamma/\gamma_t)}{\gamma/\gamma_t} \right\} \quad 4.21$$

Equation 4.21 has been plotted as a dashed curve in figure 4.9 for a value $\gamma_t = 1.5 \times 10^{-2}$ percent. The experimental range for sands given by Seed and Idriss (1970 [77]) is again included for comparison. The theoretical equation for the simple cubic array coincides approximately with the lower bound of the experimental results for most of the range of strains, $\gamma < \gamma_t = 1.5 \times 10^{-2}$ percent. The comparisons presented in figures 4.8 and 4.9 further verify the crude simple cubic model used to compute γ_t . These figures show that the model predicts in a general manner the main features of the cyclic stress-strain behavior of sands at very small strains, $\gamma < \gamma_t$.

Another interesting feature of equations 4.13 and 4.21 is that both G/G_{\max} and γ are unique functions of the normalized strain parameter, γ/γ_t . This is similar to the hyperbolic stress-strain model for cyclic loading of soils proposed by Hardin and Drnevich (1972) [29], where G/G_{\max} is a function of γ/γ_r , and γ_r = reference strain. In the simple cubic array, the threshold, γ_t , plays the role of a reference strain, and in actual sands, perhaps γ_t and γ_r are also related. In that respect, it is interesting to note that measurements in sands and other soils show that, if the confining pressure, σ , is increased, both γ_r and $(G/G_{\max})_\gamma$ at a given γ also increase (see also Richart, 1980 [66]). This is similar to the prediction of the cubic array model: equations 4.8 and 4.9 and figure 4.7 illustrate the increase in γ_t with σ , while equation 4.13 predicts an increase in G/G_{\max} as γ_t (and therefore as σ) increases. For example, for $\gamma = 10^{-2}$ percent and $\sigma = 500$ psf, equations 4.9 and 4.13 predict $(G/G_{\max})_\gamma = 10^{-2}$ percent = 0.71 for a cubic array of quartz spheres. If $\sigma = 4,000$ psf, the same trend and very similar values of $(G/G_{\max})_\gamma = 10^{-2}$ percent have been measured in several sands by Iwasaki et al., (1978 [33]).

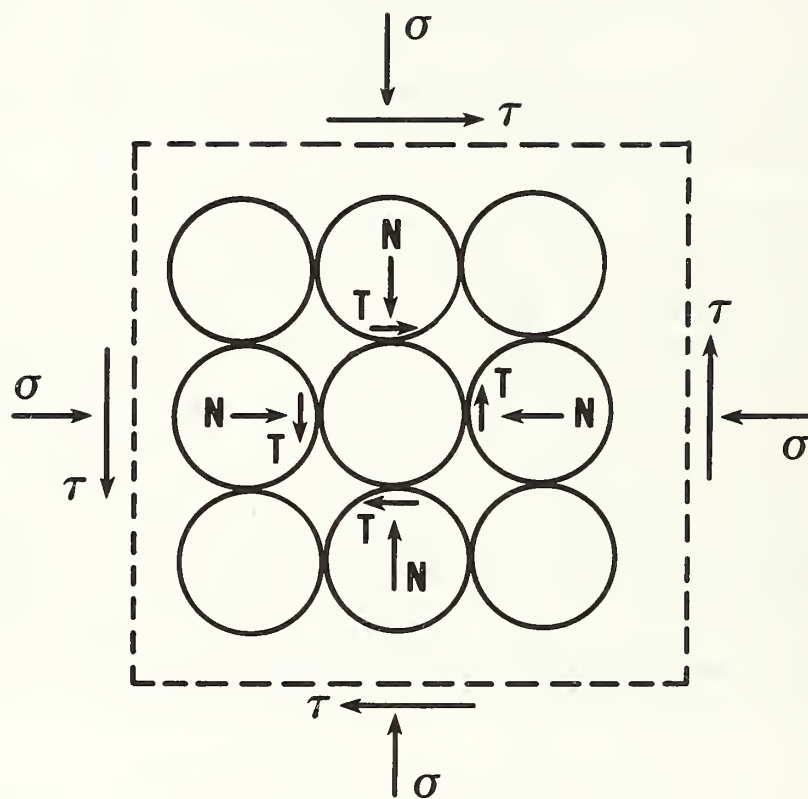


Figure 4.1 Simple cubic array of equal spheres

Confining (normal) stress

$$\sigma = N/(4R^2)$$

Shear stress

$$\tau = T/(4R^2)$$

Shear strain

$$\gamma = \delta / R$$

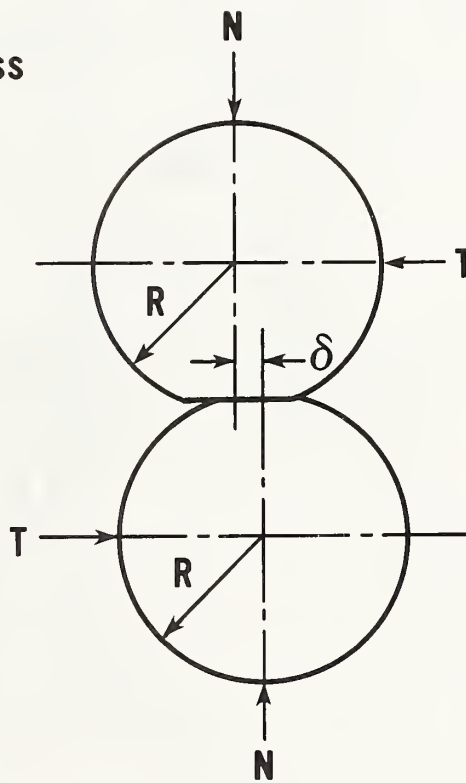
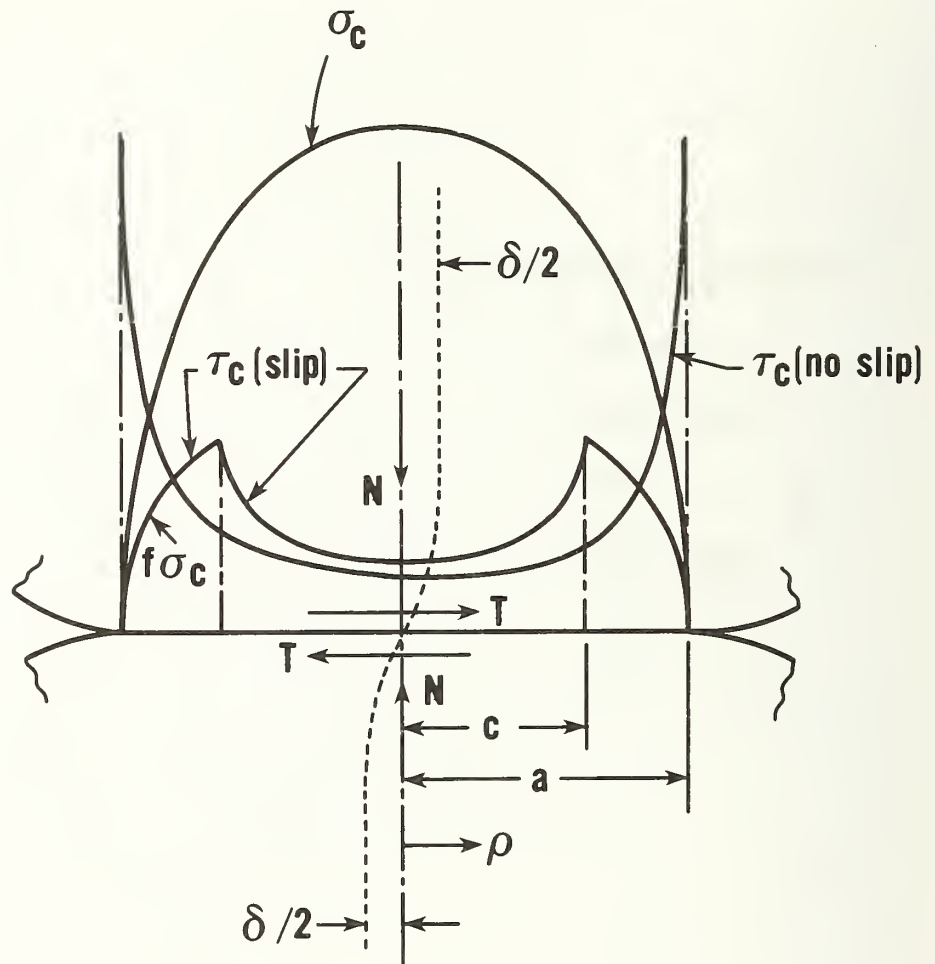


Figure 4.2 Elastic spheres under normal and tangential loads



$$\sigma_c = \frac{3N}{2\pi a^3} (a^2 - \rho)^{1/2}$$

Figure 4.3 Normal (σ_c) and tangential (τ_c) components of traction on contact region between two spheres subjected to a normal force followed by a monotonic tangential force (Deresiewicz, 1973)

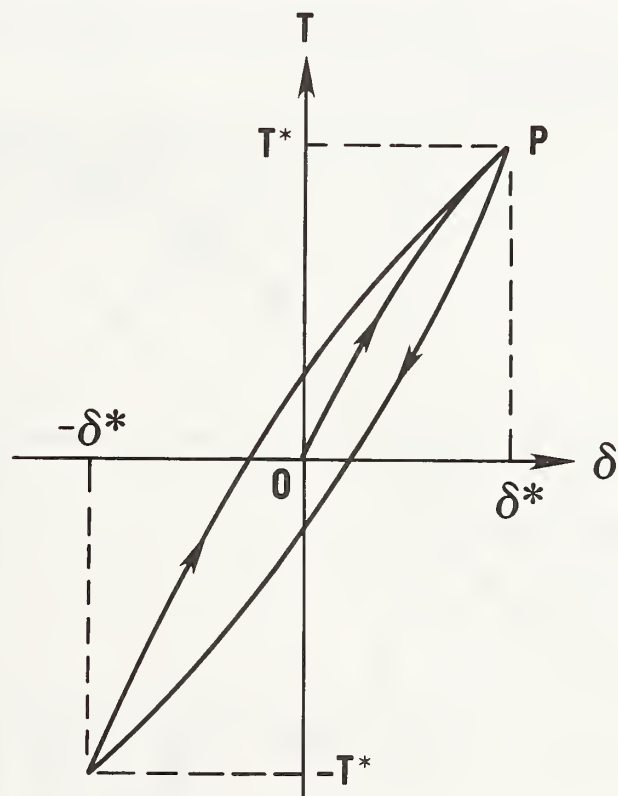


Figure 4.4 Theoretical hysteresis loop due to oscillating tangential force at constant normal force for two spheres in contact (Deresiewicz, 1973)

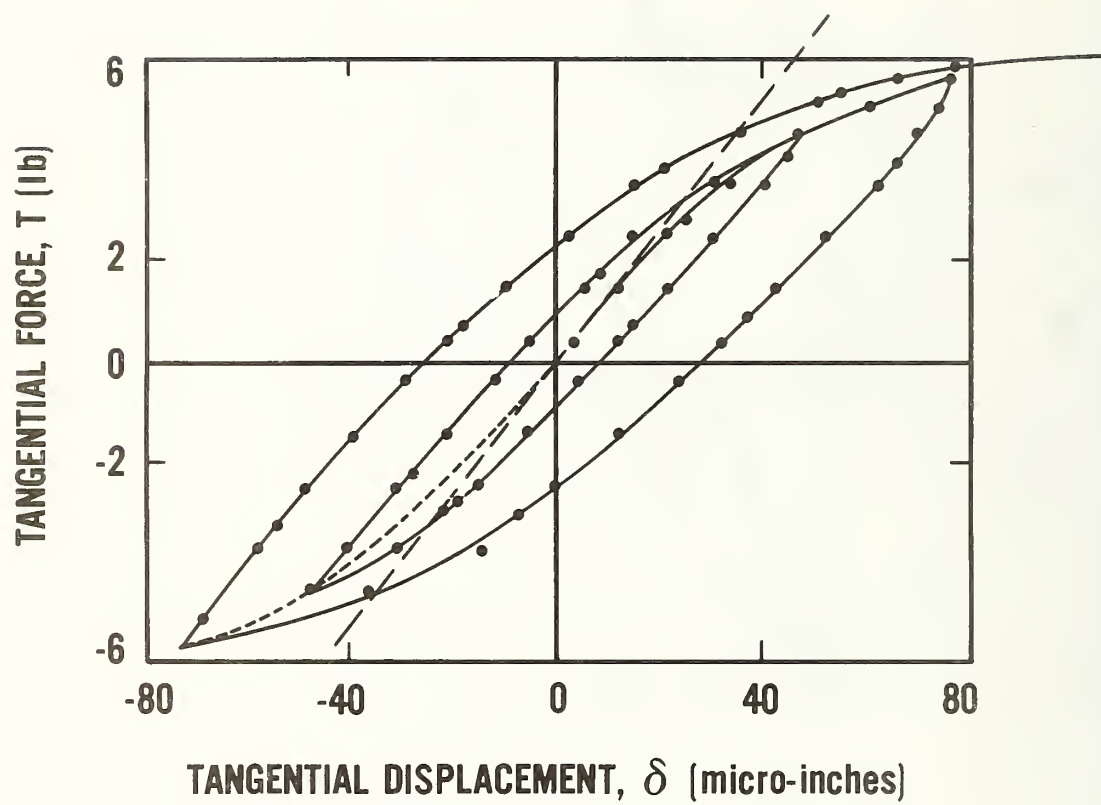


Figure 4.5 Experimental hysteresis loops obtained from cyclic tests of bodies in contact (Johnson, 1955)

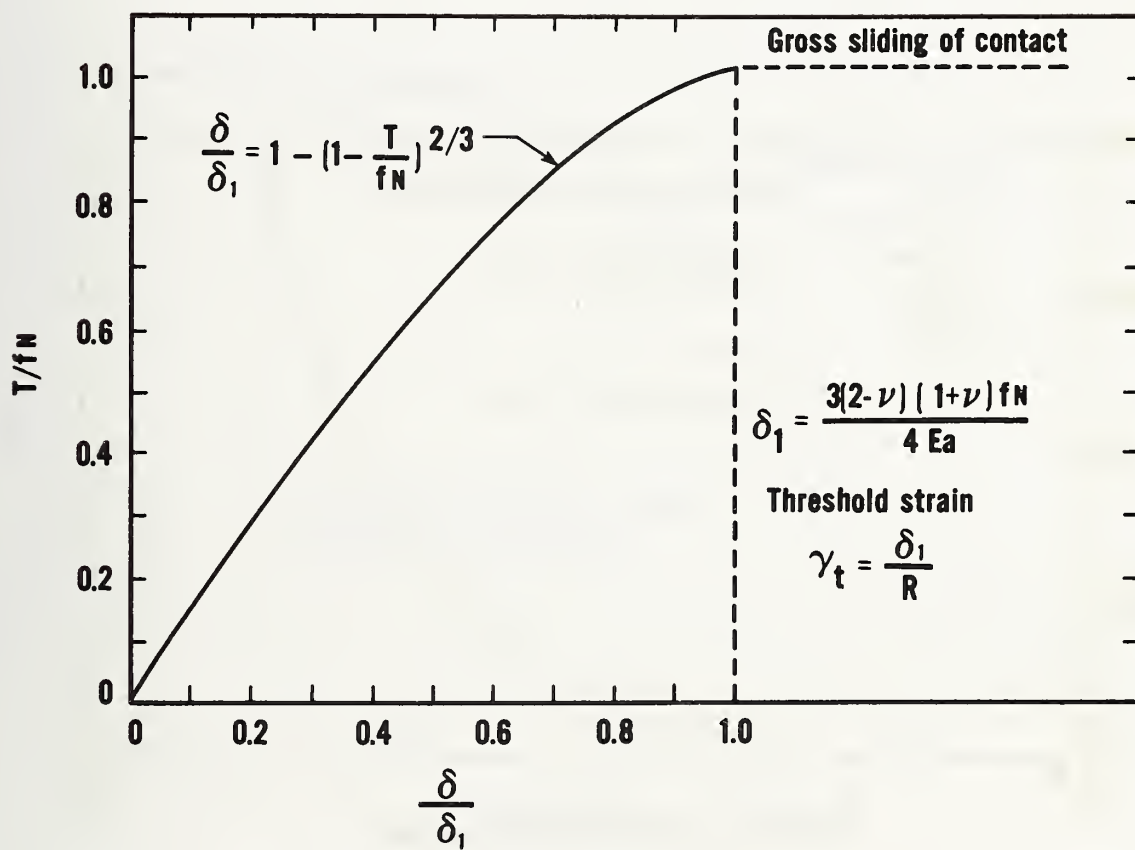


Figure 4.6 Tangential force-displacement relation for two elastic spheres under constant normal force, N (Dobry and Grivas, 1978)

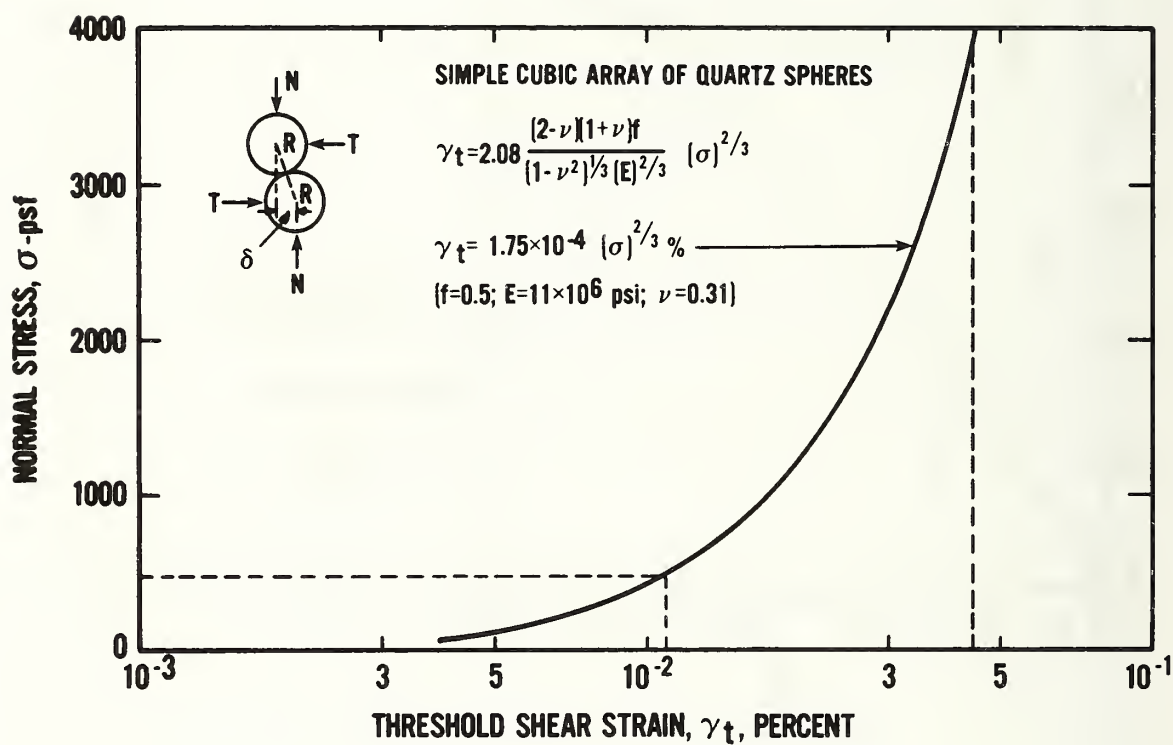


Figure 4.7 Calculated threshold shear strain as a function of isotropic confining stress for a simple cubic array of quartz spheres (Dobry and Swiger, 1979)

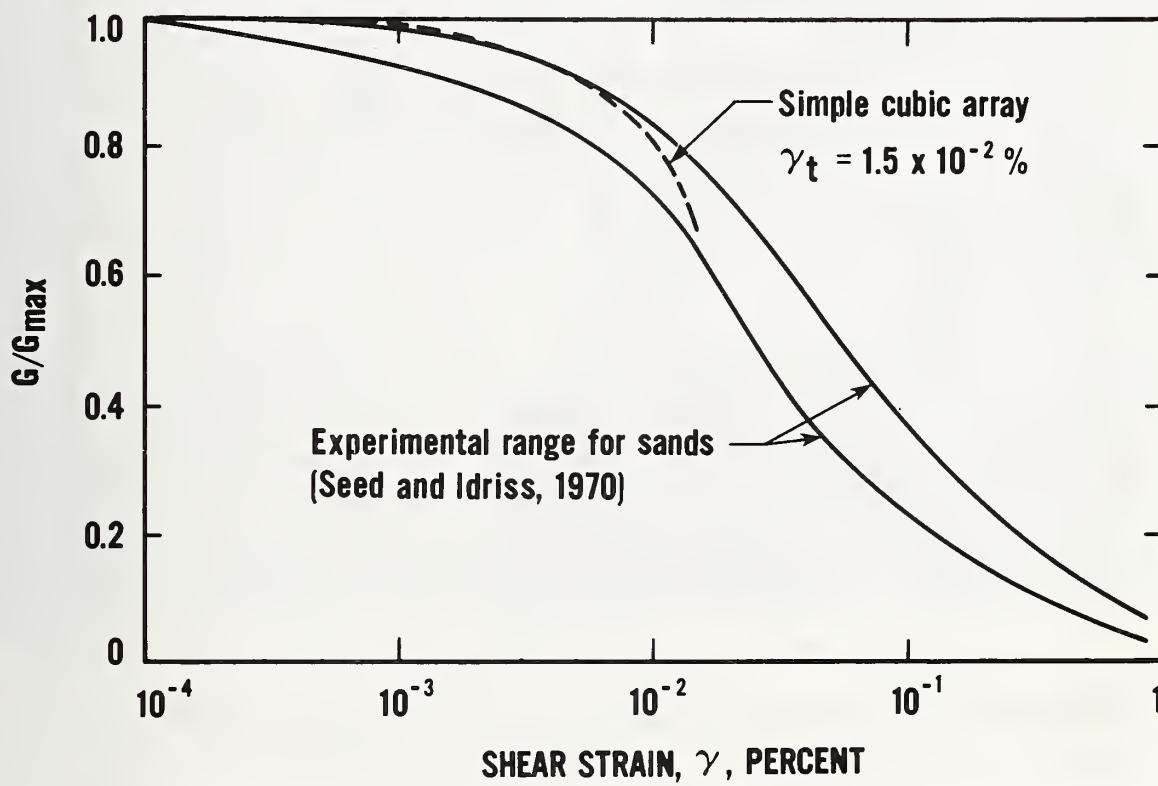


Figure 4.8 Reduction of shear modulus as a function of shear strain - comparison between calculated G/G_{\max} for a simple cubic array and experimental range for sand

FACING PAGE: Ground cracks which developed during the San Fernando February 9, 1971, earthquake in compacted fill above loose saturated sand at the partially completed Jensen Filtration Plant.

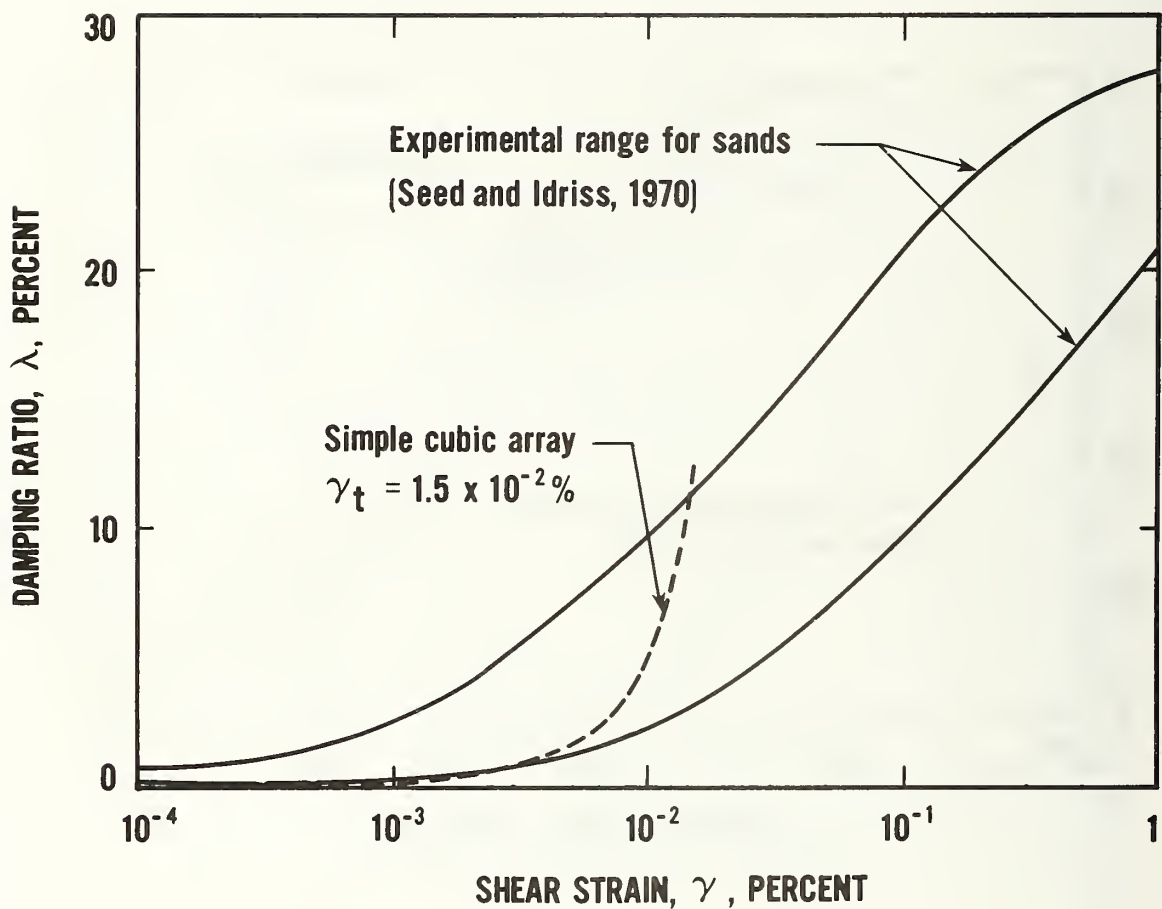


Figure 4.9 Damping ratio as a function of shear strain - comparison between calculated λ for a simple cubic array and experimental range for sand



5. CYCLIC LABORATORY MEASUREMENTS

5.1 GENERAL

This chapter presents the results of a program of undrained cyclic triaxial tests performed on specimens of saturated Monterey No. 0 sand. The tests were performed during the summer of 1979, as part of the development of the cyclic strain approach to evaluate liquefaction potential, described in this report.

For the reasons discussed in chapter 3, all cyclic tests were of the strain-controlled type. A key parameter needed for the cyclic strain approach is the shear modulus of the soil, G . Therefore, a major objective of the tests was to obtain both G at small strains (G_{\max}), and the variation of G and G/G_{\max} with cyclic shear strain amplitude, $\pm \gamma$, and with number of loading cycles, n . Another key parameter needed in the approach is the threshold strain, γ_t , which was also measured during the tests. The measurements of G at small

strains and of γ_t involved the use of an improved experimental technique recently developed by one of the authors (Ladd). Finally, the development of excess pore water pressure, Δu , with number of cycles, n , of strain-controlled loading, was also measured during the tests and is reported in this chapter. In addition, the influence of relative density (D_r) and of initial confining pressure (σ_3) on G , G/G_{\max} , γ_t and Δu was studied and is discussed in this chapter.

5.1.1 Sand Tested

The particle size distribution curve and the selected index properties of the Monterey No. 0 sand, obtained by Mulilis et al., (1975 [54]) are shown in figure 5.1 and table 5.1, respectively. The sand is a commercially available washed uniform medium-to-fine beach sand (SP), composed of quartz and feldspar particles. The maximum and minimum dry unit weight determinations were performed in accordance with the ASTM Test for Relative Density of Cohesionless Soils (D 2049-69) and Kolbuszewski's (1948 [39]) method, respectively. The specimens tested had initial relative densities, D_r , of approximately 45, 60, and 80 percent, and were prepared using the moist tamping compaction method (Ladd 1978 [44]). It should be noted that the same type of sand was used at the University of California at Berkeley to perform a number of studies on sand liquefaction and densification during earthquakes (e.g., see DeAlba, et al., 1975 [14] and Pyke et al., 1974 [65]).

5.1.2 Testing Technique

The techniques used for specimen preparation and testing include unique features such as the undercompaction of the lower layers of the specimen to achieve a more uniform density, and the capability to measure modulus and pore water pressure response at very small strains ($\gamma \approx 10^{-3}$ percent). Details of the undercompaction moist tamping technique are given by Ladd (1978 [44]).

The improved technique which has allowed extending the testing capability of cyclic triaxial equipment from $\gamma \approx 10^{-2}$ percent to $\gamma \approx 10^{-3}$ percent includes:

- (a) a frictionless loading system with precise axial alignment (air bushing and specially machined and ground components),
- (b) precise coupling between porous stones and top and bottom platens (individually lapped and indexed) and test specimen and porous stones (refined compaction techniques),
- (c) a correction for equipment compliance (see figure 5.2), and
- (d) very sensitive recording systems (load to 0.01 pound and deformation to 1×10^{-6} inch).

Additional details on the specimen preparation and testing techniques are given in the following paragraphs, while the method of performing the calculations is included in the appendix. An electrohydraulic closed-loop loading

Table 5.1 Index Properties for Monterey No. 0 Sand
Mulilis et al. (1975)

Unified Soil Classification System Group symbol	SP
Mean Specific Gravity	2.65
Particle Size Distribution Data	
D ₅₀ , mm	0.36
C _c (1)	0.9
C _u (2)	1.5
Dry Unit Weight Data	
Maximum, pcf	105.7
Minimum, pcf	89.3

(1) $C_c = (D_{30})^2 / (D_{60} \times D_{10})$

(2) $C_u = D_{60} / D_{10}$

system and specially designed and manufactured triaxial cells, were used in all tests.

The strain-controlled cyclic triaxial tests were performed in general accordance with the procedures outlined by Silver (1975 [82]) and Park and Silver (1975 [59]).

The key points followed in performing the tests are:

- 1) Each specimen was reconstituted using the moist tamping method as outlined by Ladd (1978 [44]), using a compaction mold attached to the base of the triaxial cell. This method ensures a "perfect" contact between the specimen and the loading platens. In addition, in these tests, some of which involved low relative densities, it was found that, to obtain a "perfect" contact: a) the bottom layer had to be placed and compacted in two parts, and b) the top layer had to be partially compacted, then scarified, the top stone inserted and twisted to get it seated properly and then compacted to the prescribed density, with all equipment in place, by striking the top of the loading piston.
- 2) Each specimen was saturated by backpressuring (backpressuring is done by gradually increasing the backpressure and cell pressure simultaneously) at an effective stress of 5 psi (34.5 kPa). The test specimen was considered to be saturated if the pore pressure response (B-parameter) was equal to or greater than 95 percent.

To assist in the saturation of the specimen, carbon dioxide (CO₂) and deaired water were percolated through the specimen prior to backpressuring. A backpressure of 70 psi (483 kPa) was applied in all tests.

- 3) Each specimen was isotropically consolidated in increments to the final effective confining pressure of the test, σ_3^f , on the day prior to performing the cyclic test.
- 4) During backpressuring and consolidation, the triaxial cell was completely filled with water (which had been deaired at the start of the test) and axial deformations and volume changes of the specimens were recorded. In addition, a small axial load was applied to the piston screwed into the top cap, sufficient to maintain the specimen in an isotropic state of stress.
- 5) Prior to cyclic loading, the triaxial cell was transferred from the consolidation area to the cyclic loading apparatus. During this stage, the applied values of cell pressure, axial load, and backpressure were maintained constant.
- 6) The specimen was cyclically loaded without drainage using the electrohydraulic closed-loop loading system. The system applied a sinusoidally-varying cyclic load or deformation at a frequency of 1 Hz. Just prior to cyclic loading, an air pocket was formed at the top of the cell and the O-ring seal (which was attached to the bushing assembly) was

removed, thereby switching over to an air bushing housed in the bushing assembly. During cyclic testing, changes in axial load, axial deformation, and pore water pressure were recorded on a 7-in. oscillograph recorder. These values were typically recorded within a resolution of two percent of the recorded maximum value. In addition, an x-y recorder was used to obtain hysteresis loops of selected loading cycles.

5.1.3 Test Program

A total of 12 undrained strain-controlled cyclic triaxial tests were performed on saturated specimens of Monterey No. 0 sand. The list of tests is presented in table 5.2.

With the exception of test 12, which was a staged test, all other tests used fresh specimens. These 11 tests were all very similar, with the confining pressure, σ_3 , relative density, D_r , and cyclic shear strain, γ , of the test being varied between tests. Most of the tests were conducted with $\sigma_3 = 2,000$ psf, except for tests 10 and 11, where $\sigma_3 = 533$ psf and 4,000 psf, respectively. Three relative densities, 45, 60, and 80 percent and three values of γ , 3×10^{-2} , 1×10^{-1} and 3×10^{-1} percent, were used. Table 5.3 shows in a matrix form the values of D_r and γ corresponding to each test for $\sigma_3 = 2,000$ psf.

The typical undrained cyclic testing sequence for each test was as follows:

- a) Measurements at very small strains. Measurements of G and pore water pressure response (Δu) were made at very small cyclic strains, 10^{-3} percent $< \gamma < 10^{-2}$ percent. These measurements were done by applying cyclic loads. Several levels (stages) of cyclic loads were typically applied with five loading cycles being applied in each stage. In addition to measuring the pore water pressure during cyclic loading, Δu , the residual pore water pressure, Δu_r , was also measured after cyclic loading was stopped. All these measurements were nondestructive, as verified by the fact that $\Delta u_r = 0$, and also by the repeatability of the values of G at the given γ , irrespective of the previous history of small strain cyclic loading.
- b) Measurement of γ_t . This was done by applying 10 cycles of a value of cyclic strain, γ , slightly larger than γ_t , usually in the range 1×10^{-2} percent $< \gamma < 2 \times 10^{-2}$ percent. Both Δu during cyclic testing and Δu_r after the 10 cycles were recorded. Invariably the measured values of Δu and Δu_r were very small. The shear modulus, G , was also measured during these 10 cycles; it usually varied little between the first and last cycle. After measuring Δu_r , the drainage valves were opened and reconsolidation of the system was allowed for.
- c) Measurements at very small strains. Same as in step (a) above. This was done to verify that the G values at very small strains had not been significantly affected by step (b), thus, confirming the assumption that step (b) could be considered nondestructive for practical purposes.

Table 5.2 List of Cyclic Triaxial Tests

Test No.	Confining Pressure, σ_3^1 psf	Relative Density, D_r percent	Cyclic Shear Strain, γ percent
1	2,000(1)	45	3×10^{-2}
2	2,000	45	1×10^{-1}
3	2,000	45	1×10^{-1}
4	2,000	45	3×10^{-1}
5	2,000	60	3×10^{-2}
6	2,000	60	1×10^{-1}
7	2,000	60	3×10^{-1}
8	2,000	80	1×10^{-1}
9	2,000	80	3×10^{-1}
10	533	60	3×10^{-2}
11	4,000	60	3×10^{-2}
12	533-944- 2,000-4,000 (Staged Test)	45	---

(1) 1 psf = 47.8 pascal

Table 5.3

Cyclic Triaxial Tests with $\sigma'_3 = 2,000$ psf⁽¹⁾

Relative Density D_r , percent	Cyclic Shear Strain, γ , Percent		
	3×10^{-2}	1×10^{-1}	3×10^{-1}
45	Test 1	Test 2	-
	-	Test 3	Test 4
60	Test 5	Test 6	Test 7
80	-	Test 8	Test 9

(1) 1 psf = 47.8 pascal.

- d) Testing at $\gamma > \gamma_t$, (destructive testing). Strain-controlled cyclic testing was performed at the cyclic strain of the test, γ . This is the cyclic strain reported in tables 5.2 and 5.3. In most cases the test was carried to 100 cycles or to initial liquefaction ($\Delta u = \sigma'_3$), whichever occurred first. However, tests 1, 10, and 11 were carried to 1,000 cycles. During each test the shear modulus, G , the damping ratio, λ , and the maximum pore water pressure, Δu , during the cycle were measured as a function of the number of cycles, n . In addition, the test was stopped at selected numbers of cycles to allow for measurement of the residual pore water pressure, Δu_r , and then restarted without reconsolidation.

Of special concern during the planning of the testing program was the assumed nondestructive character of step (b). To further verify this assumption, tests 2 and 3 were conducted. These two tests are identical in all respects, except that step (b) was skipped in test 2, and step (a) was followed immediately by the destructive testing (step d). The results of the two tests 2 and 3 were essentially identical, thereby verifying the nondestructive character of step (b).

Test 12 was a staged test, with stages at $\sigma'_3 = 533$ psf, 994 psf, 2,000 psf, and 4,000 psf, respectively. Cyclic loading was performed undrained at each stage, and excess pore water pressures were dissipated by reconsolidation between stages. Except for the first stage at 533 psf, the results of this test were obviously affected by the reconsolidation process and associated curing period and are not included in the detailed presentation of results included in this chapter. Further research is definitely needed on the feasibility of staged cyclic tests for determining γ_t and Δu_r .

5.2 SHEAR MODULUS AND DAMPING RATIO

Figures 5.3 through 5.10 present the experimental results for the shear modulus, G , and the damping ratio, λ . In all cases, G was measured as the secant modulus between the compression and extension peaks within the same cycle.

Figures 5.3, 5.4, and 5.5 summarize the values of G at $\sigma'_3 = 2,000$ psf, and for $D_r = 45, 60$, and 80 percent, respectively. In these figures, G is plotted versus shear strain, γ , at $n = 1$ cycle and $n = 30$ cycles. The data points for strains below or about 10^{-2} percent were determined during the nondestructive very small strain measurements (step (a) in section 5.1.3), while the data points at larger strains were obtained during the destructive measurements in step (d).

Estimated values of G_{max} were obtained using the Hardin and Drnevich (1972 [29]) equation for sands isotropically consolidated under a pressure σ'_3 :

$$G_{max} = 1230 \frac{(2.973 - e)^2}{1 + e} (\sigma'_3)^{1/2}, \quad \text{where } G_{max}, \sigma'_3 \text{ in psi} \quad 5.1$$

These G_{max} estimates are included in table 5.4 and have been superimposed on figures 5.3 to 5.5. The comparisons in these figures indicate excellent agreement between the values of G measured at very small strains ($\gamma \approx 10^{-3}$ percent)

Table 5.4 G_{\max} at $\sigma'_3 = 2,000$ psf⁽¹⁾ for Monterey No. 0 Sand

D_r percent	e	Hardin-Drnevich G_{\max} ⁽²⁾
45	0.72	1,940 ksf ⁽¹⁾
60	0.68	2,070
80	0.63	2,230

- (1) 1 psf = 47.8 pascal
1 ksf = 47.8 kpa

- (2) $G_{\max} = 1230 \frac{(2.973-e)^2}{1+e} (\sigma'_3)^{1/2}$, with G_{\max}
and σ'_3 in psi from Hardin and Drnevich (1972)

during the cyclic triaxial tests on Monterey No. 0 sand, and G_{\max} calculated using equation 5.1.

The comparison between the curves for $n = 1$ cycle and $n = 30$ cycles in figures 5.3 through 5.5 confirm that G at $\gamma \leq 10^{-2}$ percent is independent of number of cycles. For larger strains, the discrepancy between the two curves increases, indicating that modulus degradation occurs during cyclic loading, with the degradation increasing as γ increases.

Figure 5.6 compares the three experimental curves of figures 5.3 through 5.5, without the data points and only for $n = 1$.

Figure 5.7 shows the results of measurements of the damping ratio, λ , during the destructive testing in step (d), for $\sigma_3 = 2,000$ psf and for all three relative densities tested. Since λ could not be measured during the first cycle, the results presented in the figure are for $n = 2$ and $n = 30$ cycles. For $\gamma \approx 3 \times 10^{-2}$ percent, $\lambda \approx 7$ percent, with negligible influence of n . For $\gamma \approx 3 \times 10^{-1}$ percent, $\lambda = 20$ to 30 percent, with a tendency to decrease with the number of cycles. The trend of increase of λ with γ and the numerical values plotted in figure 5.7 are in general agreement with the results reported for sands by other authors (e.g., see Seed and Idriss, 1970 [77]).

Figure 5.8 presents the influence of σ_3 on the measured values of G versus γ , for $D_r = 60$ percent and $n = 1$ cycle. The corresponding values of G_{\max} calculated using equation 5.1 have also been included in the figure, and again there is good agreement between G at very small strains measured during the tests and Hardin and Drnevich's expression.

The comparisons in figures 5.3 through 5.8 between measured modulus reduction curves and G_{\max} values estimated with eq. 5.1, are very encouraging. They suggest that cyclic triaxial tests can be used to measure G_{\max} , if the improved testing techniques described herein are used. The band of experimental results for G/G_{\max} versus γ compiled by Seed and Idriss for sands, and included in figure 4.8, indicates that, at $\gamma = 10^{-3}$ percent, $G/G_{\max} = 0.95$ to 0.98. Therefore, G_{\max} was estimated using equation 5.2:

$$G_{\max} = \frac{(G)_{\gamma = 10^{-3}\%}}{0.95 \text{ to } 0.98} \quad 5.2$$

The values of G_{\max} for $D_r = 60$ percent and $\sigma_3 = 533$ psf, 2,000 psf and 4,000 psf, were calculated from the values of $(G)_{\gamma = 10^{-3}}$ percent in the experimental curves in figure 5.8 using equation 5.2. These values of G_{\max} were plotted versus σ_3 as data points in figure 5.9. Figure 5.9 also includes two other plots of G_{\max} versus σ_3 for comparison. The dashed line was obtained from Hardin and Drnevich, equation 5.1. The solid lines were obtained from the Round Robin resonant column test program on Monterey No. 0 sand (Drnevich, 1979 [22]). In the Round Robin test program, G_{\max} was measured by nine laboratories on specimens of dry Monterey No. 0 sand all using an identical sand placement procedure and testing technique. The two solid lines in figure 5.9 correspond to the range of values of G_{\max} obtained by the nine laboratories (Drnevich, 1979 [22]). The comparison between G_{\max} obtained herein and the results of of the Round

Robin test program confirm that, with the improved testing techniques used here, cyclic triaxial test measurements at $\gamma \approx 10^{-3}$ percent are feasible and can produce reliable values of G_{\max} .

An additional check of the cyclic triaxial measurements of G is presented in figure 5.10. The data points in figure 5.10 are the same as presented in figure 5.8, for $D_r = 60$ percent and $n = 1$ cycle, except that in figure 5.10, K_2 is plotted versus γ . K_2 is a normalized parameter, obtained from Seed and Idriss' (1970 [77]) equation for G :

$$G = 1,000 K_2 (\sigma'_3)^{1/2} \quad \text{where } G, \sigma'_3 \text{ in psf} \quad 5.3$$

Therefore, $K_2 = G/(\sigma'_3)^{1/2}$ if G is expressed in ksf and σ'_3 in psf. In the Round Robin resonant column testing program, tests were performed at $\sigma'_3 = 1,040$ and 6,250 psf, respectively. The average values of G_{\max} for the nine laboratories at these pressures, in conjunction with equation 5.3, gave values of $K_{2\max}$ of 50.4 and 47, respectively. These values of $K_{2\max}$ were plotted in figure 5.10, together with the corresponding curves of K_2 versus γ predicted using:

$$(K_2)_\gamma = K_{2\max} \left(\frac{K_2}{K_{2\max}} \right)_\gamma \quad 5.4$$

where the curve of $(K_2/K_{2\max})_\gamma = (G/G_{\max})$ versus γ selected for the calculations is the average curve for sands suggested by Seed and Idriss (1971 [77]) (average of the experimental band in figure 4.8).

The agreement in figure 5.10 between the data points and the curves obtained combining the Round Robin's results with those of Seed and Idriss curve is excellent at both small and large strains. The only exceptions are the data points for $\sigma'_3 = 4,000$ psf and $\gamma > 10^{-2}$ percent, which plot somewhat higher than the curves and the rest of the data points, with increasing discrepancy at larger strains. This discrepancy would tend to confirm the tendency of G/G_{\max} to be somewhat higher in soils at larger confining pressures, as discussed by Iwasaki et al., (1978 [33]), and Richart (1980 [66]). A similar effect was already discussed for the simple cubic array model in section 4.4. In any case, the comparison in figure 5.10 further validates the experimental values of G obtained in this research with the cyclic triaxial technique.

5.3 MODULUS DEGRADATION UNDER CYCLIC LOADING

In the destructive part of the strain-controlled tests ($\gamma > \gamma_t$), there was both pore water pressure buildup and degradation of the modulus with number of cycles, n . This modulus degradation effect is presented in figures 5.11 through 5.17, as experimental curves of G/G_1 versus n . In all cases, G_1 is the secant modulus measured in the first cycle conducted at the cyclic strain of the test, γ . The influence of γ on the curves of G/G_1 versus n is presented in figures 5.11, 5.12, and 5.13, for $D_r = 45, 60$ and 80 percent, respectively. These figures show that G/G_1 is significantly affected by both n and γ , with G/G_1 decreasing rapidly as γ increases above 10^{-2} percent.

Figures 5.14, 5.15, and 5.16 illustrate the effect of D_r on the curves of G/G_1 versus n for $\gamma = 3 \times 10^{-2}$, 1×10^{-1} , and 3×10^{-1} percent, respectively. These figures show that G/G_1 is significantly affected by relative density, with modulus degradation being more pronounced at the lower relative densities. Figure 5.17 shows the influence of confining pressure, for $D_r = 60$ percent and $\gamma = 3 \times 10^{-2}$ percent. Other things being equal, this figure suggests that modulus degradation is more significant at lower values of σ'_3 .

5.4 THRESHOLD STRAIN

Figures 5.18 and 5.19 show the results of the threshold strain measurements in steps (a) and (b) of the tests (see section 5.1.3), while figure 5.20 presents relevant results on γ_t for dry Monterey No. 0 sand obtained by Pyke (1973 [64]).

Figure 5.18 includes the values of the residual pore water pressure, Δu_r after $n = 10$ cycles, for $\sigma'_3 = 2,000$ psf and for the three relative densities tested. Note that the values of $\Delta u_r/\sigma'_3$ in the figure are very low and smaller than 0.1 (a value of $\Delta u/\sigma'_3 \approx 1.0$ would indicate initial liquefaction). Therefore, figure 5.18 permits determining the value of the threshold strain with a high degree of precision. Figure 5.18 demonstrates that:

- a) For the sand tested and for $\sigma'_3 = 2,000$ psf, the threshold strain is $\gamma_t \approx 1.1 \times 10^{-2}$ percent. This value of γ_t is independent of relative density in the range $45 \text{ percent} < D_r < 80 \text{ percent}$.
- b) For values of strain slightly larger than γ_t ($1.1 \times 10^{-2} \text{ percent} < \gamma < 3 \times 10^{-2} \text{ percent}$), the residual pore water pressure, Δu_r , increases rapidly with strain, and the value of Δu_r is again independent of relative density for the range studied.

Figure 5.19 shows the influence of confining pressure, σ'_3 on γ_t and Δu_r at strains up to $\gamma \approx 3 \times 10^{-2}$ percent. The curve for $\sigma'_3 = 2,000$ psf from figure 5.18 has been superimposed for comparison. The data points in figure 5.19 corresponding to $\sigma'_3 = 533$ psf were obtained from test 10 (open triangles, $D_r = 60$ percent) and from the first step of test 12 (black triangles, $D_r = 45$ percent). The data points for $\sigma'_3 = 4,000$ psf were obtained from test 11. Figure 5.19 suggests that the value of $\gamma_t \approx 1.1 \times 10^{-2}$ percent is valid for the range of pressures, $533 \text{ psf} < \sigma'_3 < 4,000 \text{ psf}$, and that the same curve of $\Delta u_r/\sigma'_3$ versus γ is valid for $\sigma'_3 = 533$ psf and $\sigma'_3 = 2,000$ psf, with this curve being independent of relative density. Although the evidence presented is not conclusive, figure 5.19 seems to suggest that $\Delta u_r/\sigma'_3$ at small strains above the threshold is somewhat smaller for $\sigma'_3 = 4,000$ psf than for $533 \text{ psf} \leq \sigma'_3 \leq 2,000 \text{ psf}$.

Figure 5.20 presents evidence on γ_t from cyclic, strain-controlled simple shear tests on dry Monterey No. 0 sand, conducted by Pyke (1973 [64]). The tests were performed on specimens placed at relative densities, D_r , between 40 percent and 80 percent, and normally consolidated to vertical pressures, σ_v , between 800 psf and 3600 psf. The plot shows the settlement in the first loading cycle, versus strain, γ . It can be seen that the settlement depends strongly on γ and on D_r , but it does not depend on σ_v . This is consistent with the

conclusion from similar tests on other sands discussed in section 3.2.2. In figure 5.20, the settlement in the first cycle becomes zero at $\gamma \approx 0.01 = 10^{-2}$ percent, independent of D_r and σ_v , thus, again suggesting $\gamma_t \approx 10^{-2}$ percent. Therefore, based on the evidence presented in figures 5.18 through 5.20, it can be concluded that $\gamma_t \approx 10^{-2}$ percent for normally (isotropically and anisotropically) consolidated Monterey No. 0 sand, with this value being valid over a wide range of relative densities and confining pressures of practical interest, for both dry and saturated sand and for triaxial and simple shear cyclic loading conditions. This independence of $\gamma_t \approx 10^{-2}$ percent from variations in the confining pressure is unexpected, as the simple cubic array model predicts an increase in γ_t as σ_3 increases (see section 4.3 and figure 4.7).

5.5 EXCESS PORE WATER PRESSURE

Figures 5.21 through 5.33 present the experimental results for the excess pore water pressure, Δu , measured during the strain-controlled cyclic triaxial tests. Note that all these plots depict Δu , the maximum value measured for the corresponding cycle during cyclic loading, rather than Δu_r , the residual value measured after stopping the cyclic loading. Figure 5.34 attempts to relate Δu and Δu_r .

Figures 5.21, 5.22 and 5.23 summarize the experimental results for $\sigma_3 = 2,000$ psf, as plots of $\Delta u/\sigma_3$ versus n for $D_r = 45, 60$, and 80 percent, respectively. These figures show that Δu increases significantly as both γ and n increase.

Figure 5.24, 5.25 and 5.26 illustrate the effect of D_r on the curves of $\Delta u/\sigma_3$ versus n , for $\gamma = 3 \times 10^{-2}$, 1×10^{-1} and 3×10^{-1} percent, respectively. As it could be expected, the pore water pressure increases as D_r decreases. However, the effect is less marked than it could be expected from plots of densification of Monterey dry sand under cyclic loading, such as shown in figures 1.2 and 5.20. At a small number of cycles, $n \leq 10$, Δu is not generally affected or is only moderately affected by D_r .

The reason why pore water pressure buildup in saturated sand is less affected by relative density than by densification of the same dry sand is not difficult to understand. If $(\Delta u)_1$ is the pore pressure increment for saturated sand corresponding to one cycle of cyclic strain, and $(\Delta \epsilon_{vol})_1$ is the volumetric strain decrement corresponding to the same dry sand having the same relative density and subjected to the same cyclic strain, then (Δu) and $(\Delta \epsilon_{vol})$ are related approximately as follows:

$$(\Delta u)_1 \approx \bar{E}_r (\Delta \epsilon_{vol})_1 \quad 5.5$$

where \bar{E}_r = drained tangent modulus of one-dimensional unloading curve of the sand (Martin et al., 1975 [49]). Although equation 5.5 was originally developed for simple shear tests, it will be assumed here for the sake of this discussion, that the same expression, or a similar one, also applies to triaxial tests. For the case of cyclic triaxial tests, $(\Delta u)_1$ should strictly be interpreted as the residual value, Δu_r , rather than the Δu values included in the plots. However, the difference between Δu and Δu_r does not seem to be affected by D_r , and therefore, this should not affect the present discussion. The

important point about the theoretical equation 5.5 is that if D_r increases, $(\Delta\epsilon_{vol})_1$ decreases but \bar{E}_r increases (a dense sand is stiffer than the same sand in a looser state). Therefore, $(\Delta u)_1$ is bound to be less affected by D_r than $(\Delta\epsilon_{vol})_1$, which is exactly what the experimental results show.

Figure 5.27 shows the influence of confining pressure, for $D_r = 60$ percent and $\gamma = 3 \times 10^{-2}$ percent. Other things being equal, normalized pore water pressure buildup at this low γ is faster at lower values of σ'_3 . The effect is not very significant at low numbers of cycles, but it becomes quite dramatic at $n = 1,000$ cycles. An interesting corollary is that if figure 5.27 were denormalized (i.e., Δu were plotted versus n), the difference would almost disappear, with the curves plotting very close to each other.

Figure 5.28, 5.29, and 5.30 summarize the results for $\sigma'_3 = 2,000$, as plots of $\Delta u/\sigma'_3$ versus γ for different numbers of cycles, and for $D_r = 45, 60$, and 80 percent, respectively. The format of these figures is very useful for the purposes of the cyclic strain approach to liquefaction, and is the same used for other sands in figures 3.23 and 3.24.

Figures 5.28 through 5.30 show again that the pore water pressure buildup for $\gamma < \gamma_t \approx 10^{-2}$ percent is insignificant, and that this conclusion is independent of number of cycles and is valid for the three relative densities shown. Δu is not exactly equal to zero for $\gamma < 10^{-2}$ percent in the plots, due to the difference between Δu and Δu_r (compare fig. 5.28 with fig. 5.18). Figures 5.28 through 5.30 show that Δu increases significantly as both γ and n increase.

Figures 5.31 and 5.32 show the effect of D_r on $\Delta u/\sigma'_3$ for $\sigma'_3 = 2,000$ psf and for $n = 10$ and 30 cycles, respectively. As discussed before, there is a slight but not dramatic influence of D_r on Δu . For some practical purposes, a representative band of results could well be taken from either figure and used irrespective of D_r . This is a very important practical conclusion. It is usually very difficult to estimate relative densities in the field and, therefore, the ability to predict pore pressure development without knowing the relative density can be very valuable.

It is of interest to compare the data on excess pore water pressures in Monterey No. 0 sand, presented here, with experimental data for other sands. Figure 3.24 compiled results for various sands and placement techniques, obtained for $D_r = 60$ percent and $n = 10$ cycles during strain-controlled cyclic triaxial tests. All the data in figure 3.24 were for a range of $\sigma'_3 = 1,400$ to 2,800 psf. Figure 3.24 is reproduced in figure 5.33, where the data points for Monterey No. 0 sand have also been added. The data for Monterey No. 0 sand, obtained in this study and included in figure 5.33, are for $D_r = 60$ percent and $\sigma'_3 = 2,000$ psf. The agreement in figure 5.33 between the old curve and the new data points for Monterey No. 0 sand is outstanding. This reinforces the conclusion that the curve in figure 5.33 is valid for most clean, normally consolidated, saturated sands subjected to strain-controlled cyclic triaxial testing for $\sigma'_3 = 1,400$ to 2,800 psf, $D_r \approx 60$ percent, and $n = 10$ cycles. It must be reemphasized that the data points in figure 5.33 correspond to three different sands, placed using three different methods, and that the tests were conducted independently at two different laboratories.

5.5.1 Comparison Between Δu and Δu_r

As discussed before, two different types of excess pore water pressure were measured during the cyclic triaxial tests reported here. They were: a) the peak cyclic pore water pressure during cyclic loading, Δu , and b) the residual pore water pressure, measured after cyclic loading had stopped, Δu_r (see also section 5.1.3). In those cases where both Δu and Δu_r were available, invariably $\Delta u \geq \Delta u_r$. In particular, for nondestructive testing at strains below the threshold, $\gamma < 10^{-2}$ percent, $\Delta u_r = 0$ while $\Delta u > 0$.

It seems reasonable to assume that the difference between Δu and Δu_r corresponds to an "elastic" pore water pressure response, associated with the increase in volumetric stress generated by the cyclic loading. Therefore, as a first approximation, the following expression is assumed valid:

$$\Delta u = \Delta u_r + (\Delta u)_{\text{elastic}} \quad 5.6$$

If the soil skeleton is assumed to be both elastic and isotropic, $(\Delta u)_{\text{elastic}}$ should be proportional to the cyclic deviator stress, $\Delta \sigma_1$ (Lambe and Whitman, 1969 [45]) or:

$$(\Delta u)_{\text{elastic}} = \frac{1}{3} \Delta \sigma_1 \quad 5.7$$

Combining equations 5.6 and 5.7, the desired relation between Δu and Δu_r is obtained.

$$\Delta u = \Delta u_r + \frac{1}{3} \Delta \sigma_1 \quad 5.8$$

In particular, at strains lower than 10^{-2} percent, where $\Delta u_r = 0$ and the behavior of the soil could be expected to be close to being elastic and isotropic, $\Delta u = \frac{1}{3} \Delta \sigma_1$ is predicted.

The expression $(\Delta u - \Delta u_r) / (1/3 \Delta \sigma_1)$ was computed for tests 1 through 11, for all cyclic strains and numbers of cycles for which both Δu and Δu_r were available. It was found that, at small strains, above and below the threshold, $\gamma \lesssim 3 \times 10^{-2}$ percent, and for moderate pore pressure buildup, $0.01 \leq \Delta u / \sigma_3' \leq 0.20$, the expression has a fairly constant value, which is $(\Delta u - \Delta u_r) / (1/3 \Delta \sigma_1) = 0.42 \pm 0.07$, as shown in figure 5.34. For values of $\Delta u / \sigma_3'$ outside this range the values are more erratic. Therefore, for small strain testing ($\gamma \lesssim 3 \times 10^{-2}$ percent), above and below the threshold, and for $\Delta u / \sigma_3' \lesssim 0.20$, the plots of $\Delta u / \sigma_3'$ presented in this section could be approximately converted into plots of $\Delta u_r / \sigma_3'$ by means of equation 5.9:

$$\frac{\Delta u_r}{\sigma_3'} = \frac{\Delta u}{\sigma_3'} - \frac{0.14 \Delta \sigma_1}{\sigma_3'} \quad 5.9$$

where $\pm \Delta \sigma_1$ is the cyclic deviator stress. The fact that $(\Delta u - \Delta u_r) / (1/3 \Delta \sigma_1)$ is not equal to 1.0, as predicted by equation 5.8, but instead is equal to 0.42, is probably due to the membrane compliance effect (Martin et al., 1978 [50]).

5.6 PORE WATER PRESSURE AND MODULUS DEGRADATION

Sections 5.3 and 5.5 discussed the modulus degradation and the development of excess pore water pressure during cyclic loading, respectively. Modulus degradation was studied using the normalized parameter G/G_1 , which is 1.0 at the beginning of the destructive cyclic loading and subsequently decreases to values between 0 and 1. Excess pore water pressure buildup was studied by means of the normalized parameter, $\Delta u/\sigma'_3$, which is zero at the beginning and subsequently increases to values between 0 to 1. Both modulus degradation and pore water pressure increase are affected significantly by γ and n , and to a lesser degree by D_r and σ'_3 , and the effect of all these factors is very similar for both G/G_1 and $\Delta u/\sigma'_3$, i.e., the factors which decrease G/G_1 increase $\Delta u/\sigma'_3$ and vice versa. Furthermore, at strains below the threshold, $\gamma < 10^{-2}$ percent, $G/G_1 \approx 1$ and $\Delta u/\sigma'_3 \approx 0$, i.e., they both stay constant, independently of n , D_r and σ'_3 .

It seems reasonable from the above discussion to assume that G/G_1 and $\Delta u/\sigma'_3$ are directly related. To test this hypothesis, the two parameters were plotted together as shown in figure 5.35. Figure 5.35 is reasonably consistent, considering the diversity of test conditions. A single curve could be fitted to the data points as shown in the figure. This relation between $\Delta u/\sigma'_3$ and G/G_1 for Monterey No. 0 sand under cyclic triaxial conditions is of considerable theoretical and practical interest. It suggests that for pore water pressure buildup and liquefaction analyses, the modulus G , can also be calculated using a relation such as that shown in the figure if the pore water pressure, Δu , is known at any time during cyclic loading.

The largest amount of scatter in figure 5.35 occurs near the middle of the plot, for $(1 - (\Delta u/\sigma'_3)) \approx 0.4$ to 0.7 . There, the lowest data points, having somewhat lower modulus degradation for a given pore pressure buildup, correspond to tests 1, 5, 10, and 11, all run with a low cyclic strain, $\gamma = 3 \times 10^{-2}$ percent. Conversely, the highest point corresponds to test 4, run with a high cyclic strain, $\gamma = 3 \times 10^{-1}$ percent. If needed, this influence of γ could be used to refine the correlation of figure 5.35 and decrease its present scatter.

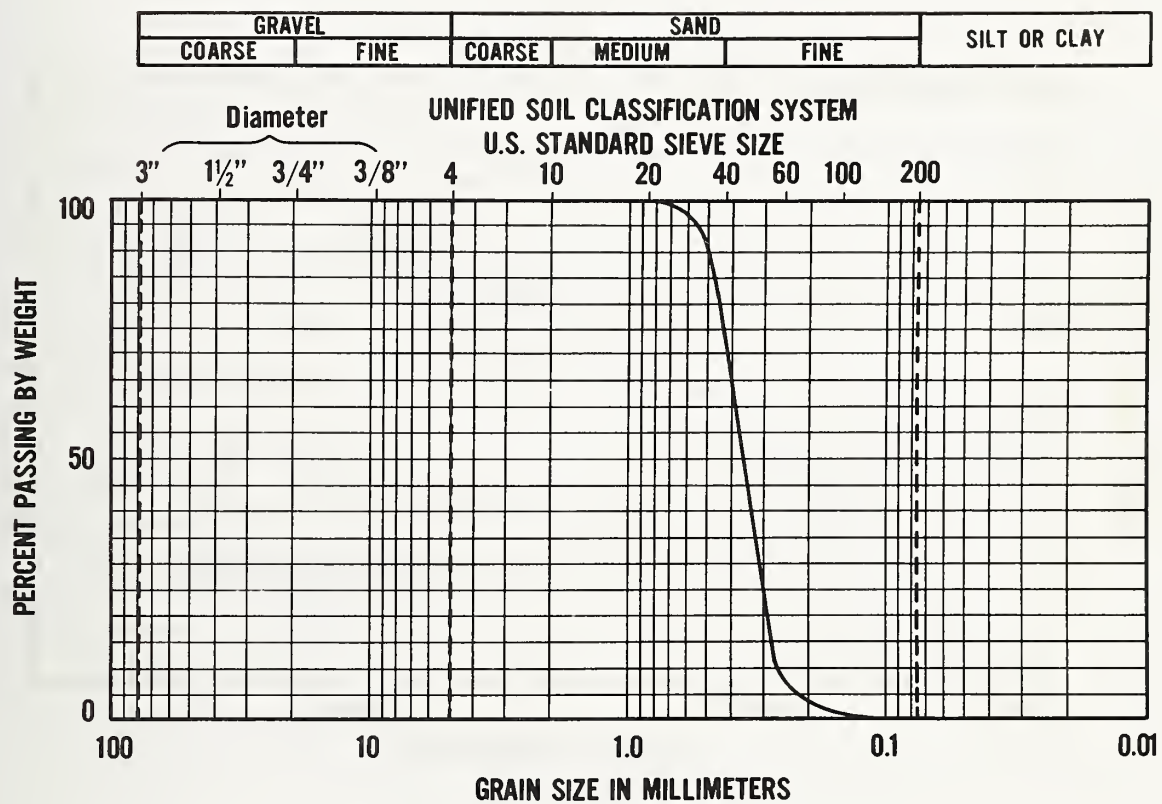


Figure 5.1 Grain size distribution of Monterey No. 0 sand

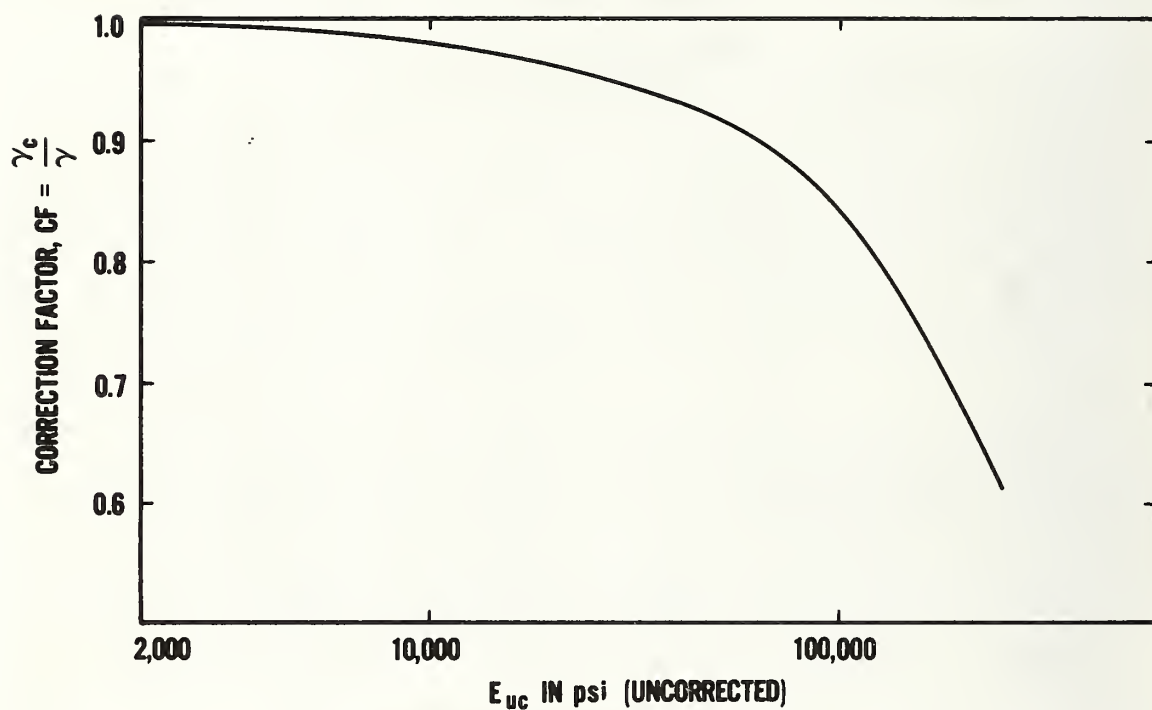


Figure 5.2 Typical correction factor for equipment compliance, cyclic triaxial tests

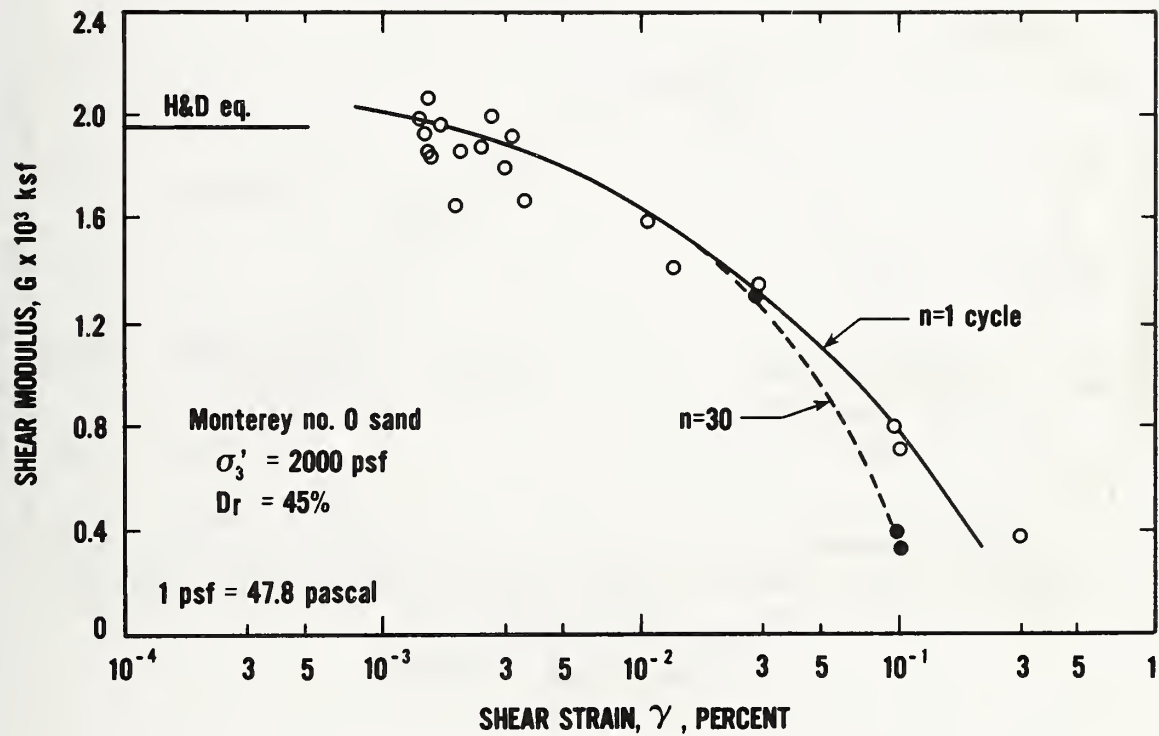


Figure 5.3 Reduction of shear modulus as a function of cyclic shear strain for Monterey No. 0 sand at $\sigma'_3 = 2000$ psf and $D_r = 45$ percent

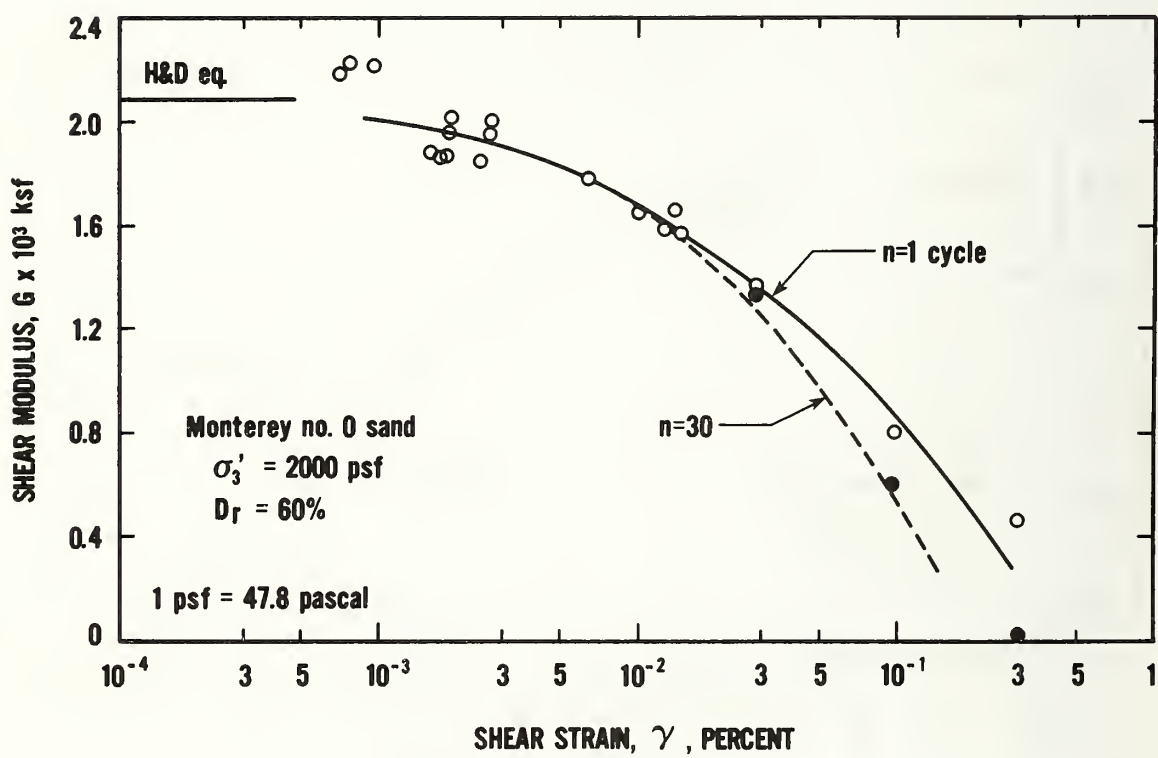


Figure 5.4 Reduction of shear modulus as a function of cyclic shear strain for Monterey No. 0 sand at $\sigma'_3 = 2000$ psf and $D_r = 60$ percent

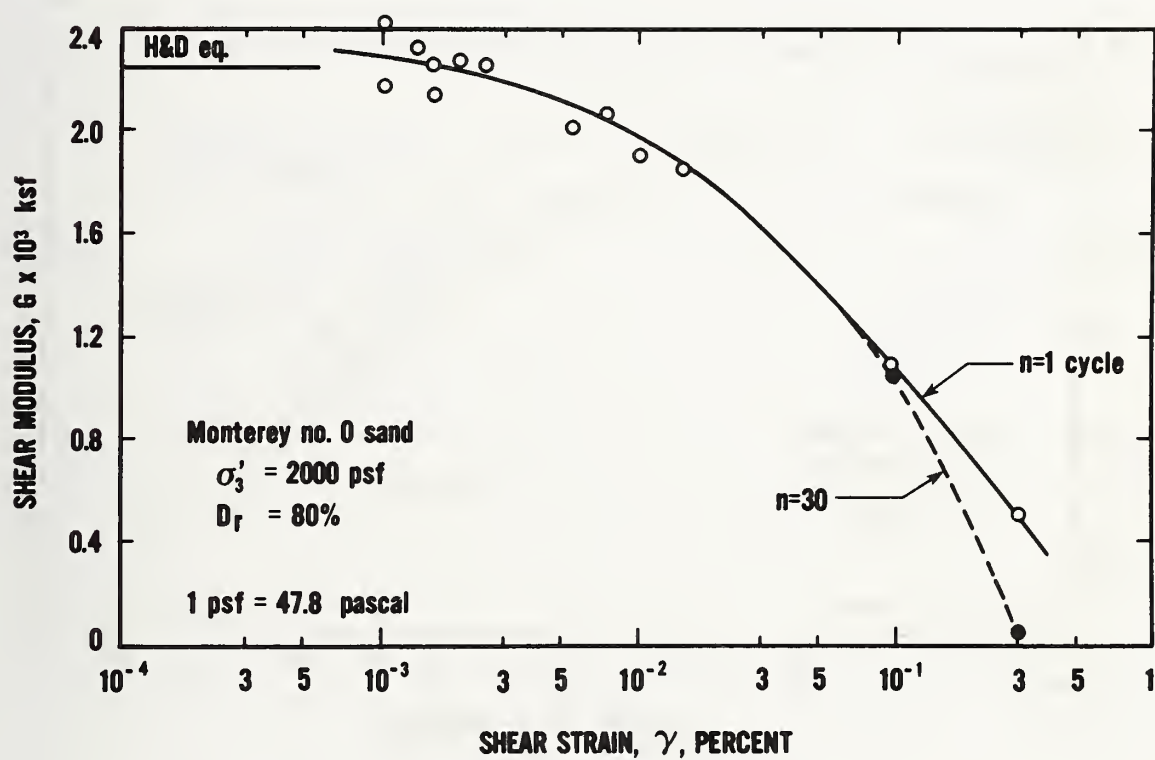


Figure 5.5 Reduction of shear modulus as a function of cyclic shear strain for Monterey No. 0 sand at $\sigma'_3 = 2000$ psf and $D_r = 80$ percent

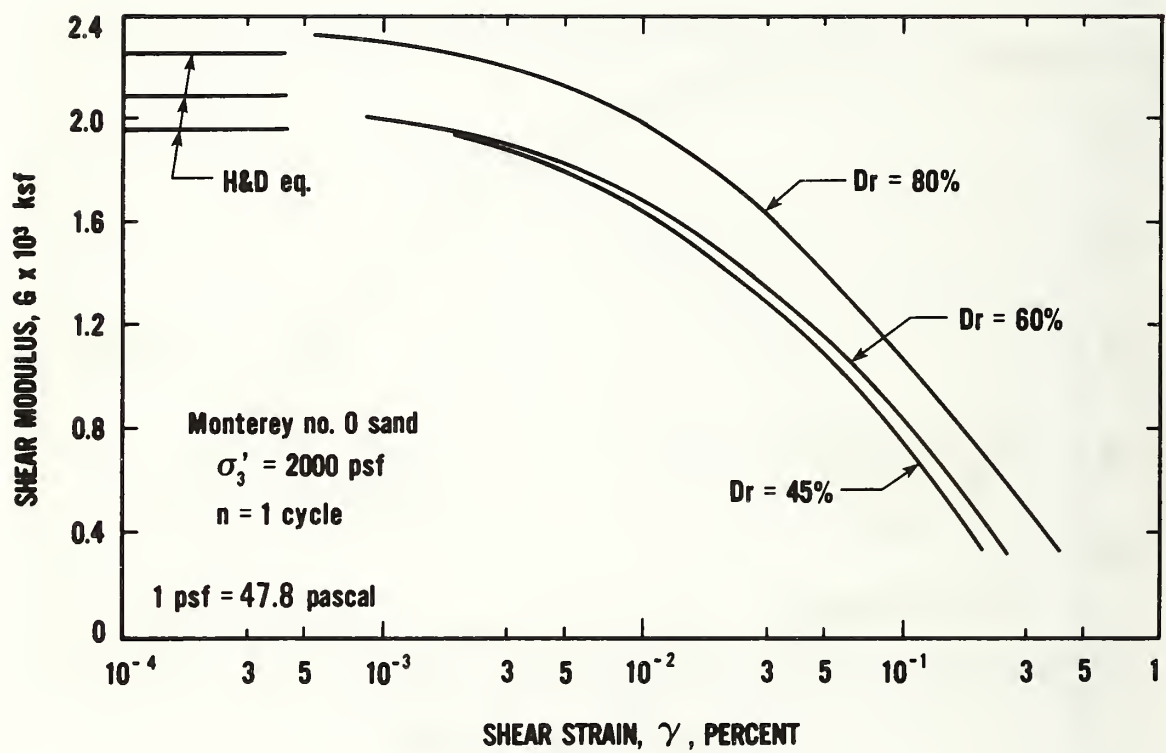


Figure 5.6 Reduction of shear modulus as a function of cyclic shear strain for Monterey No. 0 sand at $\sigma'_3 = 2000$ psf and $D_r = 45, 60$, and 80 percent

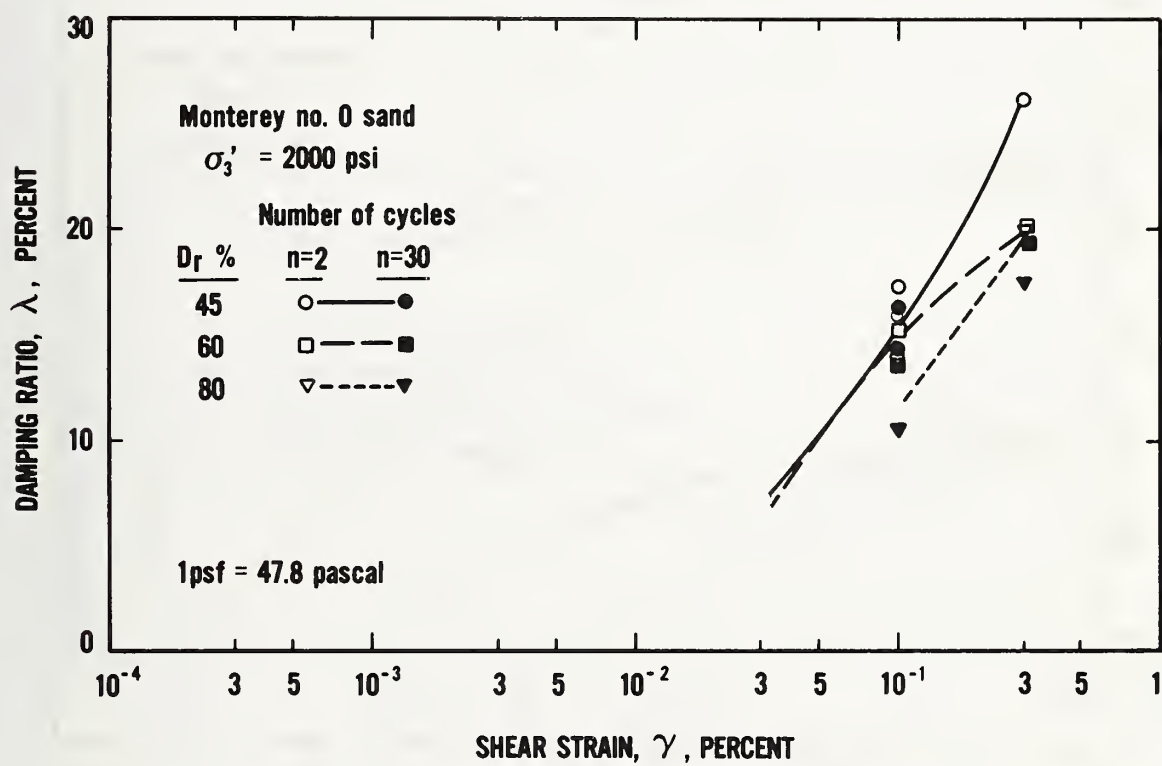


Figure 5.7 Damping ratio as a function of cyclic shear strain for Monterey No. 0 sand at $\sigma'_3 = 2000$ psf and $D_r = 45, 60,$ and 80 percent

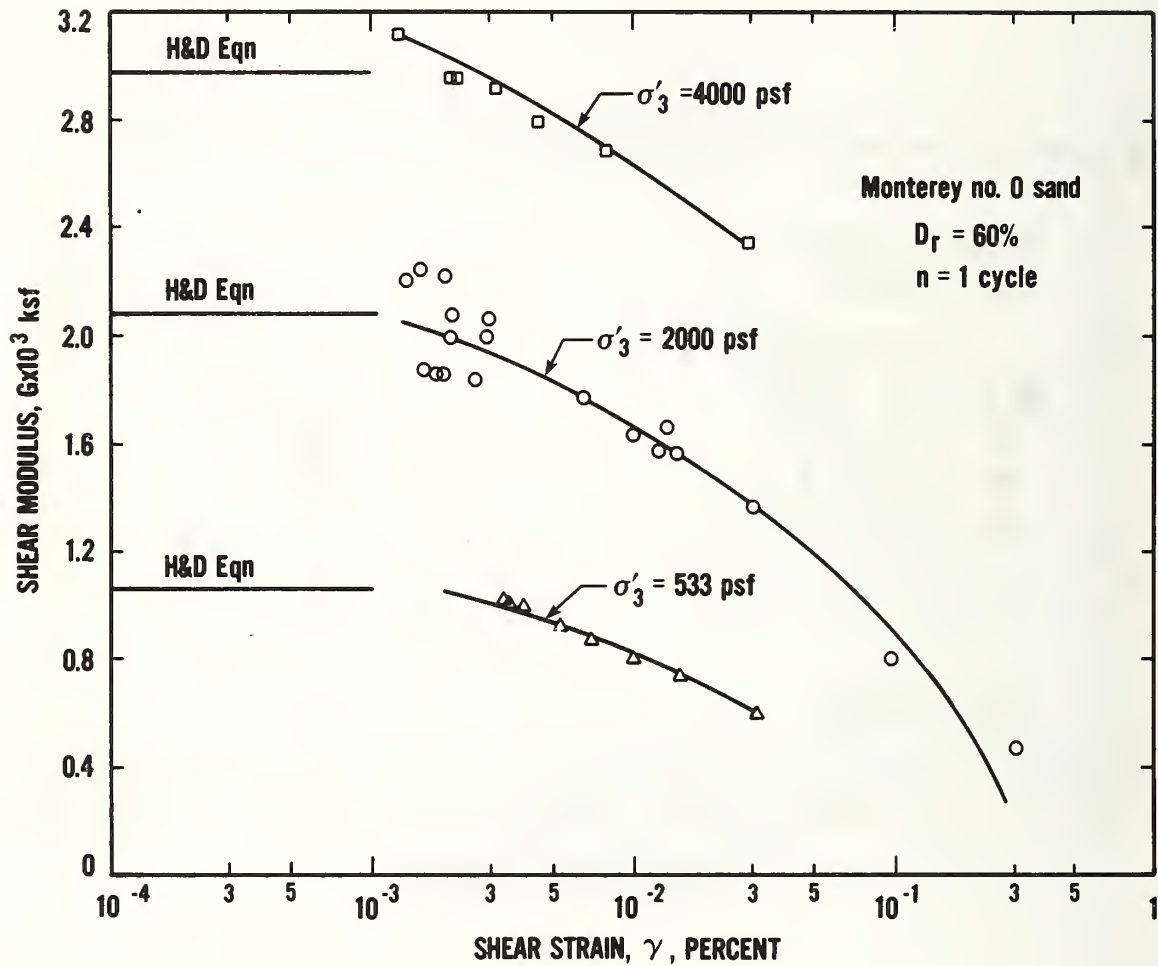


Figure 5.8 Reduction of shear modulus as a function of cyclic shear strain for Monterey No. 0 sand at $D_r = 60$ percent and $\sigma'_3 = 533, 2000$, and 4000 psf

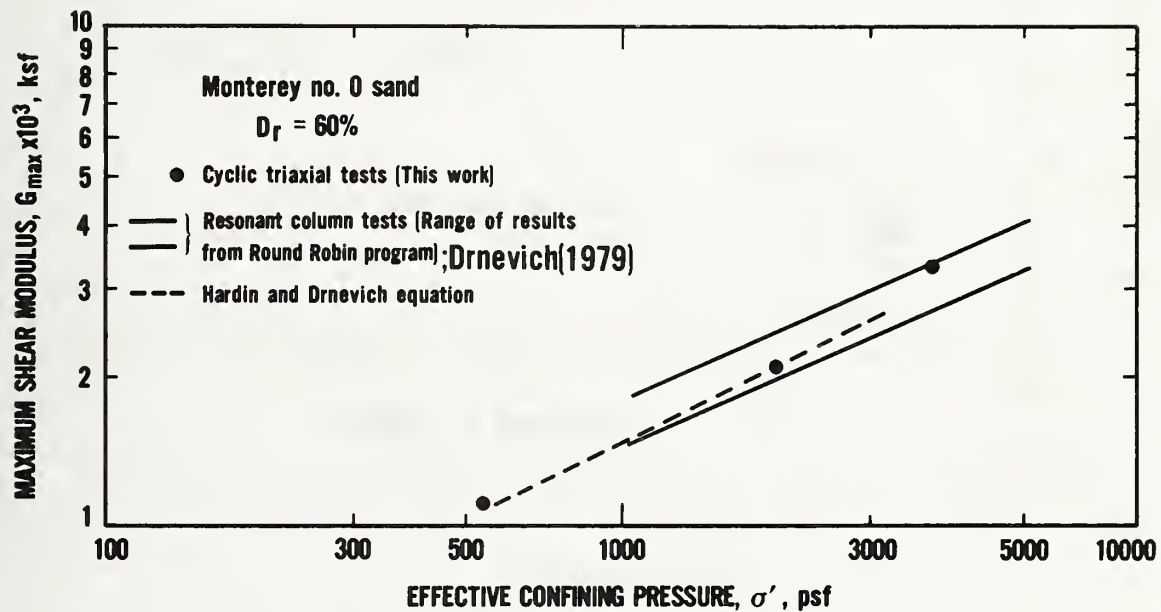
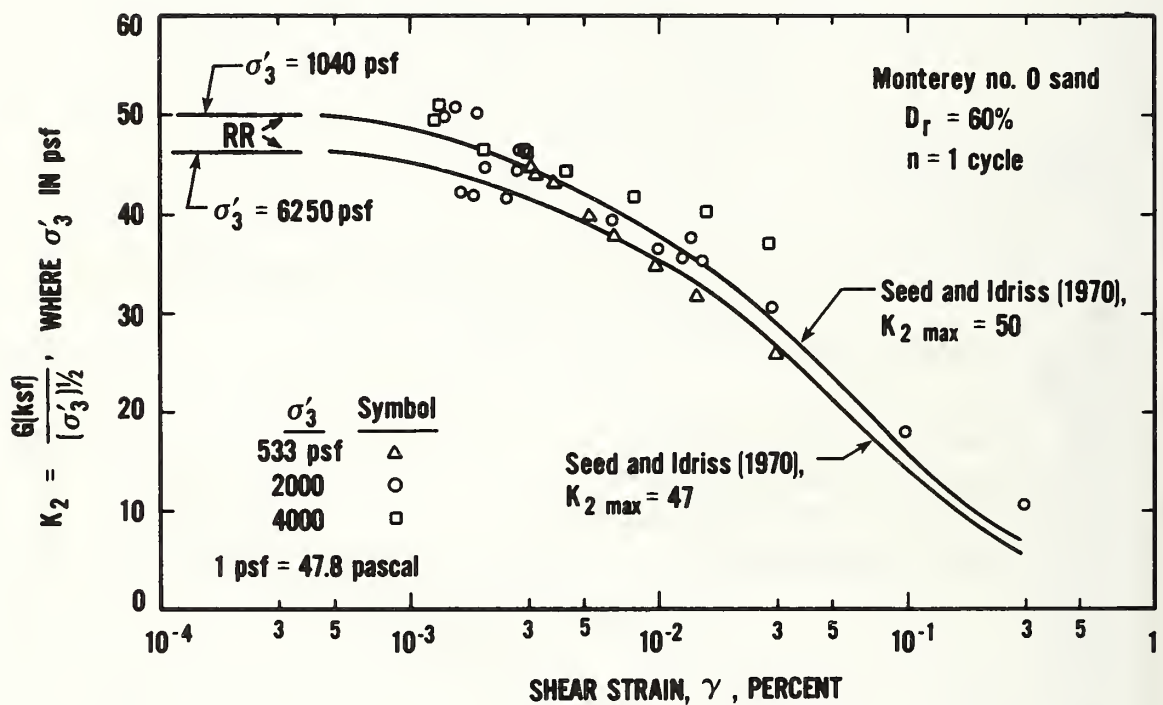


Figure 5.9 Shear modulus of very small shear strains (G_{max}) as a function of effective confining pressure (σ'_3) for Monterey No. 0 sand and $D_r = 60$ percent



RR ROUND ROBIN RESONANT COLUMN TESTING PROGRAM
 (Drnevich, 1979 [22])

Figure 5.10 Normalized stiffness parameter as a function of cyclic shear strain for Monterey No. 0 sand at $D_r = 60$ percent, $\sigma'_3 = 2000$ psf and various effective confining pressures

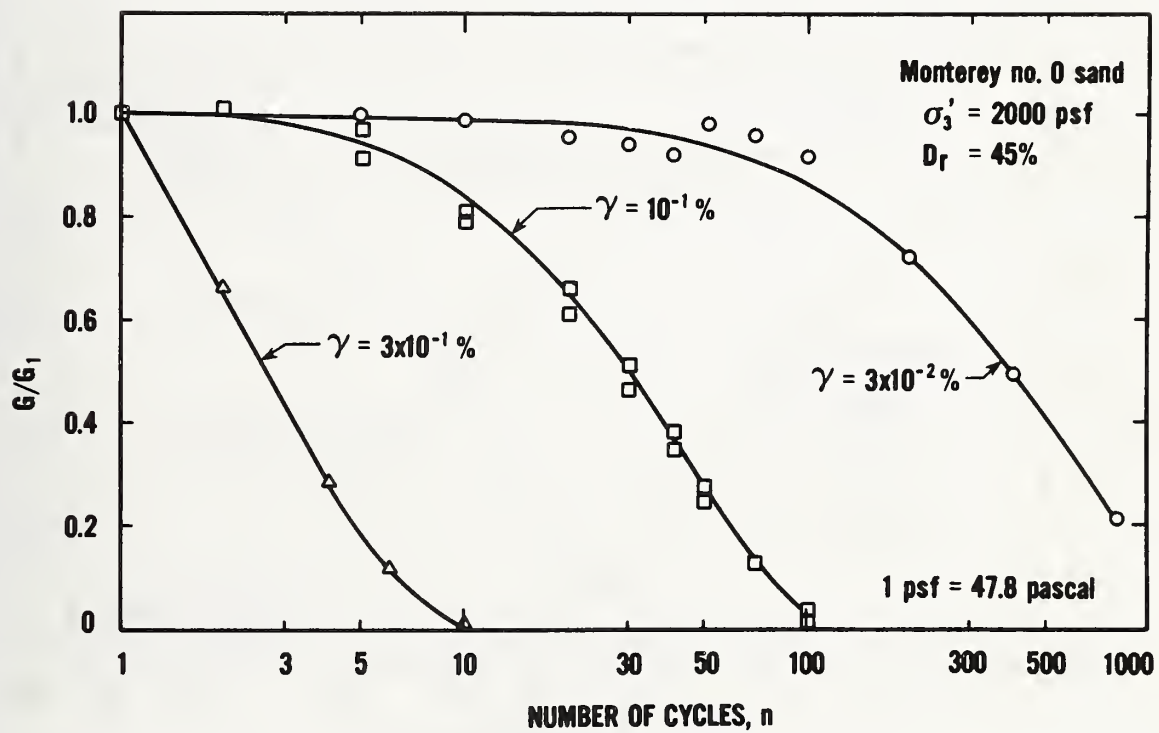


Figure 5.11 Degradation of shear modulus as a function of number of cycles for Monterey No. 0 sand at $D_r = 45$ percent, $\sigma'_3 = 2000$ psf and various cyclic shear strains

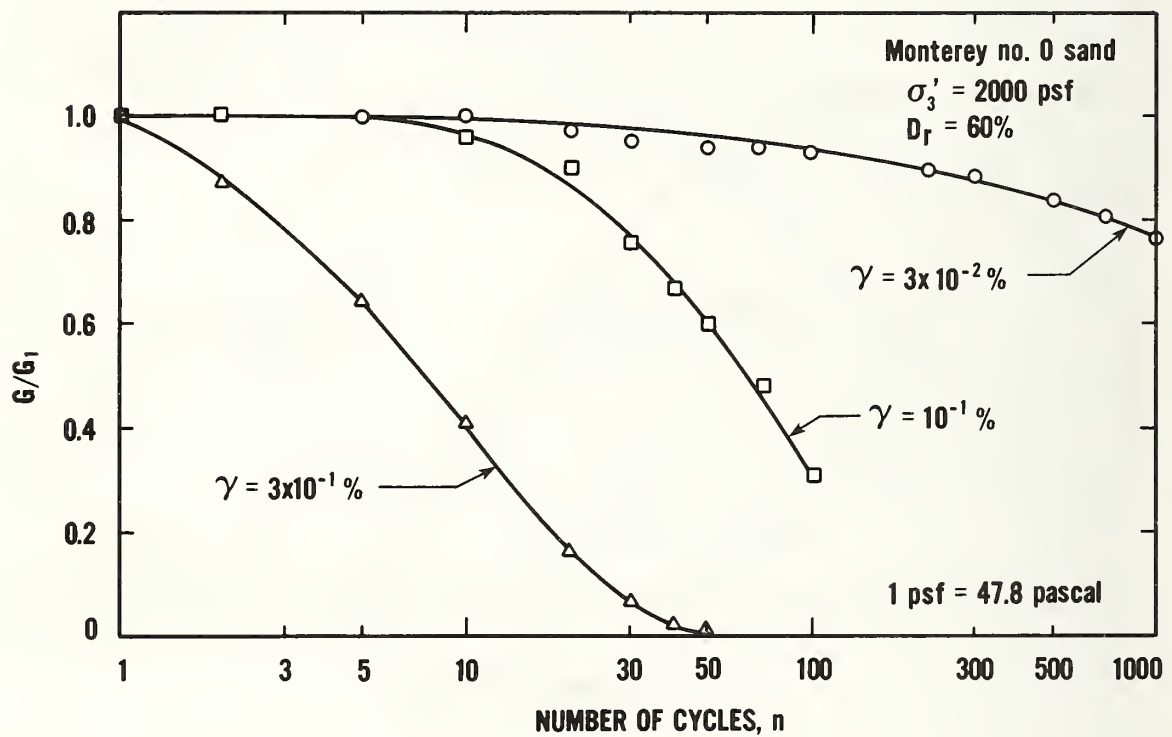


Figure 5.12 Degradation of shear modulus as a function of number of cycles for Monterey No. 0 sand at $D_r = 60$ percent, $\sigma'_3 = 2000$ psf and various cyclic shear strains

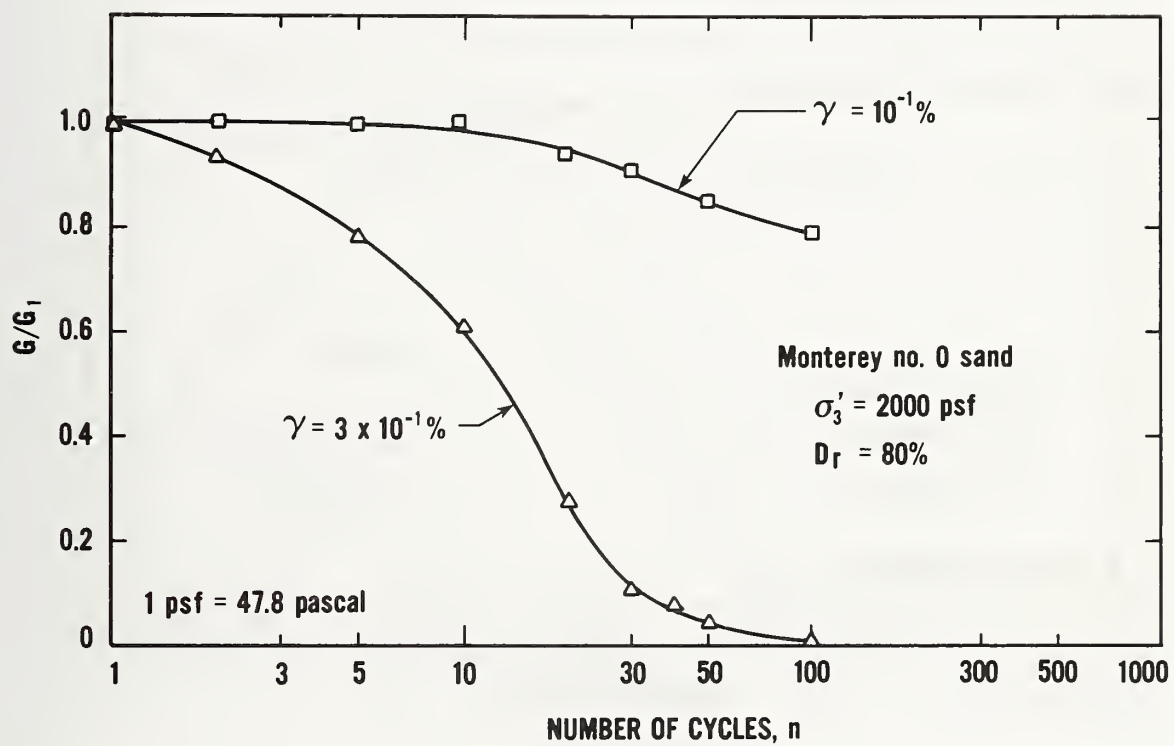


Figure 5.13 Degradation of shear modulus as a function of number of cycles for Monterey No. 0 sand at $D_r = 80$ percent, $\sigma'_3 = 2000$ psf and various cyclic shear strains

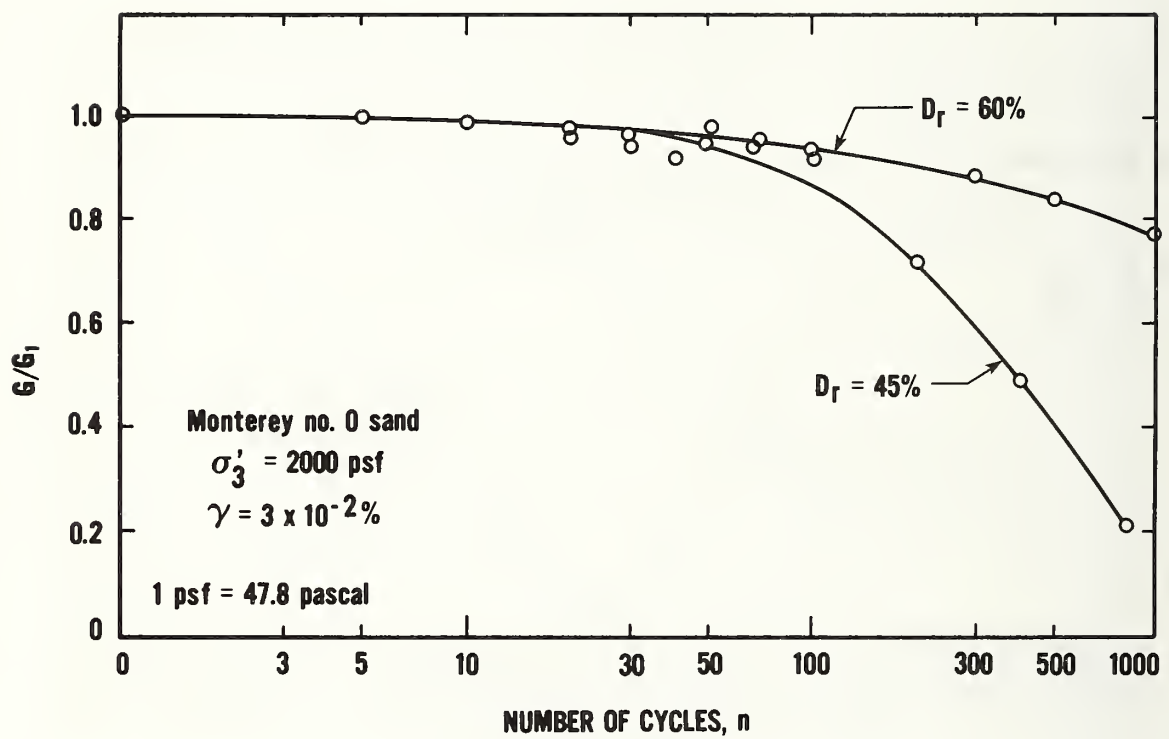


Figure 5.14 Degradation of shear modulus as a function of number of cycles for Monterey No. 0 sand at $\sigma'_3 = 2000 \text{ psf}$, $\gamma = 3 \times 10^{-2} \%$ percent and $D_r = 45$ and 60 percent

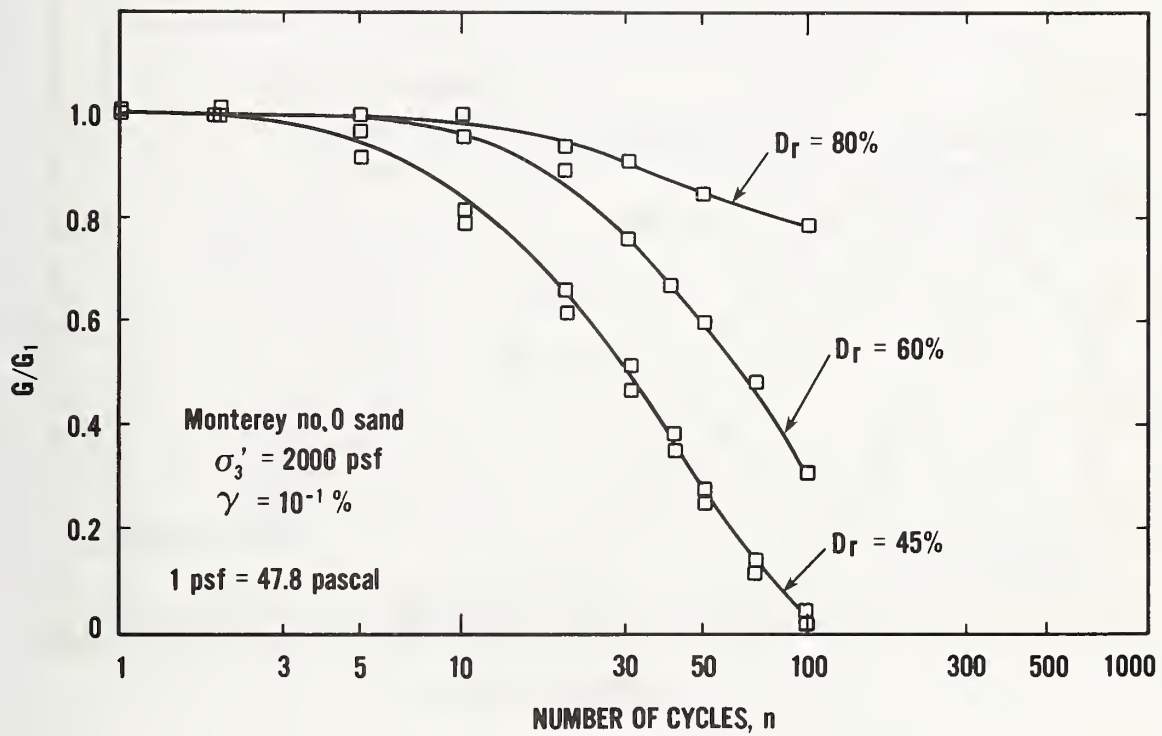


Figure 5.15 Degradation of shear modulus as a function of number of cycles for Monterey No. 0 sand at $\sigma'_3 = 2000$ psf, $\gamma = 1 \times 10^{-1}$ percent and $D_r = 45, 60, \text{ and } 80$ percent

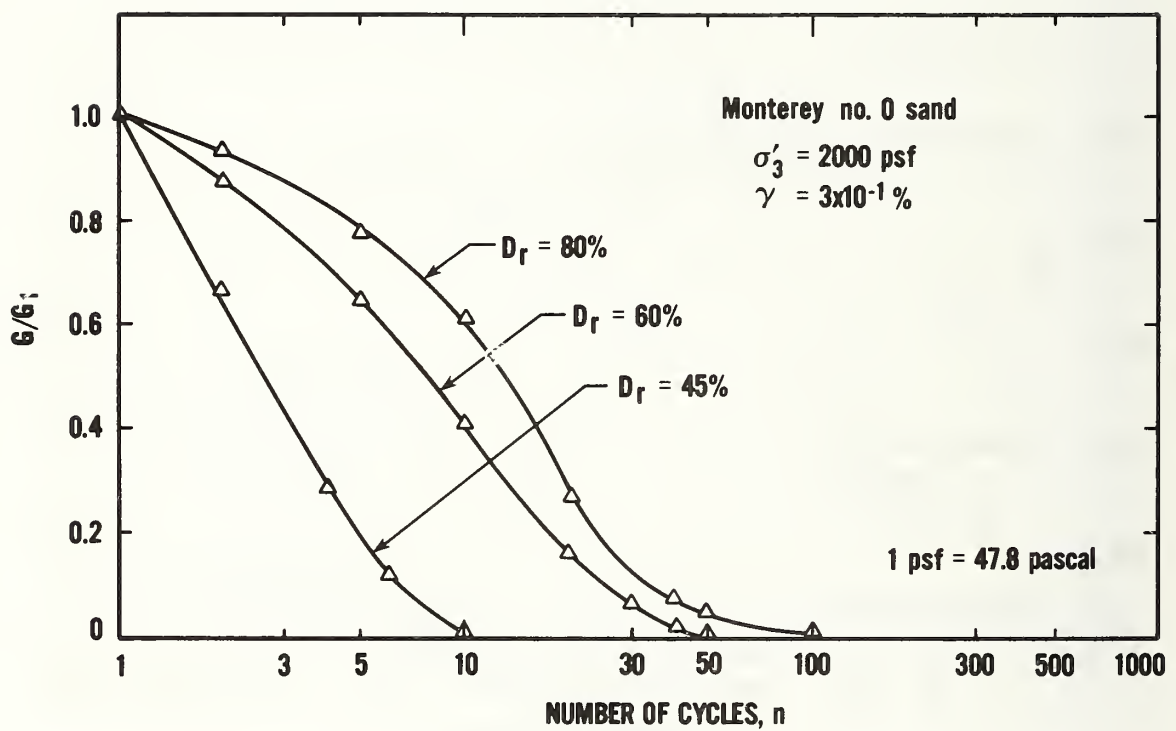


Figure 5.16 Degradation of shear modulus as a function of number of cycles for Monterey No. 0 sand at $\sigma'_3 = 2000$ psf, $\gamma = 3 \times 10^{-1}$ percent and $D_r = 45, 60, \text{ and } 80$ percent

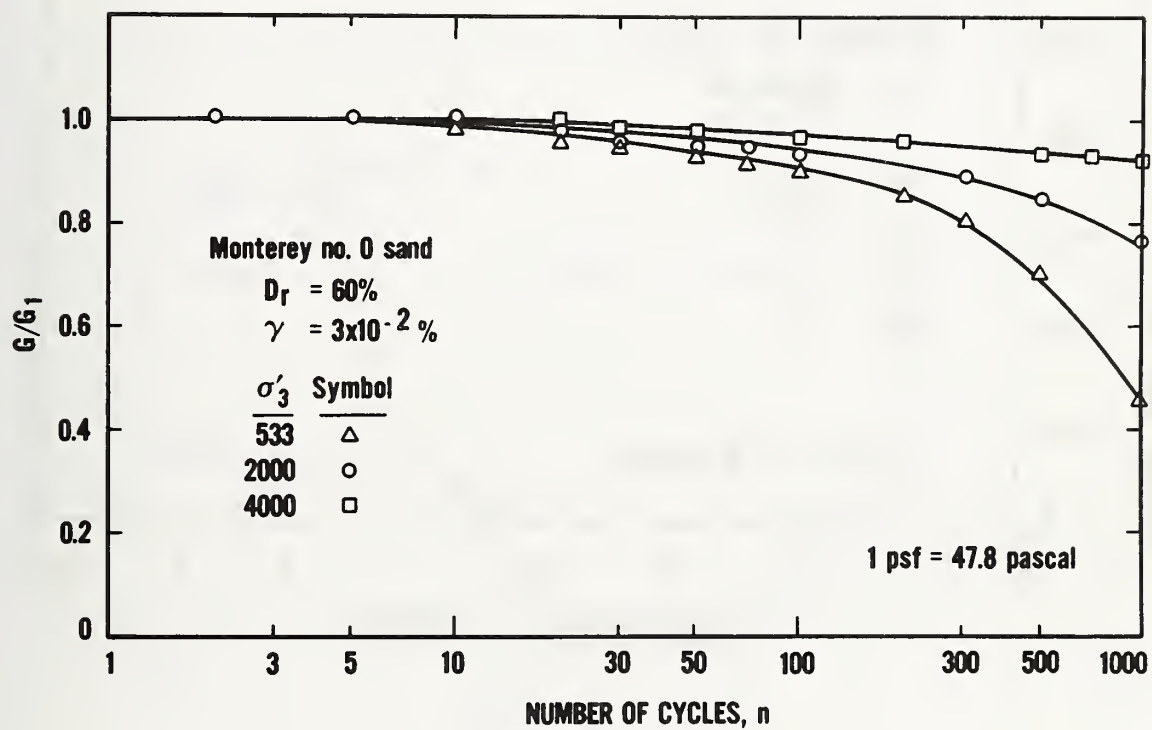


Figure 5.17 Degradation of shear modulus as a function of number of cycles for Monterey No. 0 sand at $D_r = 60$ percent, $\gamma = 3 \times 10^{-2}$ percent, and $\sigma'_3 = 533, 2000, \text{ and } 4000$ psf

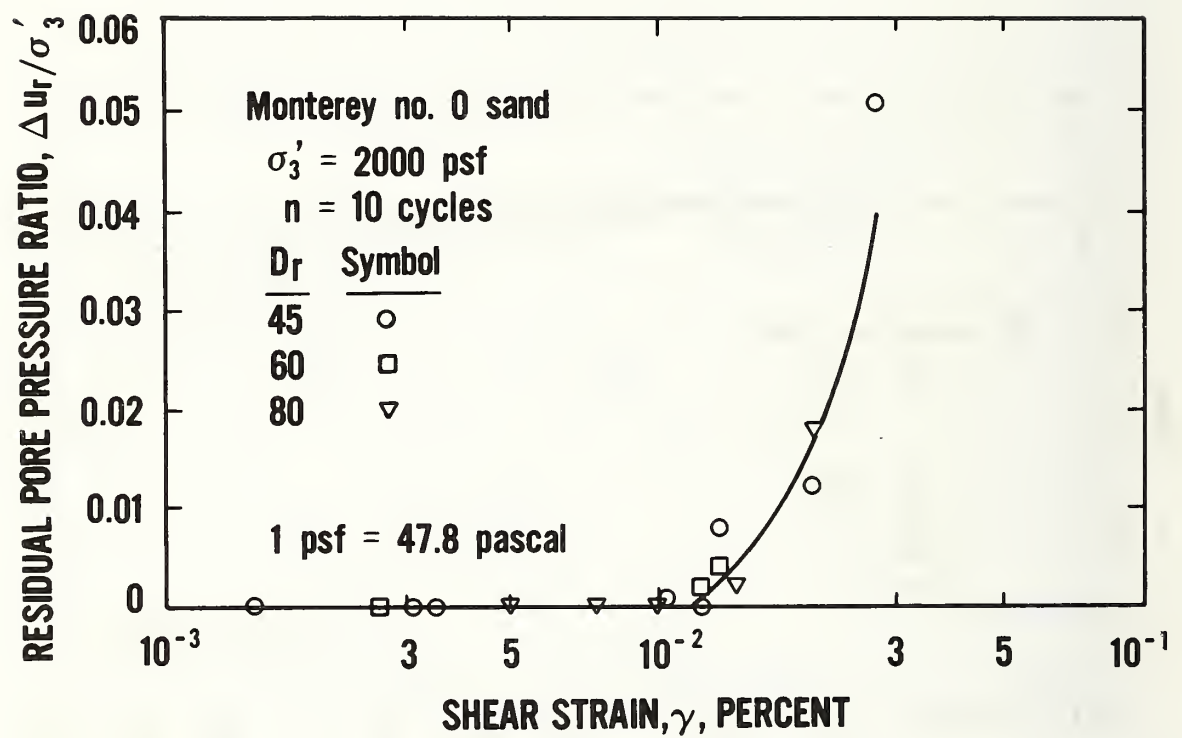


Figure 5.18 Residual pore water pressure buildup after ten loading cycles, as a function of cyclic shear strain for Monterey No. 0 sand at $\sigma'_3 = 2000$ psf and $D_r = 45, 60,$ and 80 percent

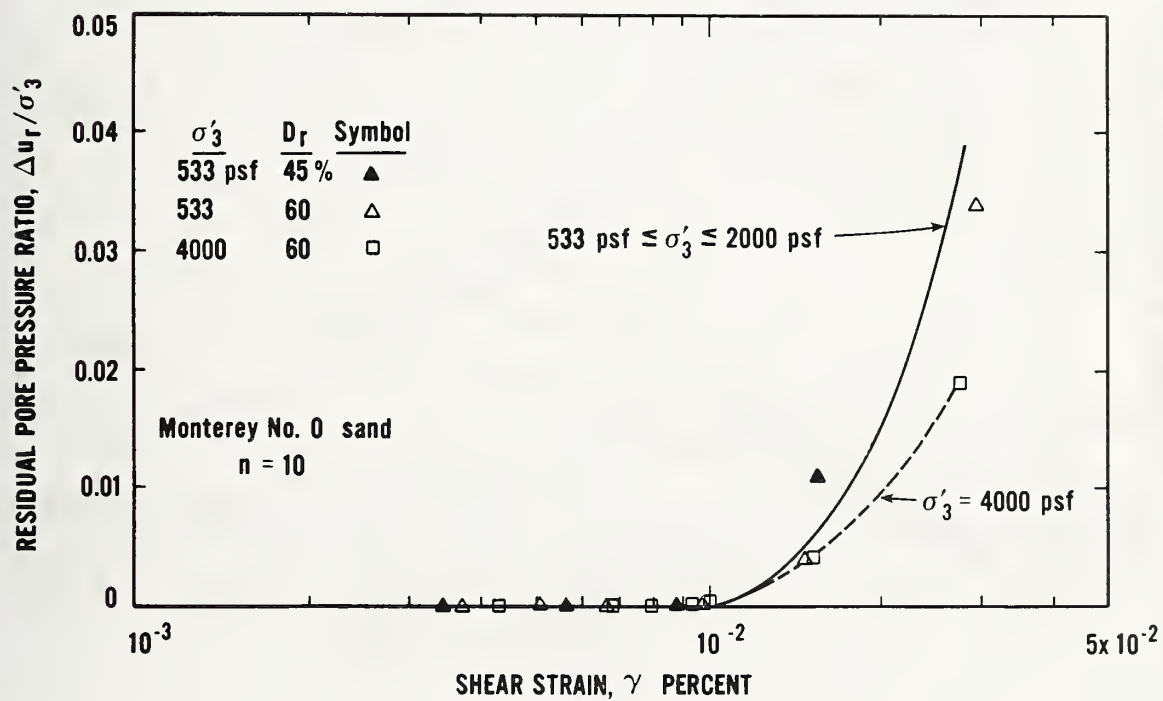


Figure 5.19 Residual pore water pressure buildup after ten loading cycles, as a function of cyclic shear strain for Monterey No. 0 sand at $\sigma'_3 = 533, 2000, \text{ and } 4000$ psf and $D_r = 45, 60, \text{ and } 80$ percent

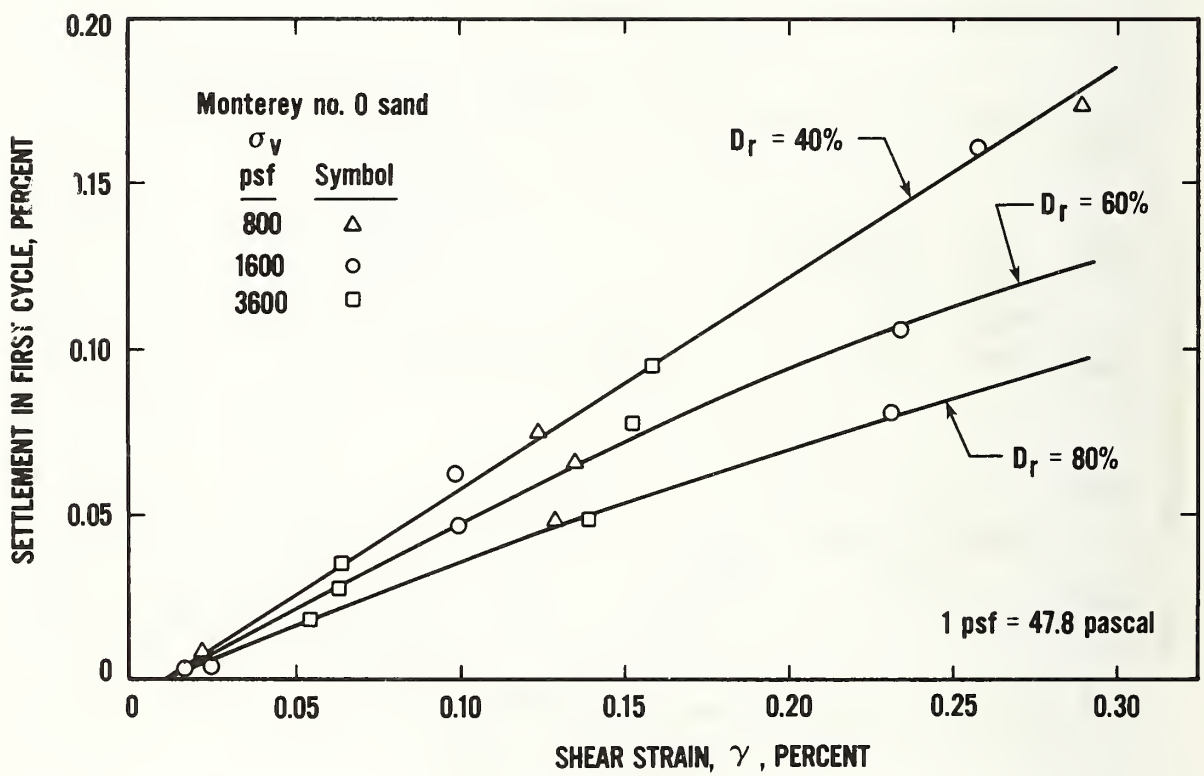


Figure 5.20 Settlement in the first loading cycle as a function of cyclic shear strain for dry Monterey No. 0 sand at various relative densities and confining pressures, simple shear tests (Pyke, 1973)

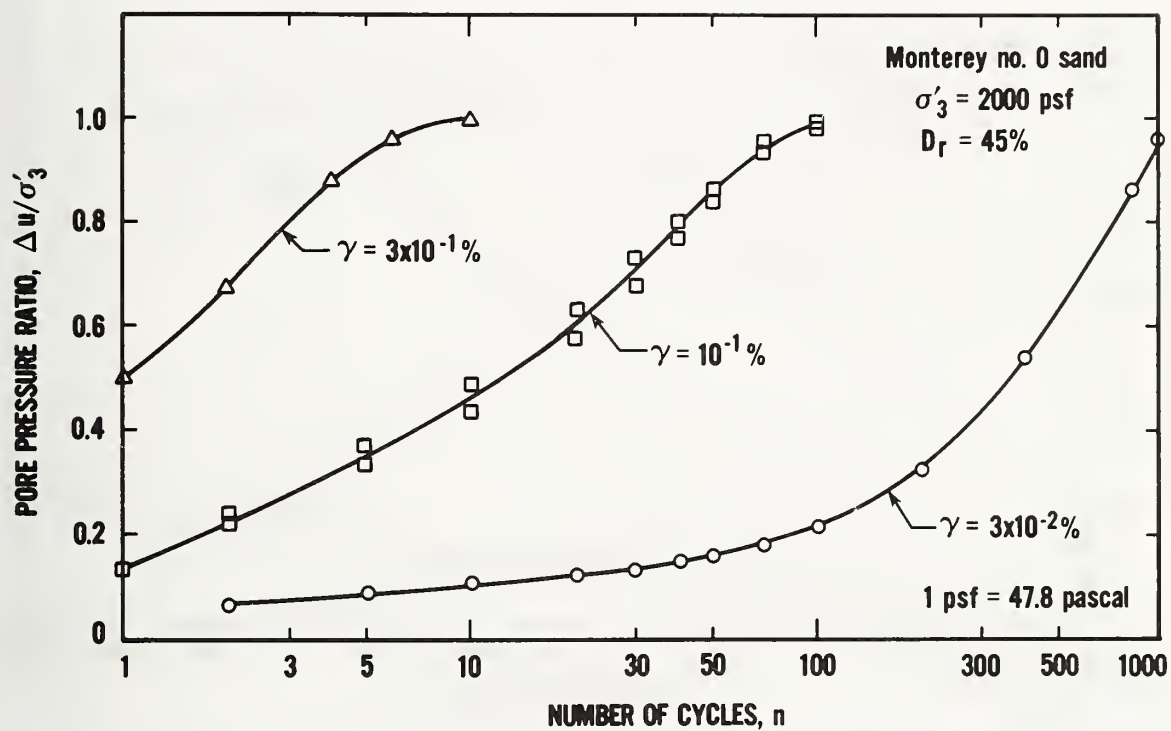


Figure 5.21 Pore water pressure buildup as a function of number of cycles for Monterey No. 0 sand at $\sigma'_3 = 2000$ psf, $D_r = 45$ percent and various cyclic shear strains

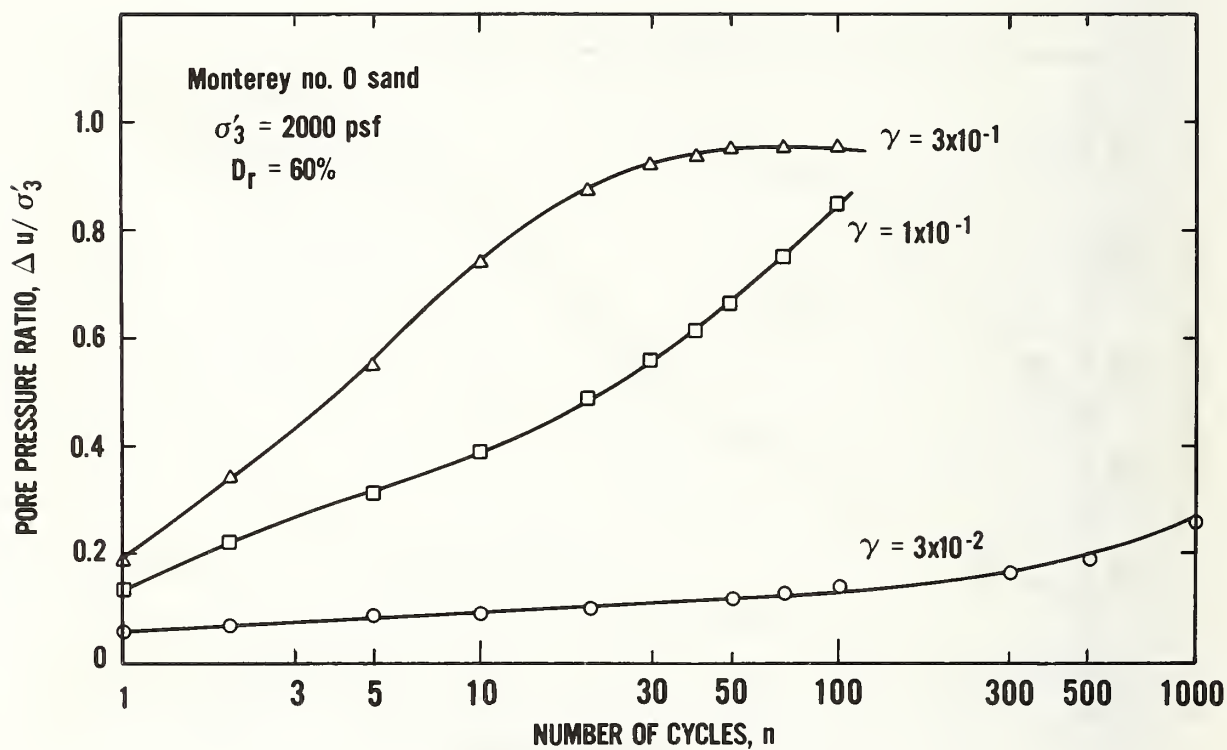


Figure 5.22 Pore water pressure buildup as a function of number of cycles for Monterey No. 0 sand at $\sigma'_3 = 2000$ psf, $D_r = 60$ percent and various cyclic shear strains

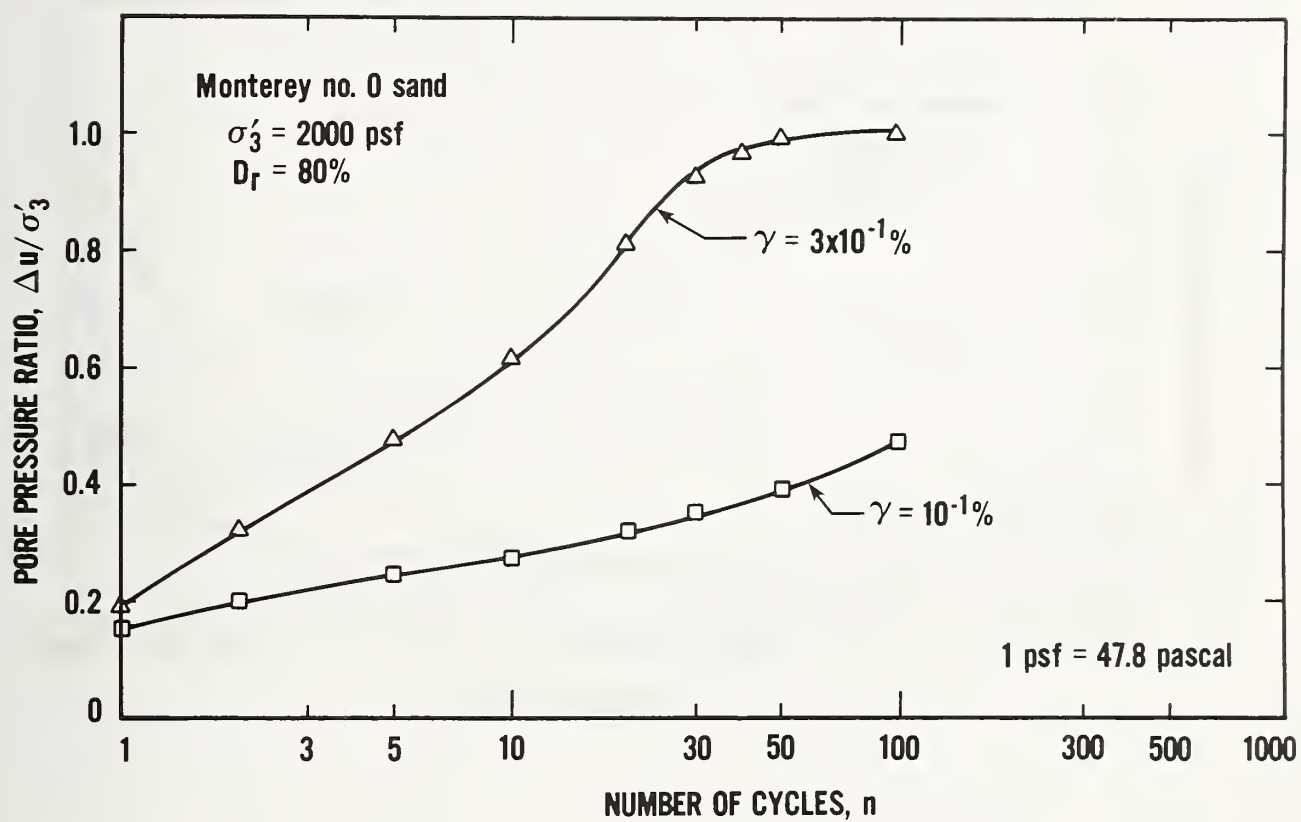


Figure 5.23 Pore water pressure buildup as a function of number of cycles for Monterey No. 0 sand at $\sigma'_3 = 2000$ psf, $D_r = 80$ percent and various cyclic shear strains

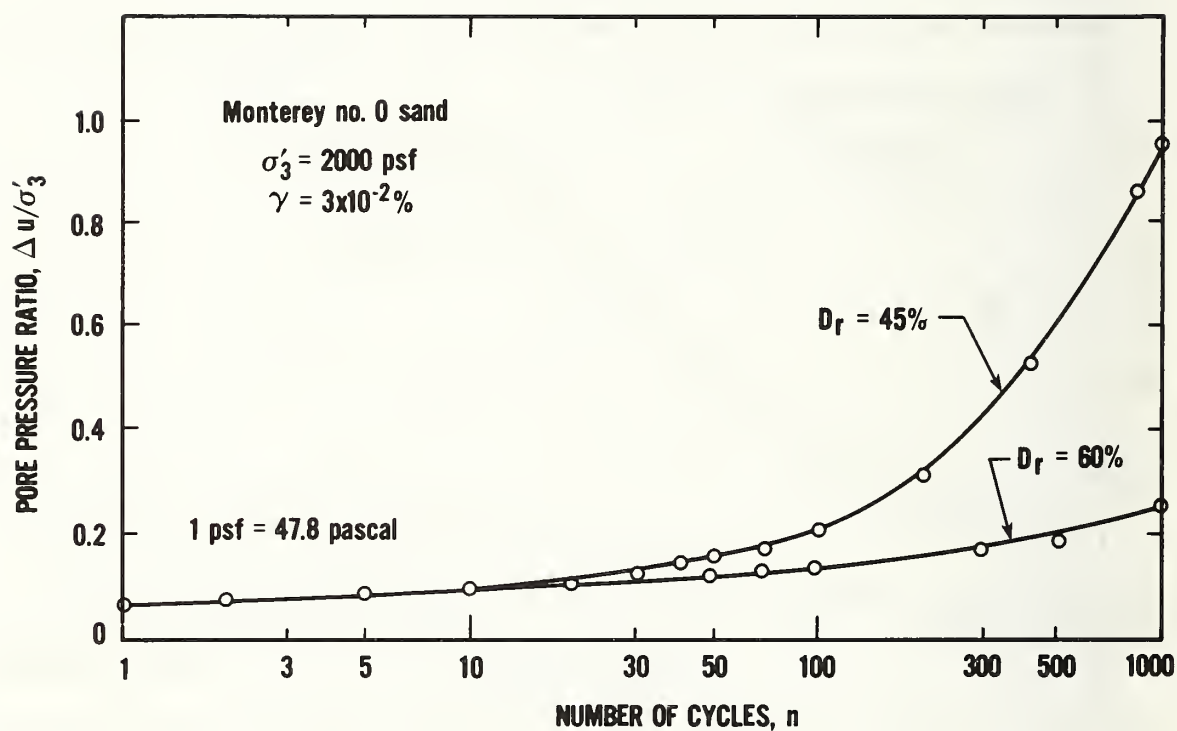


Figure 5.24 Pore water pressure buildup as a function of number of cycles for Monterey No. 0 sand at $\sigma'_3 = 2000 \text{ psf}$, $\gamma = 3 \times 10^{-2}$ percent, and $D_r = 45$ and 60 percent

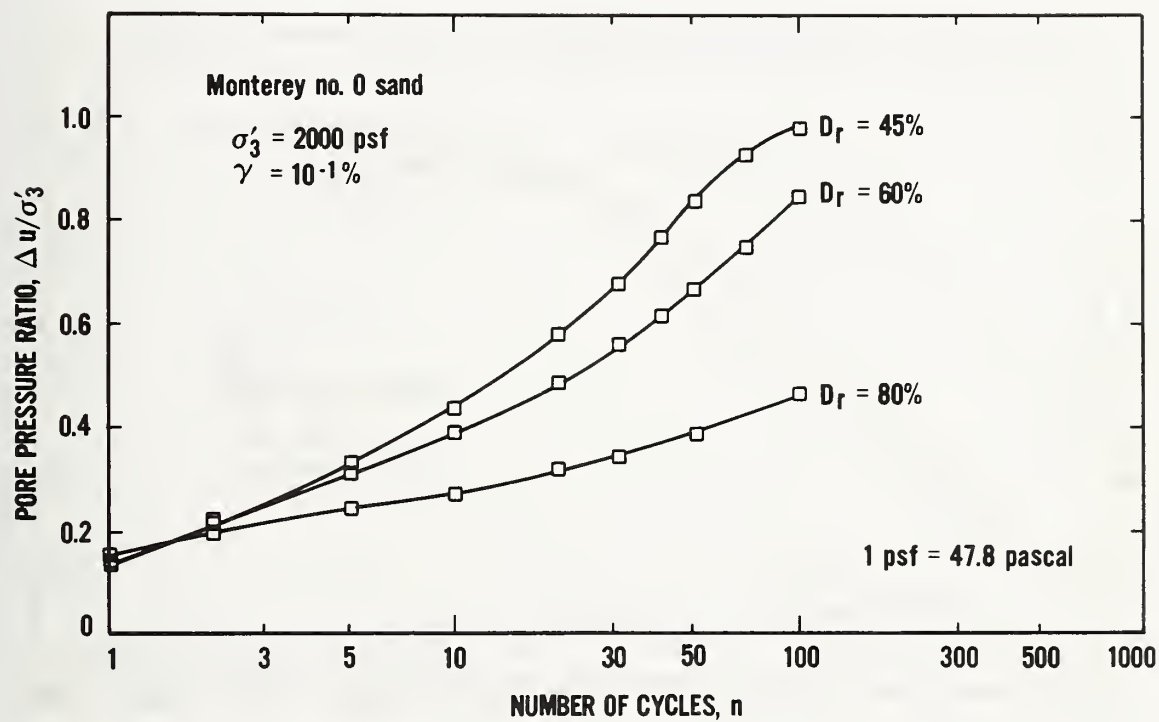


Figure 5.25 Pore water pressure buildup as a function of number of cycles for Monterey No. 0 sand at $\sigma'_3 = 2000 \text{ psf}$, $\gamma = 1 \times 10^{-1}$ percent, and $D_r = 45, 60, \text{ and } 80$ percent

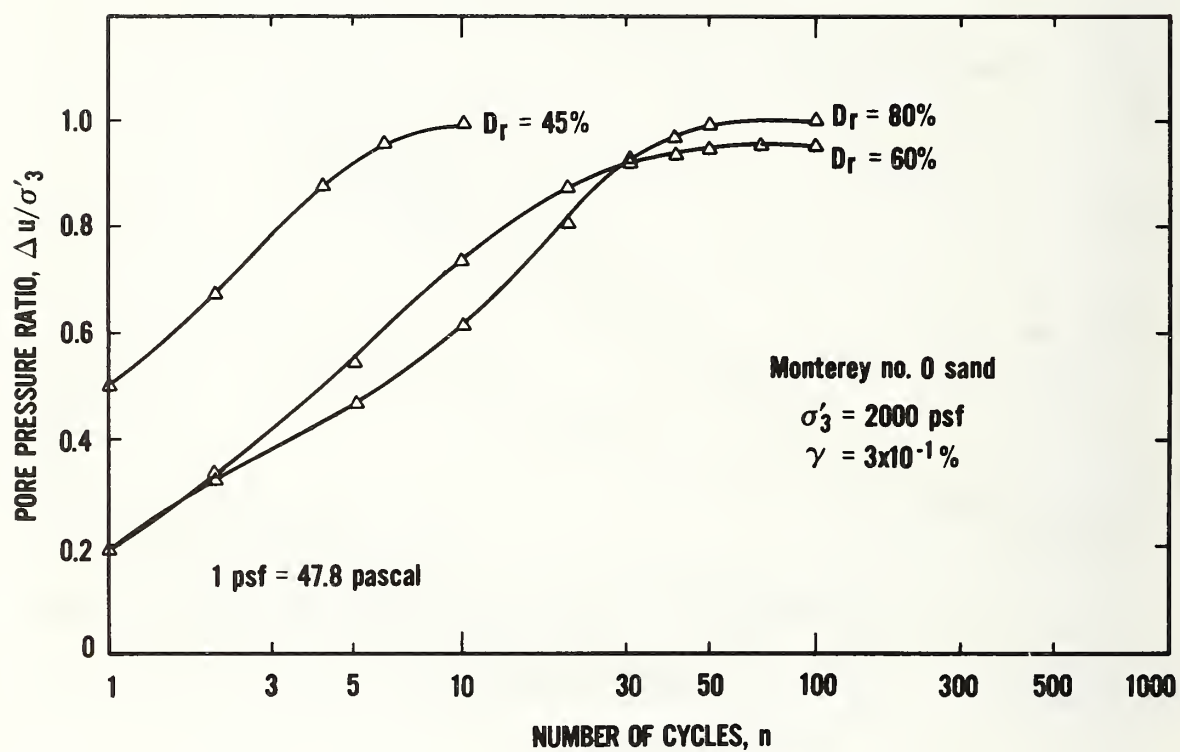


Figure 5.26 Pore water pressure buildup as a function of number of cycles for Monterey No. 0 sand at $\sigma'_3 = 2000 \text{ psf}$, $\gamma = 3 \times 10^{-1}$ percent, and $D_r = 45, 60, \text{ and } 80$ percent

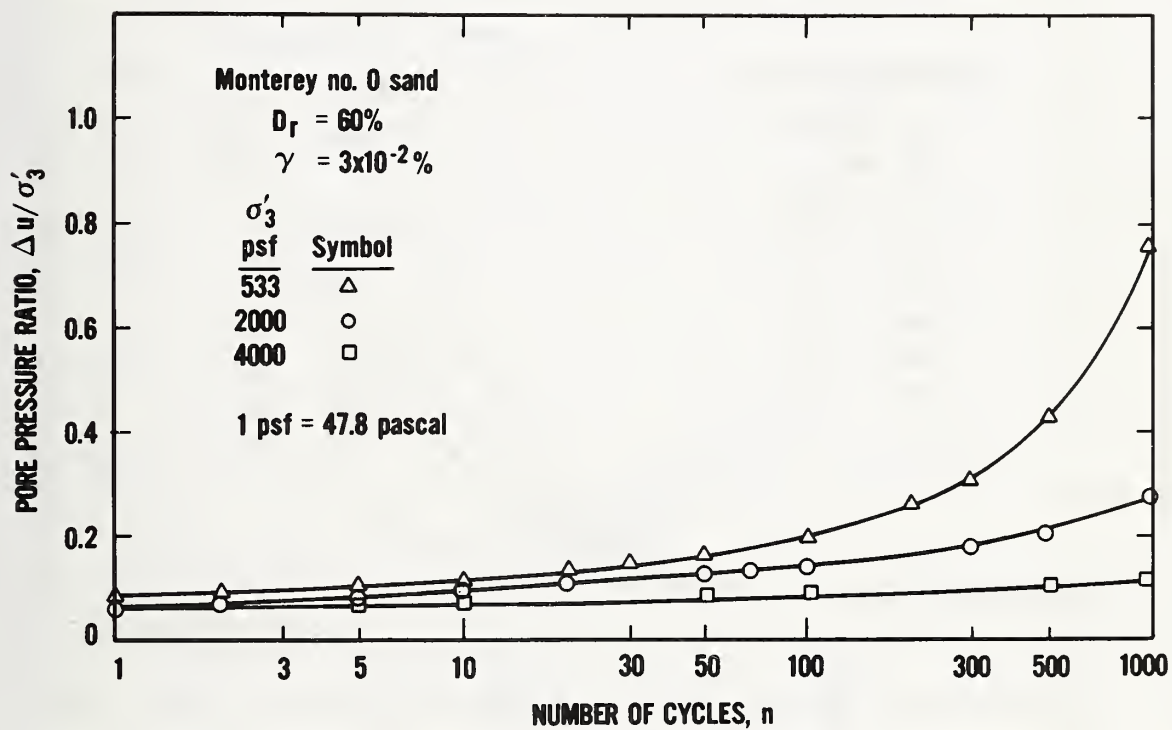


Figure 5.27 Pore water pressure buildup as a function of number of cycles for Monterey No. 0 sand at $D_r = 60$ percent, $\gamma = 3 \times 10^{-2}$ percent and various effective confining pressures

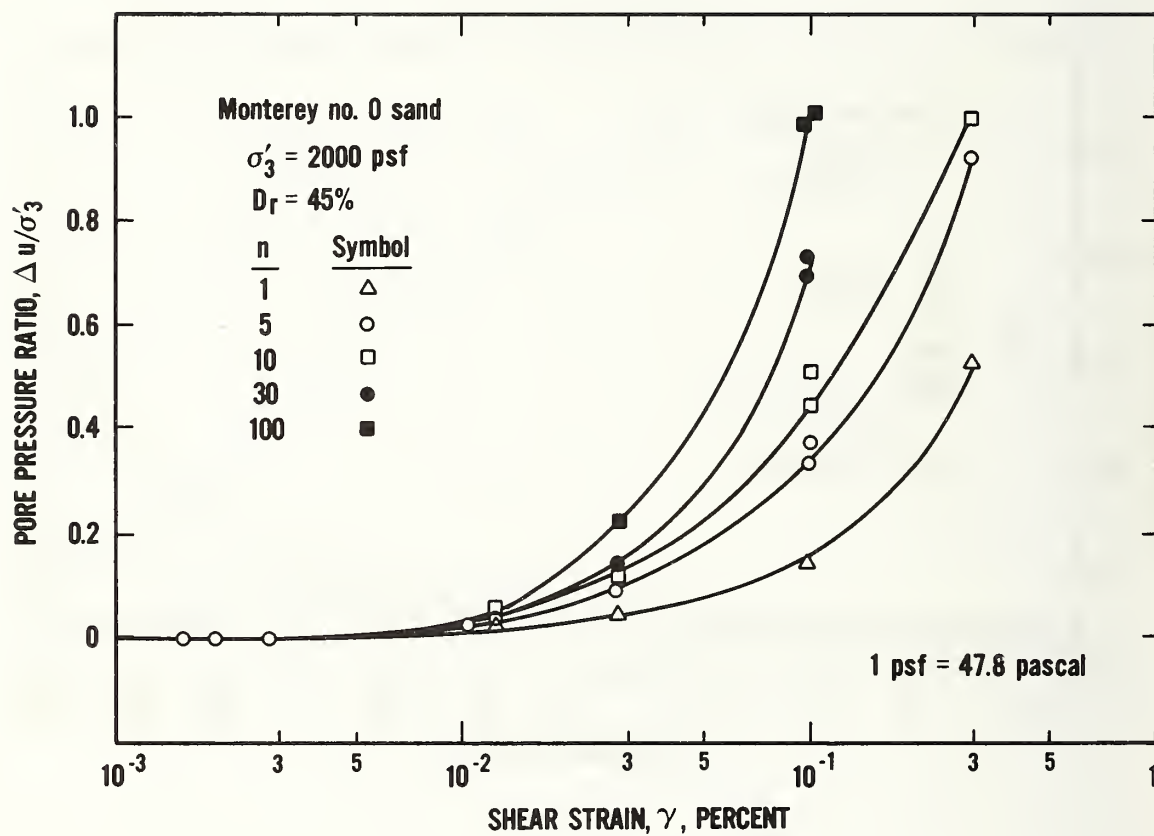


Figure 5.28 Pore water pressure buildup as a function of cyclic shear strain for Monterey No. 0 sand at $D_r = 45$ percent, $\sigma'_3 = 2000$ psf and various numbers of cycles

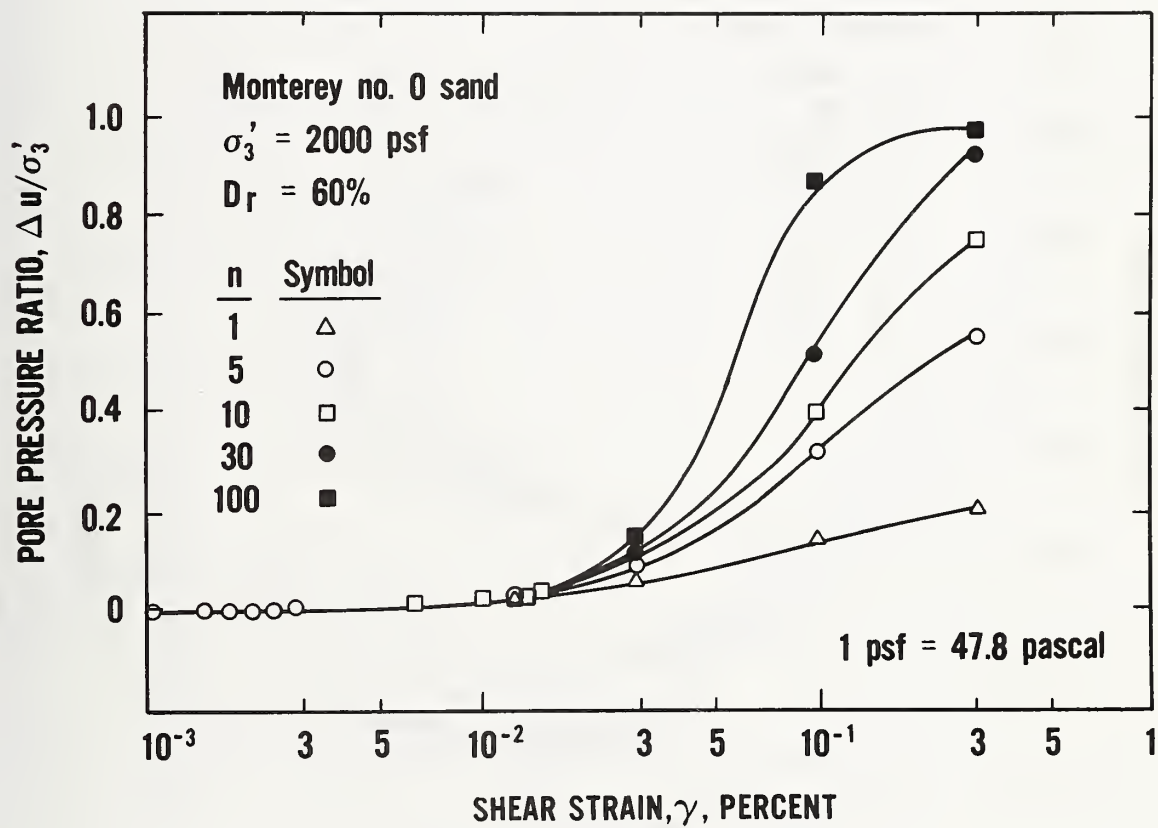


Figure 5.29 Pore water pressure buildup as a function of cyclic shear strain for Monterey No. 0 sand at $D_r = 60$ percent, $\sigma'_3 = 2000$ psf and various numbers of cycles

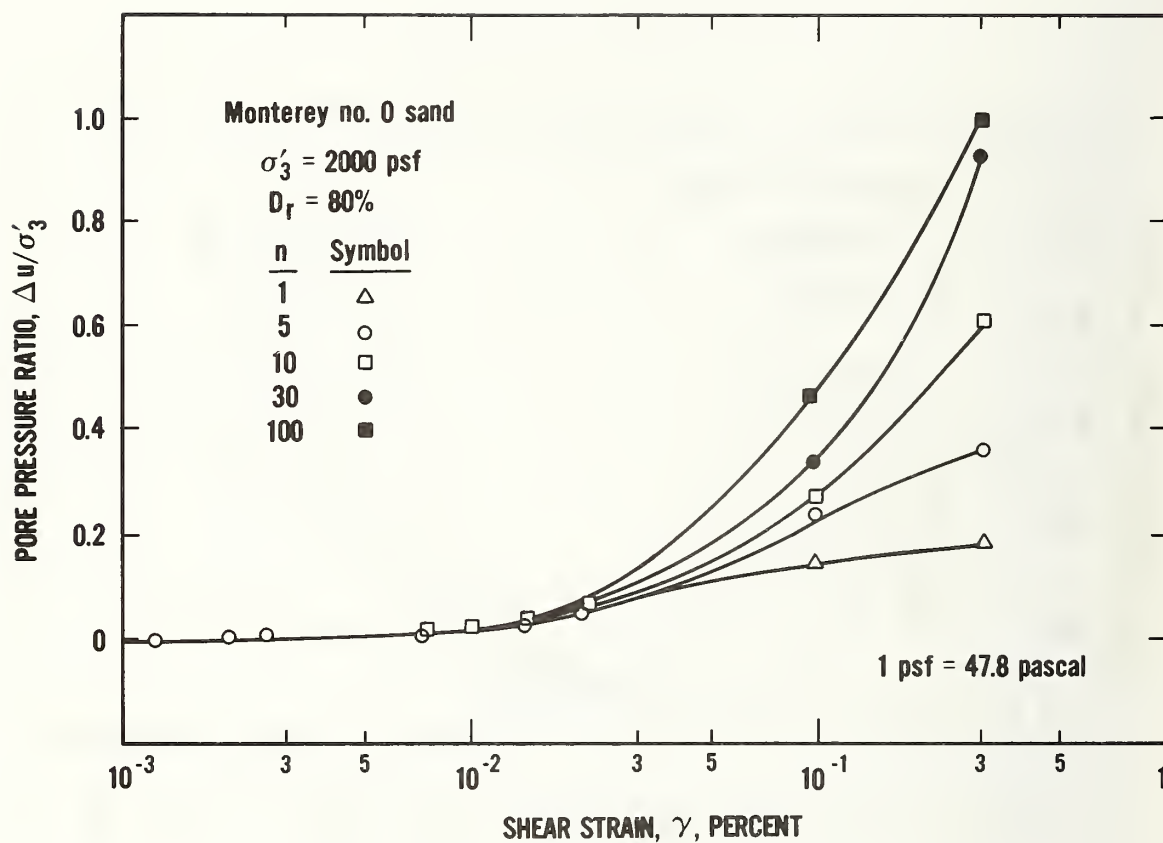


Figure 5.30 Pore water pressure buildup as a function of cyclic shear strain for Monterey No. 0 sand at $D_r = 80$ percent, $\sigma'_3 = 2000$ psf and various numbers of cycles

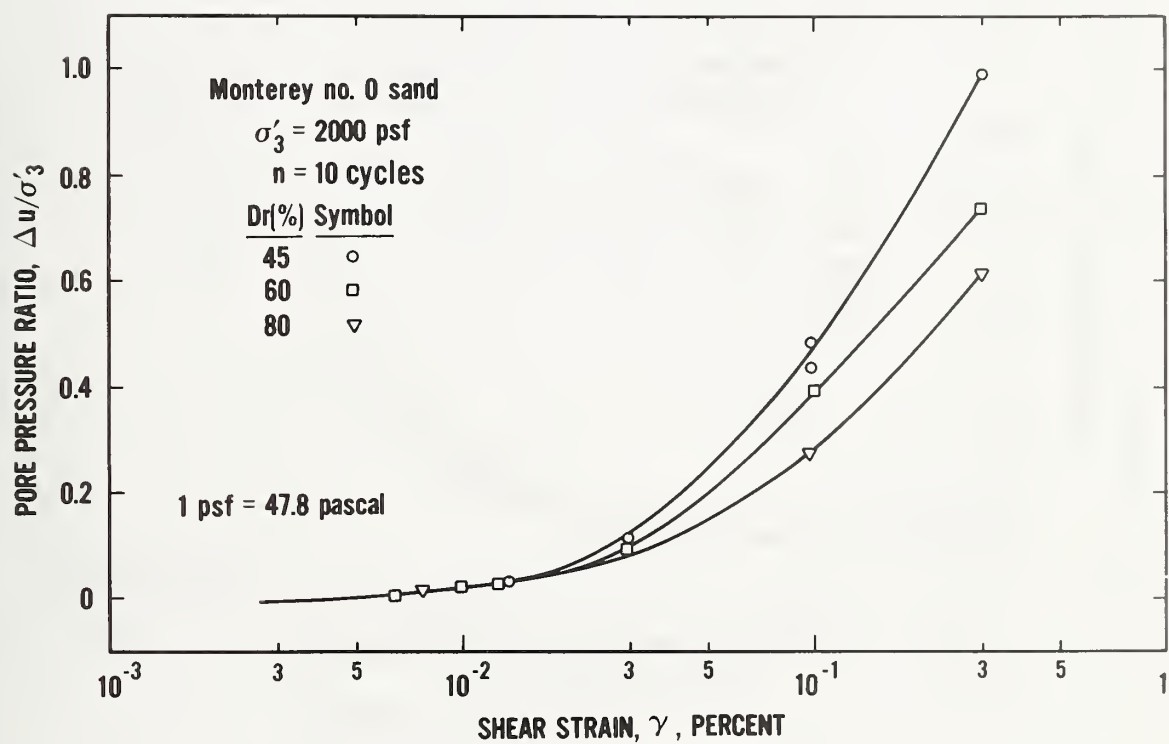


Figure 5.31 Pore water pressure buildup after ten loading cycles, as a function of cyclic shear strain for Monterey No. 0 sand at $\sigma'_3 = 2000$ psf and $D_r = 45, 60,$ and 80 percent

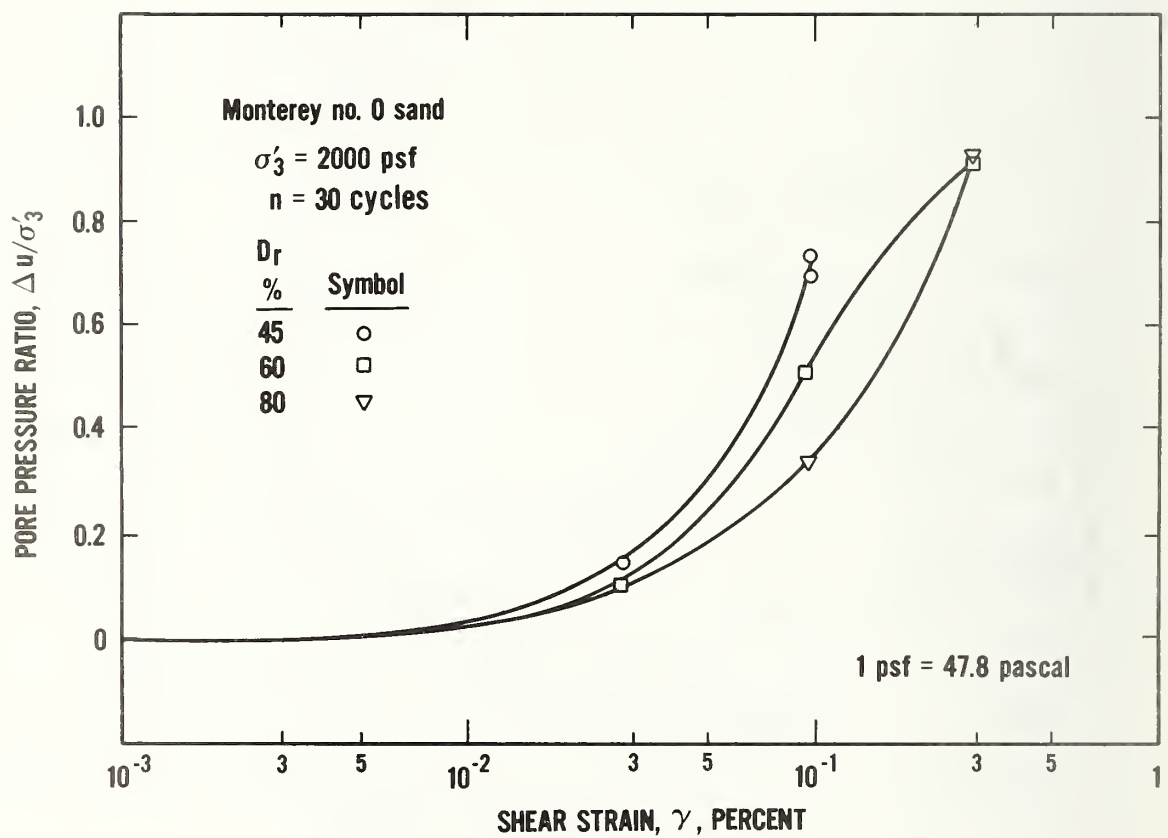


Figure 5.32 Pore water pressure buildup after thirty loading cycles, as a function of cyclic shear strain for Monterey No. 0 sand at $\sigma'_3 = 2000$ psf and $D_r = 45, 60,$ and 80 percent

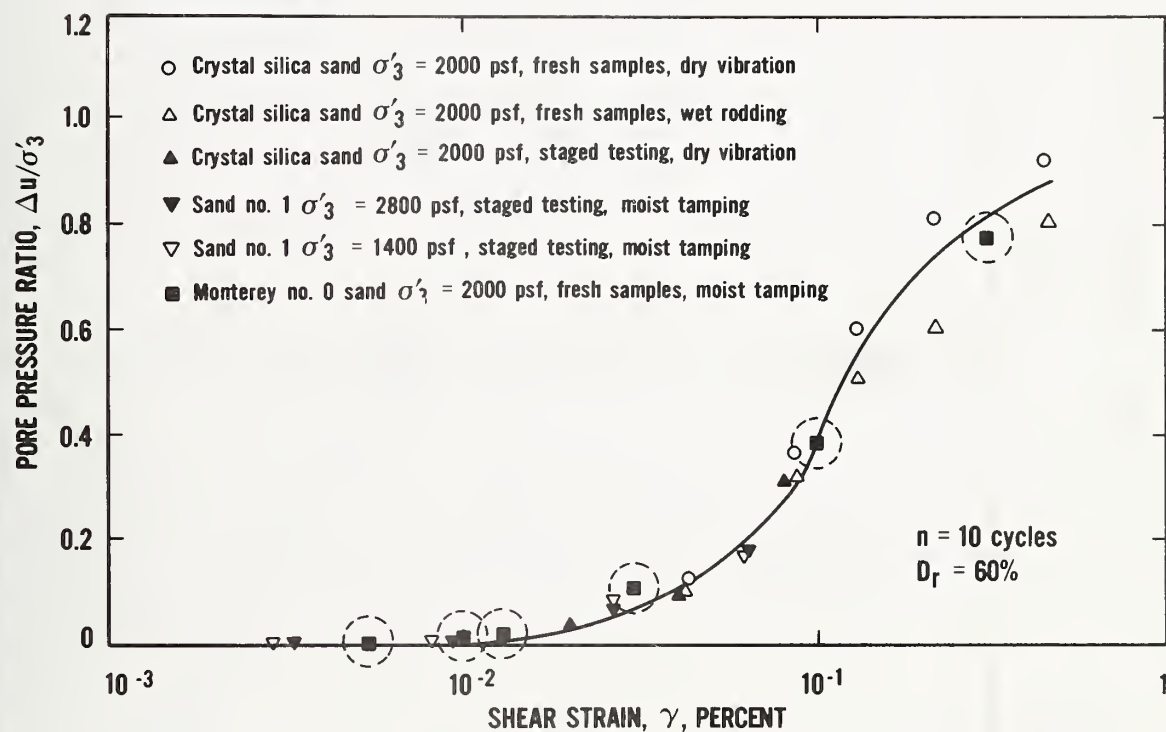


Figure 5.33 Pore water pressure buildup in cyclic triaxial strain-controlled tests after ten loading cycles, as a function of cyclic shear strain, for various NC saturated sands at $D_r = 60$ percent and for various confining pressures

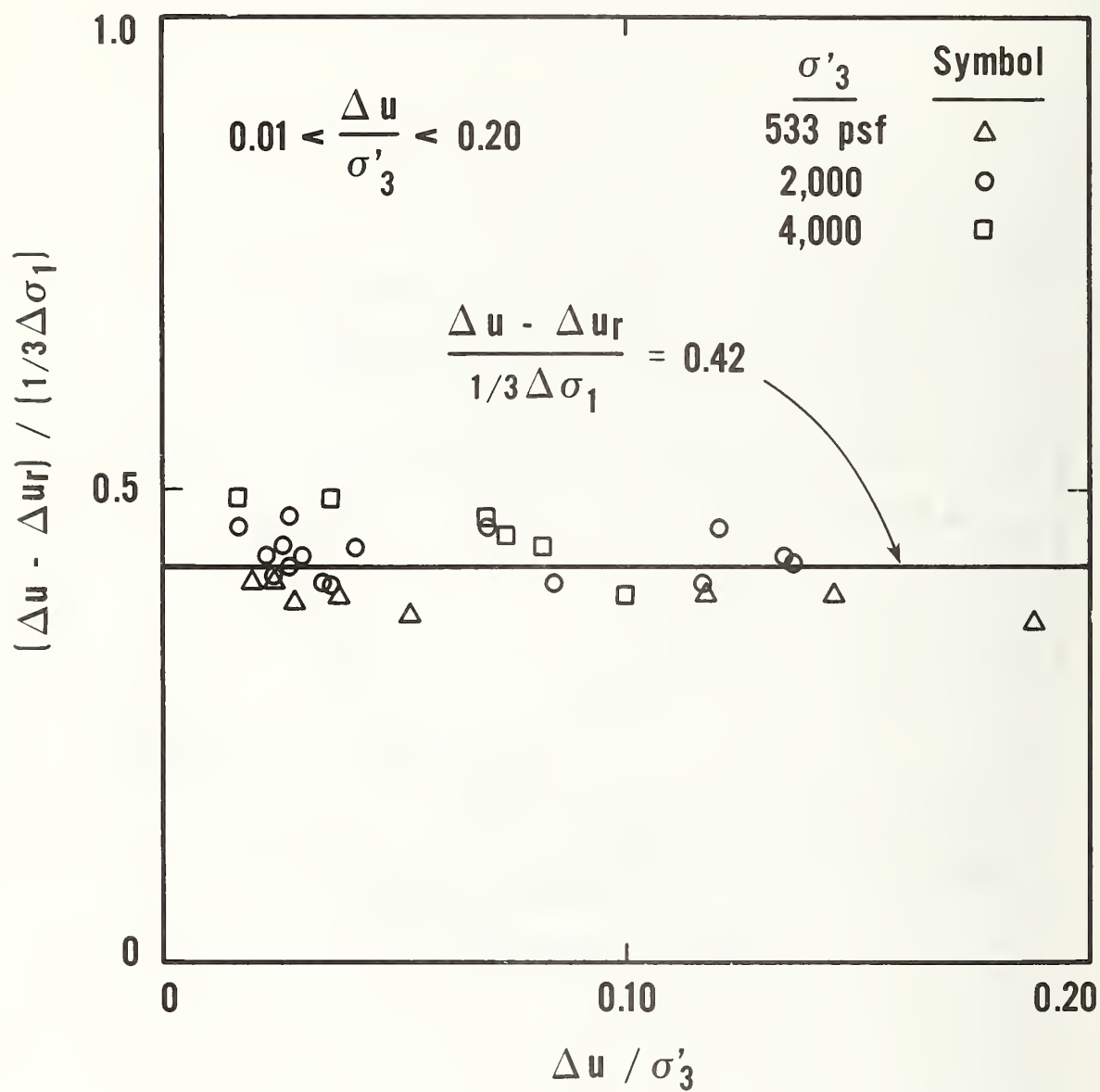


Figure 5.34 Comparison between Δu and Δu_r as a function of pore water pressure ratio for Monterey No. 0 sand at $D_r = 45, 60$ and 80 percent and $\sigma'_3 = 533, 2000, \text{ and } 4000 \text{ psf}$

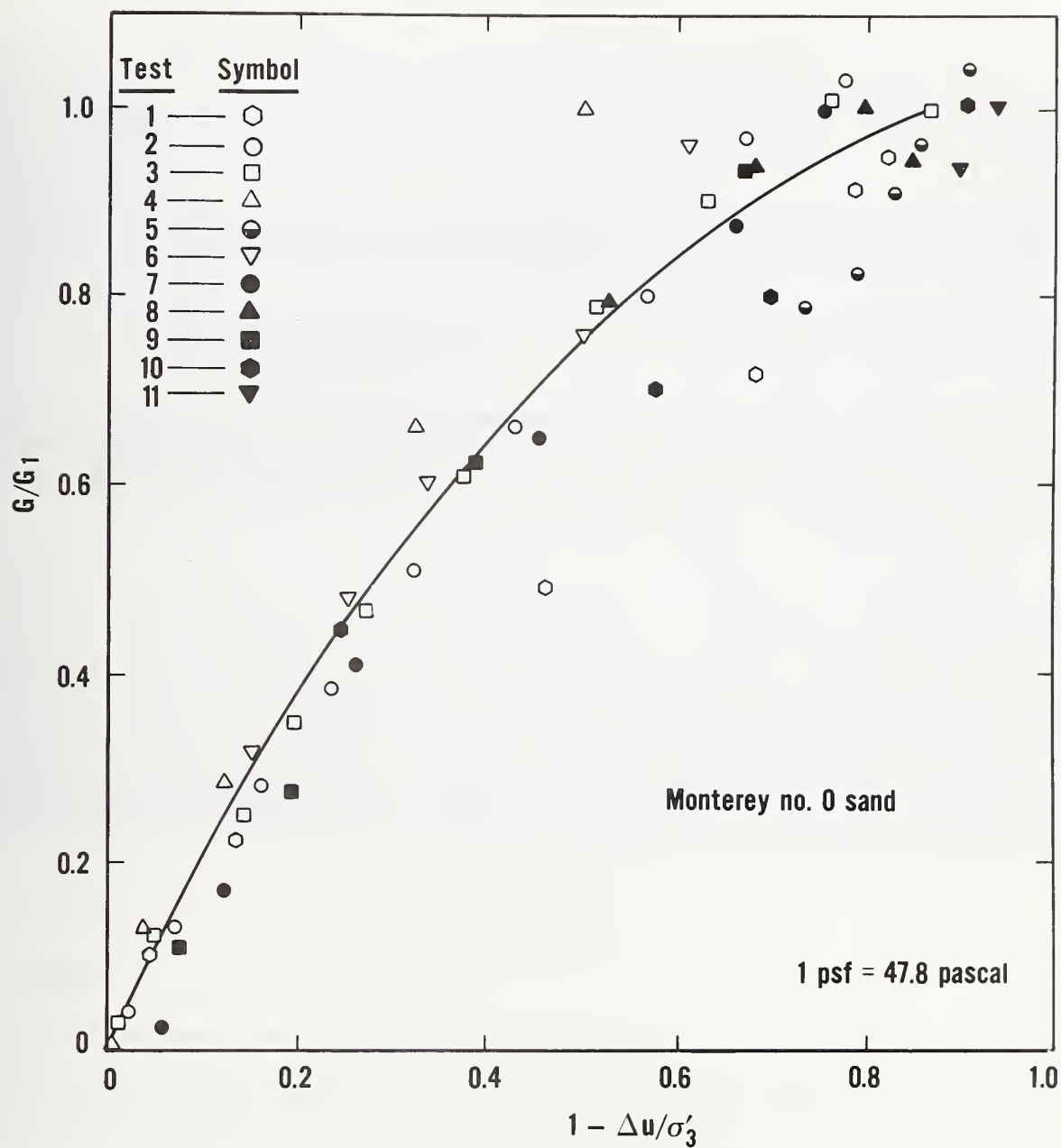


Figure 5.35 Degradation of shear modulus as a function of pore water pressure buildup for Monterey No. 0 sand at $\sigma'_3 = 2000$ psf

FACING PAGE: *Landslide on the shore of Lake Merced induced by the liquefaction of loose saturated sand during the 1957 San Francisco, CA, earthquake.*



6. EARTHQUAKE ACCELERATION AND THRESHOLD STRAIN

6.1 GENERAL

Laboratory and analytical results have been presented, thus far, to support the use of a cyclic strain approach for predicting liquefaction potential. The basic equation of the proposed method is equation 3.5 as restated below:

$$\gamma_c = 0.65 \frac{a_p}{g} \frac{\sigma_v r_d}{G_{\max} \left(\frac{G}{G_{\max}} \right) \gamma_c} \quad 3.5$$

where the symbol σ_v is used instead of σ_o (used in section 3.2) to denote total vertical pressure. The rest of the symbols in equation 3.5 are the same as defined for equation 3.5 originally.

Equation 3.5 can be used in principle to compute the equivalent seismic cyclic shear strain, γ_c , acting on a layer of sand located below the groundwater table. An element of this sand layer is sketched in figure 6.1. The soil is subjected to a peak ground surface horizontal acceleration, a_p , which induces the seismic strain γ_c at depth z .

When using equation 3.5, a_p is assumed known, and σ_v can be obtained from the unit weights of the layers between the ground surface and depth z , if the depth to groundwater level, z_w , is also known. The value of r_d can be obtained from a plot such as figure 3.4. The other two factors in equation 3.5 are G_{max} and $(G/G_{max})\gamma_c$. The shear modulus at small strains, G_{max} , can be measured in the field by means of geophysical techniques. The measuring in situ of G_{max} is one of the key aspects of the proposed cyclic strain method, and one of its main advantages. The main source of uncertainty in equation 3.5 is $(G/G_{max})\gamma_c$ which will be discussed in detail in the following paragraphs. $(G/G_{max})\gamma_c$ is a function or curve giving G/G_{max} once γ_c is known. Typical measured curves of (G/G_{max}) versus γ_c for sands are given in figure 6.2. Therefore, the determination of γ_c using equation 3.5 will, in general, involve iterating.

Two different cases may arise when using equation 3.5 to compute γ_c :

- (a) The computed value is smaller than or about equal to the threshold strain, i.e., $\gamma_c \lesssim \gamma_t \approx 10^{-2}$ percent $= 10^{-4}$. This will occur for a "stiff" sand (G_{max} high) and/or a small acceleration, a_p . In this case, the use of equation 3.5 is straightforward. At these small strains ($\gamma_c \lesssim 10^{-2}$ percent), $(G/G_{max})\gamma_c$ is not far from unity (see fig. 6.2) and G_{max} is a very reliable predictor of the secant shear modulus, G , at the strain γ_c . In addition, there is no pore water pressure buildup in the sand layer during shaking, and neither G nor $(G/G_{max})\gamma_c$ change during cyclic loading. This is illustrated by the test results for $\gamma_c < 10^{-2}$ in figures 5.3, 5.4, and 5.5.
- (b) The computed value is significantly larger than the threshold, i.e., $\gamma_c > \gamma_t \approx 10^{-2}$ percent. This condition will occur for a "flexible" sand (G_{max} low) and/or a large acceleration, a_p . In this case, the use of equation 3.5 involves additional uncertainties due to the increased uncertainty in the value of $(G/G_{max})\gamma_c$. One of the reasons for this is the reduction of G/G_{max} to values significantly less than unity at large strains (see fig. 6.2), with the corresponding increase in the uncertainty of the calculated $(G/G_{max})\gamma_c$. In other words G_{max} is a less reliable predictor of the secant modulus G , at large values of γ_c , than at small values of γ_c . A second source of uncertainty for $(G/G_{max})\gamma_c$ is that for $\gamma_c > \gamma_t$, there is a pore water pressure buildup, and due to that the values of G and $(G/G_{max})\gamma_c$ are reduced with duration of cyclic loading (see results in figs. 5.3, 5.4, and 5.5). Both G and $(G/G_{max})\gamma_c$ are now a function of the number of cycles, and hence, of the duration of shaking, thus, further complicating the use of equation 3.5 and adding to the uncertainty of the calculated γ_c . These problems, arising from the use of expressions such as equations 3.5 for strains above the threshold, have also been recently discussed by Seed (1980 [75]).

The rest of this chapter focuses on case (a), and specifically on the conditions under which the seismic strain is equal to the threshold value, $\gamma_c \approx \gamma_t$. Case (b) requires further research, and is not further discussed herein.

The available evidence for the existence and value of the threshold strain, γ_t , is discussed elsewhere in this report and includes experimental results reported by several authors, analytical results using a model of spheres in chapter 4, and a very precise measurements of γ_t in Monterey No. 0 sand presented in figures 5.18 and 5.19. All these results are remarkably consistent, and suggest that $\gamma_t \approx 10^{-2}$ percent is a realistic estimate of the threshold for normally consolidated sands over a wide range of confining pressures and relative densities. For this reason, a value of $\gamma_t = 10^{-2}$ percent = 10^{-4} will be used for the calculations in the rest of this chapter.

If the value $\gamma_c = \gamma_t = 10^{-4}$ is placed in equation 3.5, the peak ground surface acceleration which induces the threshold strain in the sand layer can be computed. We call this acceleration the "threshold peak ground surface acceleration" and label it " $(a_p)_t$ ":

$$\frac{(a_p)_t}{g} = 1.538 \times 10^{-4} \frac{G_{\max} (G/G_{\max}) \gamma_t}{\sigma_v r_d} \quad 6.1$$

If $(a_p)_t$ is measured in g's, equation 6.1 can be rewritten:

$$(a_p)_t = 1.538 \times 10^{-4} \frac{G_{\max} (G/G_{\max}) \gamma_t}{\sigma_v r_d} \quad (\text{g's}) \quad 6.2$$

Throughout the rest of this chapter, equation 6.2 is used to compute $(a_p)_t$. Section 6.2 reviews available values of G_{\max} for sands measured in the laboratory and in situ, and the modulus reduction curve, $(G/G_{\max})\gamma$ versus γ , is discussed in section 6.3. In section 6.4, equation 6.2 is used as the basis for a parametric study of the value of $(a_p)_t$ for different sand stiffnesses and depths, as well as for different water table elevations in the field.

6.2 THE MODULUS AT SMALL STRAINS, G_{\max}

6.2.1 Laboratory Results

Hardin and Drnevich (1972 [29]) performed an extensive study of G_{\max} in the laboratory, using the resonant column technique, and they proposed the expression for G_{\max} shown in equation 5.1, which was used in chapter 5 to evaluate the triaxial measurements of G at small strains in Monterey No. 0 sand. Seed and Idriss (1970 [77]) modified equation 5.1, and suggested the use of the expression:

$$G_{\max} = 1,000 K_{2\max} (\sigma'_m)^{1/2} \quad G_{\max}, \sigma'_m \text{ in psf} \quad 6.3$$

where $\sigma'_m = \frac{1}{3} (\sigma'_1 + \sigma'_2 + \sigma'_3)$ is the average effective normal stress, and $K_{2\max}$ is a function of the relative density of the sand, D_r . Equation 6.3 is certainly valid for isotropically consolidated sands, in which $\sigma'_1 = \sigma'_2 = \sigma'_3$. There is also evidence suggesting its applicability to the case of anisotropically consolidated sands, and to sands subjected to a static compressive deviator stress in cyclic triaxial tests (Hardin and Black, 1968 [28]; Tatsuoka, et al., 1979 [85]).

Figure 6.3 shows the function $K_{2\max}$ versus D_r , proposed by Seed and Idriss. For a loose sand with a relative density, $D_r \approx 30$ percent, $K_{2\max} \approx 35$, and for a very dense sand with $D_r \approx 90$ percent, $K_{2\max} \approx 70$. Therefore, figure 6.3 predicts that, for a given state of stresses, G_{\max} will approximately double for dense sand as compared with loose sand.

6.2.2 In Situ Measurements

Several geophysical (seismic) techniques have been used to measure G_{\max} of soils in situ. In all these techniques, the shear wave velocity, V_s , at small strains is measured in the field and G_{\max} is obtained from the expression:

$$G_{\max} = \rho V_s^2 \quad 6.4$$

where ρ = mass density of soil layer = total unit weight/acceleration due to gravity. The geophysical techniques used for this purpose include the cross-hole method, the downhole method, the refraction method and the Rayleigh wave method (Anderson and España, 1978 [2]; Woods, 1978 [87]). Of these, the most reliable one is the crosshole technique sketched in figure 6.4. In this method, a vertically polarized shear wave impulse propagates horizontally, and the travel time of the impulse between drillholes is measured to compute V_s .

Powell (1979 [63]) performed a literature review of available in situ measurements of G_{\max} in sands which had been obtained using these geophysical methods. As these measurements were made at depths varying between 10 and 130 ft at sites having different groundwater elevations, the values of effective vertical overburden pressure, σ'_v and of average effective stress, σ'_m varied widely. It would have been useful to normalize these measured G_{\max} values by means of equation 6.3, thus, obtaining $K_{2\max}$:

$$K_{2\max} = \frac{G_{\max}}{1,000 (\sigma'_m)^{1/2}} \quad 6.5$$

In field conditions, $\sigma'_m = \frac{1}{3} \sigma'_v (1 + 2K_o)$; nevertheless, K_o was generally not measured at those sites. Therefore, Powell normalized G_{\max} by $(\sigma'_v)^{1/2}$, as the value of σ'_v could be easily estimated in all cases and a coefficient A was defined instead of $K_{2\max}$:

$$A = \frac{G_{\max}}{816.5 (\sigma'_v)^{1/2}} \quad 6.6$$

In equation 6.5, both G_{\max} and σ'_v are in psf and the units of A are the same as these of $K_{2\max}$, i.e., $(\text{lb}^{1/2}/\text{ft})$. The numerical coefficient 816.5 in equation 6.5 was selected so that, for $K_0 = 0.5$, $\sigma'_m = (\frac{1}{3}) \sigma'_v [1 + (2)(0.5)]$, $A = K_{2\max}$ and equations 6.4 and 6.5 become one and the same. A value of $K_0 = 0.5$ is a reasonable estimate for normally consolidated, freshly deposited, noncompacted sand deposits.

Figure 6.5 shows the data compiled by Powell, as a plot of A versus depth z, for 10 sandy sites consisting of clean sand and silty sand deposits without gravel or clay. The values of A range from 35 to 240 with most of them between 35 and 150.

It is interesting to compare the values of A from the field in figure 6.5 with the values of $K_{2\max}$ from the laboratory in figure 6.3. The lower bound of $A \approx 35$, coincides well with the lower bound of $K_{2\max} \approx 35$, corresponding to loose sands. This observation is reasonable, as it could be expected that the lower values of G_{\max} (and of A) in the field should correspond to loose, normally consolidated sands having a low value of $K_0 (\approx 0.5)$. On the other hand, the upper bound of the A values in figure 6.5, which is at least 150 and may be as high as 240, is much above the highest value, $K_{2\max} = 70$ in figure 6.3. Therefore, while the laboratory results might suggest that, for a given state of stress, sands may have values of G_{\max} differing by a factor of only about two, the field results suggest that this ratio may be as high as four or seven.

From the viewpoint of the proposed strain approach to liquefaction, this wide variation of the A value from field results is of great importance. A value of $A \approx 35$ would define a "flexible" sand, while a value of $A \approx 150$ or 200 would define a "very stiff" sand. The practical implications for liquefaction of a sand being "flexible" or "stiff" will be demonstrated in section 6.4. For the purpose of this study, a range of values of A between 35 and 150 is used.

The possible reasons for this discrepancy between the highest measured values of $K_{2\max}$ and A will now be examined.

One possibility for the discrepancy is that the actual range of $K_{2\max}$ for different sands is larger than the ratio of 2 suggested by figure 6.3. In fact, equation 6.3 and figure 6.3 are somewhat simplified versions of Hardin-Drnevich equation 5.1. G_{\max} is really a function of the void ratio e, rather than a function of relative density, D_r . Therefore, different sands having different grain size distributions and silt contents, such as those summarized in figure 6.5, may have quite different values of e, and thus may, as a group, cover a wider range of G_{\max} than that suggested by figure 6.3.

Another possible explanation is that $K_0 > 0.5$ in the field due to overconsolidation or other factors, in which case $A \neq K_{2\max}$. From equations 6.4 and 6.5, the relation between $K_{2\max}$ and A for any value of K_0 is

$$\frac{K_{2\max}}{A} = \left(\frac{2}{1 + 2K_0} \right)^{1/2} \quad 6.6$$

For an overconsolidated sand, K_0 is a function of the overconsolidation ratio, OCR. As shown by the typical data in figure 6.6, for $OCR = 1$, $K_0 \approx 0.4$, which is close to $K_0 = 0.5$ assumed here. For $OCR \approx 7$, $K_0 \approx 1$, while for much large values of OCR, K_0 can even approach 1.6 or 1.8. Equation 6.6 is plotted in figure 6.7 for the range of K_0 between 0.4 and 1.6. It can be seen that for a sand with $OCR \approx 7$ and $K_0 \approx 1$, $K_{2max} \approx 0.8A$. Therefore, if some of the sands having $A \approx 150$ in figure 6.3 were consolidated with $K_0 \approx 1$, $K_{2max} \approx (0.8)(150) = 120$, and the factor between maximum and minimum K_{2max} in the field would be 3.4 instead of 4 obtained before.

The variation discussed above for the void ratio, e , and for K_0 of sands in the field may serve as a partial explanation of the difference in ranges between figures 6.3 and 6.5. However, they do not explain all the differences since other factors also seem to play an important role. These other factors, which have been shown to increase G_{max} of sands in the laboratory and yet were not considered, neither in the original Hardin-Drnevich equation (eq. 5.1) nor in the modified Seed-Idriss version (eq. 6.3), include: (i) seismic prestraining, and (ii) time under pressure.

The seismic prestraining effect was originally discussed by Drnevich and Richart (1970 [23]), when performing resonant column tests on dry sand. They found that a large number of cycles of high amplitude shear straining could cause a large increase in the value of G_{max} if the amplitude is above the threshold strain, $\gamma > \gamma_t \approx 10^{-2}$ percent. The increase in G_{max} was significant for a few thousands of cycles (an increase of about 30 percent) while for one million cycles G_{max} was increased by a factor of two or three. This large increase in G_{max} could not be explained by changes in void ratio, and was attributed by Drnevich and Richart to wear and stiffening of the contacts between the sand grains. Another possible explanation of the effect of prestraining in sand has been suggested by Youd (1977a [95]). In his hypothesis, cyclic straining produces changes in the packing of the sand by means of the collapse of the more unstable grain arrangements. These collapses have a negligible or small influence on the overall relative density or void ratio of the sand, but they do produce a more stable and stiffer structure or fabric of the soil. A large number of high amplitude oscillations of the soil may occur in situ because of man-made operations, e.g., compaction of sand with vibrating equipment, vibrations due to nearby operating machinery, traffic, etc., or in geologically old natural soil deposits located in active seismic areas.

The effect of time under pressure on G_{max} of soils has been studied systematically by Afifi and Richart (1973 [1]) and Anderson and Stokoe (1977 [3]). The test results discussed by these authors show that G_{max} increases with time of secondary consolidation in all soils. The increase for G_{max} in sands in the laboratory is typically of the order of one percent per log cycle of time after 1,000 minutes. An extrapolation of this rate of increase would suggest a significant increase in G_{max} for geologically old sand deposits.

6.3 THE MODULUS REDUCTION FACTOR, G/G_{\max}

The modulus reduction curve $(G/G_{\max})\gamma$ versus cyclic shear strain, γ , is critical for the application of the proposed strain approach. Of special interest is the value of $(G/G_{\max})\gamma_t$ at the threshold strain, $\gamma_t = 10^{-2}$ percent. Hardin and Drnevich (1972 [29]) and Seed and Idriss (1970 [77]) discussed the curve of $(G/G_{\max})\gamma$ versus γ for sands. After reviewing the experimental evidence available at the time, Seed and Idriss proposed the curve shown in figure 6.2, with an experimental band to take into account the scatter of the results. This band was previously shown in figure 4.8. Both the curve in figure 6.2 and the band in figure 4.8 are independent of the relative density of the sand and of confining pressure. At the threshold strain, $\gamma_t \approx 10^{-2}$ percent, $(G/G_{\max})\gamma_t \approx 0.75$ with the band giving a dispersion range between 0.65 and 0.85.

More recent results have confirmed these values reported by Seed and Idriss. Figure 6.2 includes a comparison of (G/G_{\max}) curves obtained by different investigations, which was compiled and originally published by Iwasaki et al., (1978 [33]). At $\gamma_t = 10^{-2}$ percent, $(G/G_{\max})\gamma_t$ in figure 6.2 ranges from 0.75 to 0.90. Figure 6.8, which was also published by Iwasaki et al., (1978 [33]), includes results for 13 sands having different grain size distributions. The factor B in the figure is a constant characteristic of each sand. Of special interest in figure 6.8 is the value of $(G/G_{\max})\gamma_t$ for $\gamma_t = 10^{-2}$ percent which is notably constant and equal to 0.75 for the 13 sands used. It should be noted that these 13 sands were tested by Iwasaki et al. in a dry state by a combination of the resonant column and torsional shear techniques, and for a confining pressure of 2,000 psf ($\approx 1 \text{ kg/cm}^2$). Iwasaki et al. also performed tests at other confining pressures in the range from 550 to 4,000 psf and found similar results to those presented in figure 6.2. They noticed a tendency for $(G/G_{\max})\gamma$ to increase with confining pressure; however, all $(G/G_{\max})\gamma_t$ values were in the range from 0.70 to 0.85. This influence of confining pressure on $(G/G_{\max})\gamma_t$ is consistent with the discussion by Richart (1980 [66]) and with the results for Monterey No. 0 sand summarized in figure 5.10.

The results discussed above strongly suggest that $(G/G_{\max})\gamma_t \approx 0.75$ for $\gamma_t = 10^{-2}$ percent, with an experimental scatter between about 0.65 and 0.85. These numbers seem to be independent of relative density and to be generally representative for the range of confining pressures of practical interest. Tatsuoka et al. (1979 [85]) showed that these conclusions for $(G/G_{\max})\gamma_t$ are valid for both isotropically ($K = 1$) and anisotropically consolidated in the range $0.33 < K < 1$) sand specimens. Very recently, Canales (1980 [8]) presented results showing that, although G_{\max} is strongly affected by prestraining, the curve $(G/G_{\max})\gamma$ and the value $(G/G_{\max})\gamma_t$ at the threshold are about the same before and after prestraining. With respect to the influence of time under pressure on G/G_{\max} , Anderson and Stokoe (1977 [3]) have suggested that G/G_{\max} may increase somewhat due to this effect. Specifically, at the threshold, $(G/G_{\max})\gamma_t$ may increase from about 0.75 without the time effect, to 0.80 or 0.90 after long time under pressure.

For the purposes of this study, a representative value of $(G/G_{\max})\gamma_t = 0.75$ is adopted for sands at $\gamma_t = 10^{-2}$ percent, with lower and upper bounds of 0.65 and 0.85, respectively.

6.4 PARAMETRIC STUDY

This section presents the results of a parametric study of the threshold peak surface acceleration, $(a_p)_t$, based on equation 6.2 and on the results discussed in sections 6.2 and 6.3. For simplicity, in equation 6.2, G_{max} is replaced by A as defined by equation 6.5, and a total unit weight = 115 lb/ft^3 is assumed for the soil both above and below the groundwater table. For the field condition sketched in figure 6.1, $\sigma_v = 115 z \text{ (lb/ft}^2\text{)}$, and $\sigma'_v = 115 z_w + (115 - 62.4)(z - z_w)$. Finally, and for $(G/G_{max})\gamma_t = 0.75$, equation 6.2 becomes

$$\frac{(a_p)_t}{A} = 8.2 \times 10^{-4} \frac{(62.4 z_w + 52.6z)^{1/2}}{z r_d} \quad (a_p)_t \text{ in g's.} \quad 6.7$$

Equation 6.7 was used for the parametric study. In the calculations, the following values of r_d , obtained from figure 3.4 were used.

z (feet)	r_d
10	0.98
20	0.96
30	0.92

The calculations were performed for values of z below the water table, $z > z_w$. Equation 6.7 has been plotted in figure 6.9 as a function of z_w and for depths $z = 10, 20$, and 30 feet, which covers the range of depths where liquefaction most frequently occurs.

Equation 6.7 is also plotted as $(a_p)_t$ versus z_w in figure 6.10 for the depth, $z = 20 \text{ ft}$ and for $A = 35, 100$, and 150 .

Figures 6.9 and 6.10 clearly show the influence of the parameters z , z_w , and A in determining the value of $(a_p)_t$. In figure 6.9, for the same stiffness, A , there is a large decrease in $(a_p)_t$ between $z = 10 \text{ ft}$ and $z = 20 \text{ ft}$ while the decrease is much smaller from 20 to 30 ft . As expected, $(a_p)_t$ increases when the depth to groundwater, z_w , increases.

The effect of the stiffness parameter, A , on $(a_p)_t$ is very dramatic. As $(a_p)_t$ is directly proportional to A , the value of $(a_p)_t$ should more than quadruple when going from a "flexible" ($A = 35$) sand to a "stiff" ($A = 150$) sand, other conditions being equal. This is illustrated by figure 6.10. In a sand layer having a measured $A = 35$ and located at 20 ft , and for shallow groundwater, $z_w = 0$, the threshold is $(a_p)_t \approx 0.05g$. If the sand is very stiff with $A = 150$, then $(a_p)_t \approx 0.21g$. This difference is very significant since a peak surface ground acceleration of $0.20g$ is quite strong and can even be higher than the design acceleration in many low seismicity areas. As shown by figure 6.10, for $z = 20 \text{ ft}$, $(a_p)_t$ can be substantially larger than $0.20g$ if $A > 150$ and/or the groundwater is located at some depth.

For an example of application using figures 6.9 and 6.10, let us assume that we have two adjacent soil profiles, both with the groundwater level at $z_w = 10$ ft and potentially liquefiable sand layers at $z = 20$ ft. The design surface acceleration is also the same, $a_p = 0.15g$ which corresponds to a magnitude 8 (long duration) earthquake. In site 1, the sand layer has a value of $A = 35$, measured using the crosshole technique. Therefore, $(a_p)_t \approx 0.06g$ and this layer will most probably liquefy. In site 2, the sand layer has a measured $A = 150$. Therefore, $(a_p)_t = 0.26g$. The sand layer in site 2 will not even start developing an excess pore water pressure, let alone liquefy during the design earthquake.

Figures 6.9 and 6.10 also suggest that sand deposits will not liquefy for peak ground accelerations less than about $0.05g$, even for the worst soil conditions, shallow water table, and for large earthquake magnitudes causing the longest durations of shaking. Seed et al., (1975 [81]) compiled a list of thirty-eight liquefaction case histories. According to that list, the smallest value of a_p to cause liquefaction is $0.08g$ which occurred during the 1933 Tohankai earthquake in Japan, which had a magnitude 8.3 and a long duration of shaking. Based on a review of about 100 liquefaction failures in Japan during the last century, Kuribayashi and Tatsuoka (1975 [42]) concluded that the minimum intensity in the Japanese Intensity Scale, JMA for which liquefaction has occurred is five, which corresponds to a range of peak acceleration between $0.08g$ and $0.25g$. Finally, liquefaction is usually associated with earthquakes having Modified Mercalli Intensities MMI of VI or larger. The MMI of VI corresponds approximately to a ground acceleration of $0.05g$. Therefore, the available evidence indicates that the results of the parametric study present herein are generally consistent with reported cases of liquefaction during earthquakes.

In order to evaluate the uncertainty in $(a_p)_t$ introduced by the scatter of values of r_d and $(G/G_{max})\gamma_t$, the chart of figure 6.10 was recalculated to obtain lower bound and upper bound curves, as follows.

	r_d	$(G/G_{max})\gamma_t$
Lower Bound Curve	0.98	0.65
Average Curve (figure 6.10)	0.96	0.75
Upper Bound Curve	0.94	0.85

The corresponding values of $(a_p)_t$, calculated using modified versions of equation 6.7, are plotted in figure 6.11 for $z = 20$ ft, and for $A = 35$ and $A = 150$. Although the numerical values of $(a_p)_t$ change somewhat when the variations in r_d and $(G/G_{max})\gamma_t$ are considered, the main conclusions reached above on the influence of stiffness on $(a_p)_t$ do not change. For $z_w = 0$, if $A = 35$, $(a_p)_t$ varies between 0.04 and $0.06g$, while if $A = 150$, $(a_p)_t$ varies between $0.18g$ and $0.24g$. For the example of sites 1 and 2 discussed above, with $z_w = 10$ ft and $z = 20$ ft, the ranges of $(a_p)_t$ are 0.05 to $0.07g$ and 0.22 to $0.30g$ for sites 1 and 2, respectively. Therefore, for a design acceleration of $0.15g$ and a long duration earthquake, site 1 may liquefy and site 2 will not, as concluded previously using average values of r_d and $(G/G_{max})\gamma_t$.

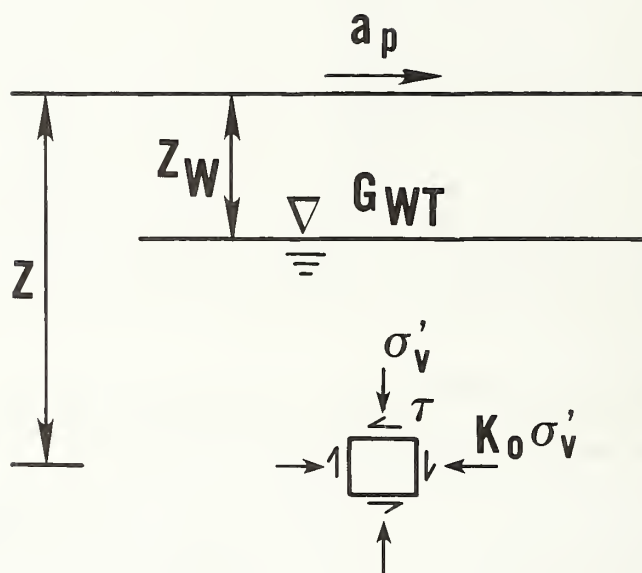


Figure 6.1 Simplified soil profile

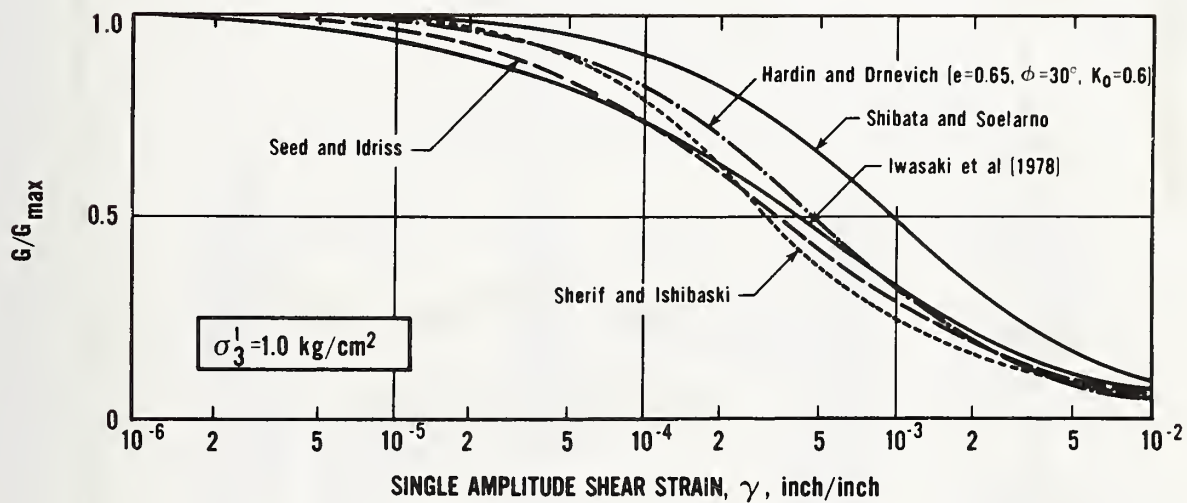


Figure 6.2 Modulus reduction curves for sands (Iwasaki et al., 1978)

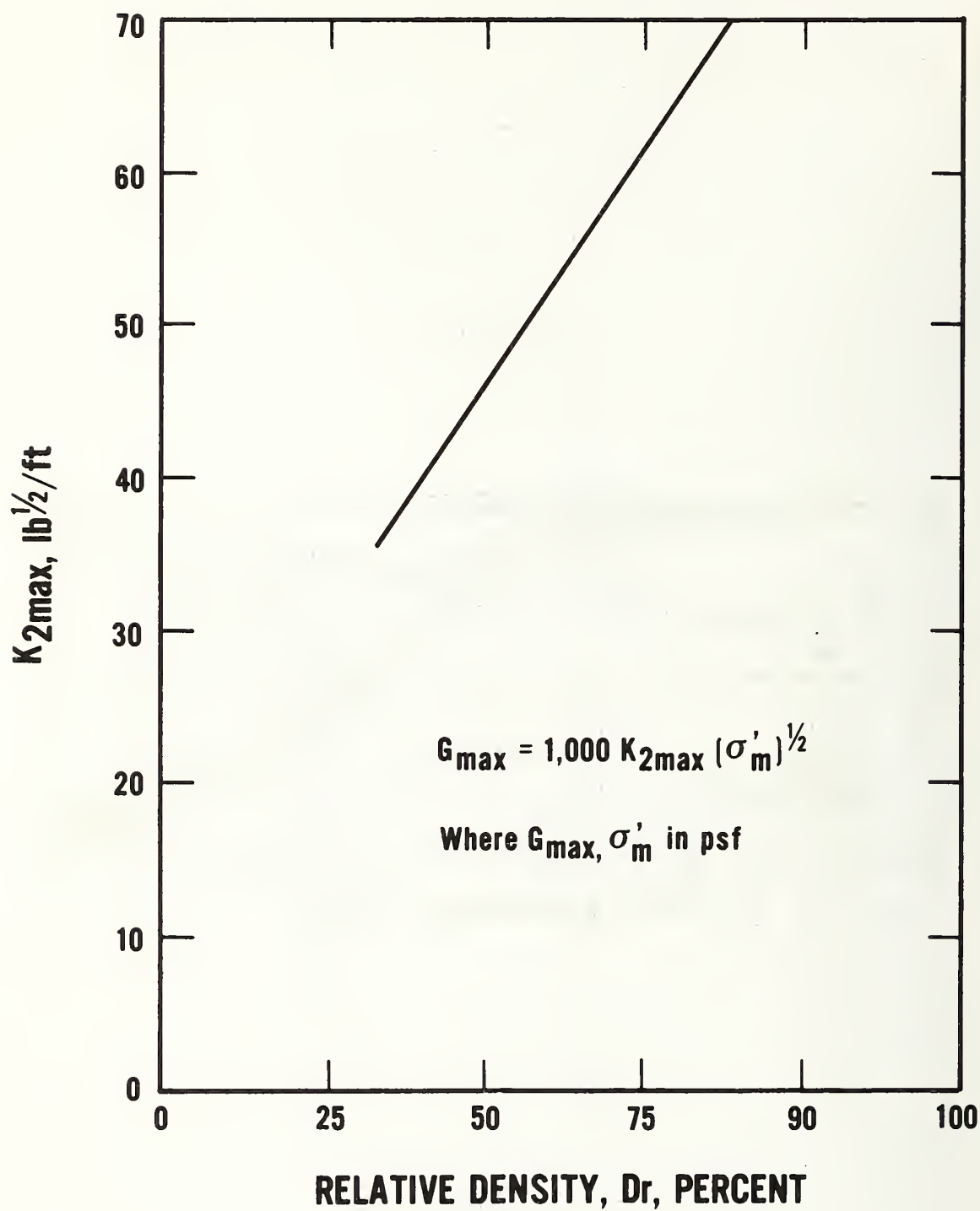
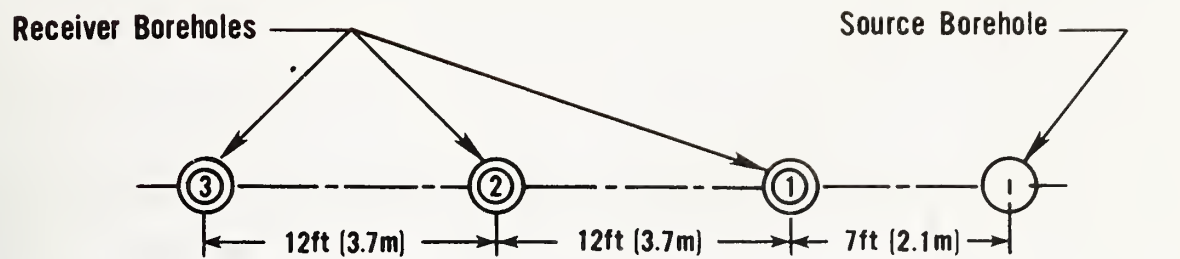
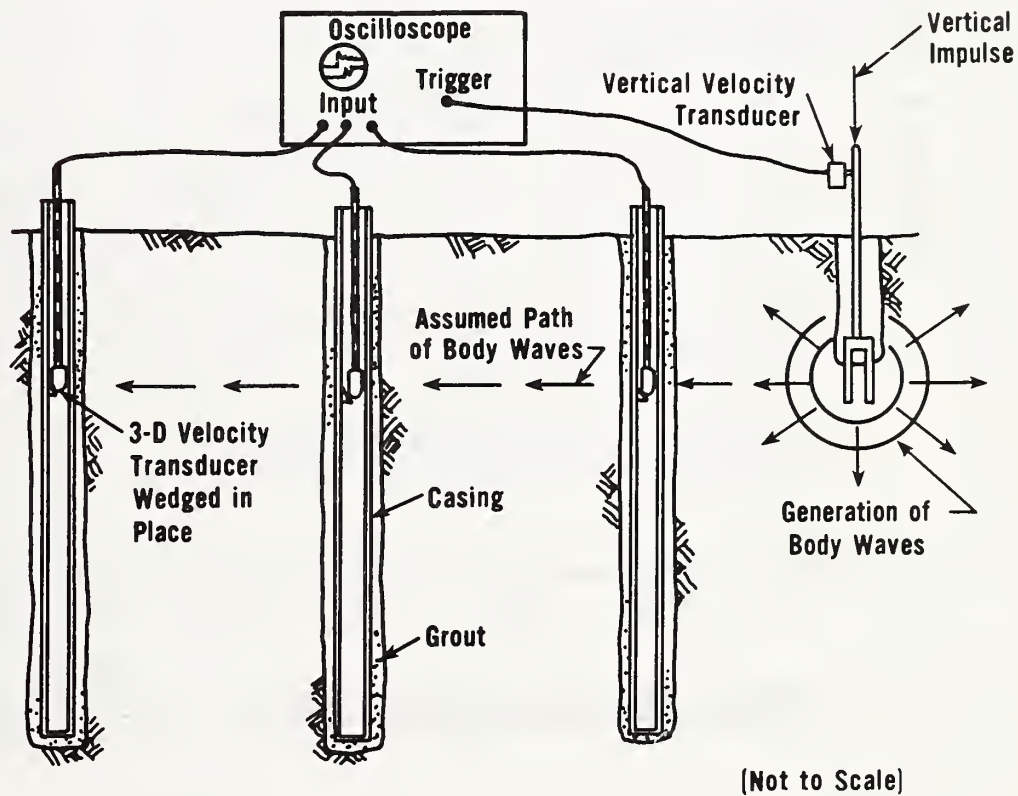


Figure 6.3 Relation between normalized stiffness parameter, K_{2max} , and relative density (modified from Seed and Idriss, 1970)



a.-PLAN VIEW



b.-CROSS-SECTIONAL VIEW

Figure 6.4 Crosshole geophysical method (Hoar and Stokoe, 1977)

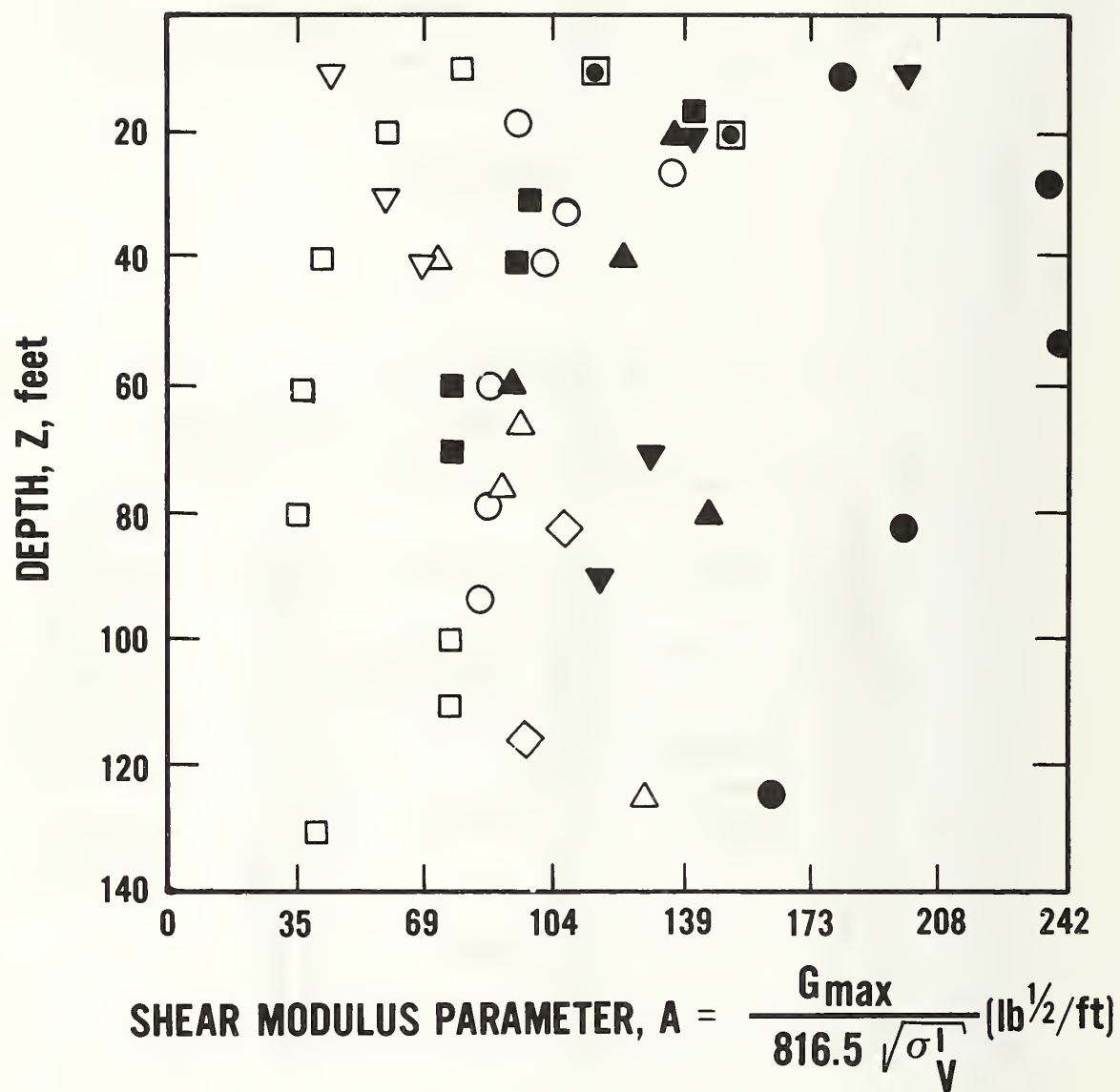


Figure 6.5 Normalized shear modulus parameter, A, measured for sands in the field using geophysical techniques (Powell, 1979)

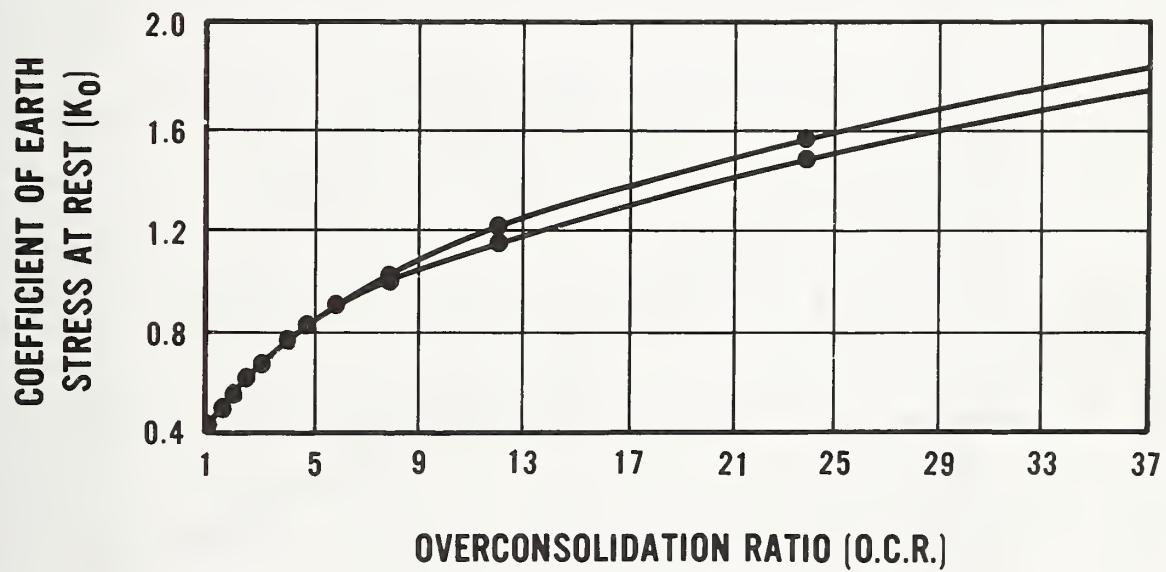


Figure 6.6 Coefficient of earth pressure at rest, K_0 , as a function of overconsolidation ratio, OCR (Hendron, 1963)

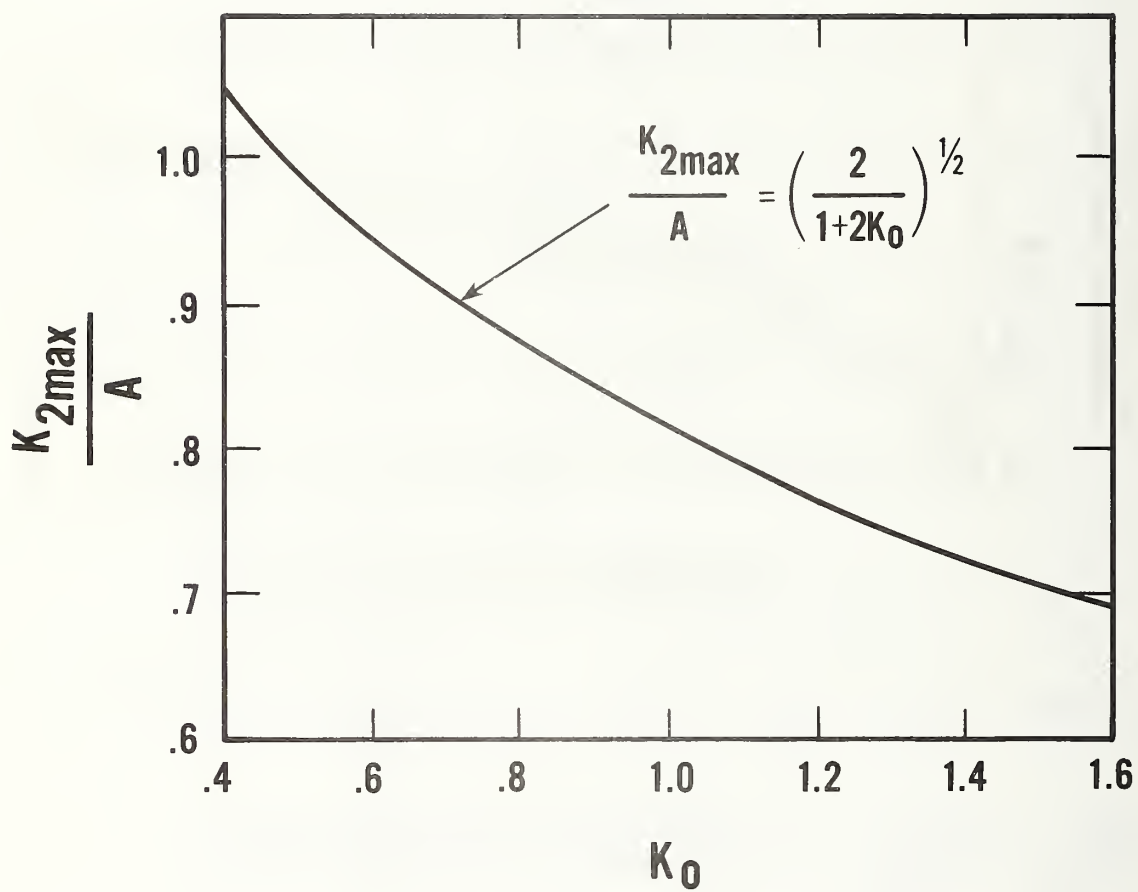


Figure 6.7 Influence of the coefficient of earth pressure at rest, K_0 , on the normalized shear modulus parameter, A

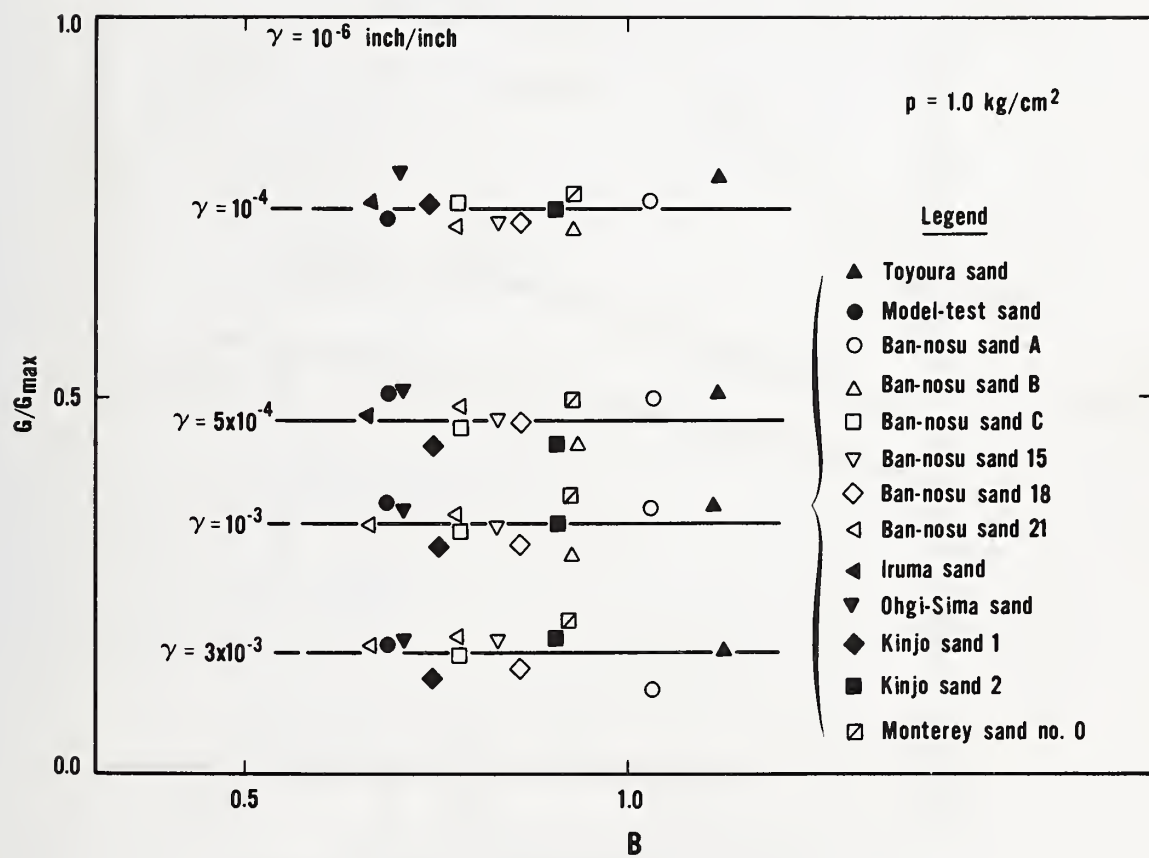


Figure 6.8 Reduction of shear modulus at different cyclic shear strains, γ , for sands (data from Iwasaki et al., 1978; B is a coefficient characteristic of each sand tested)

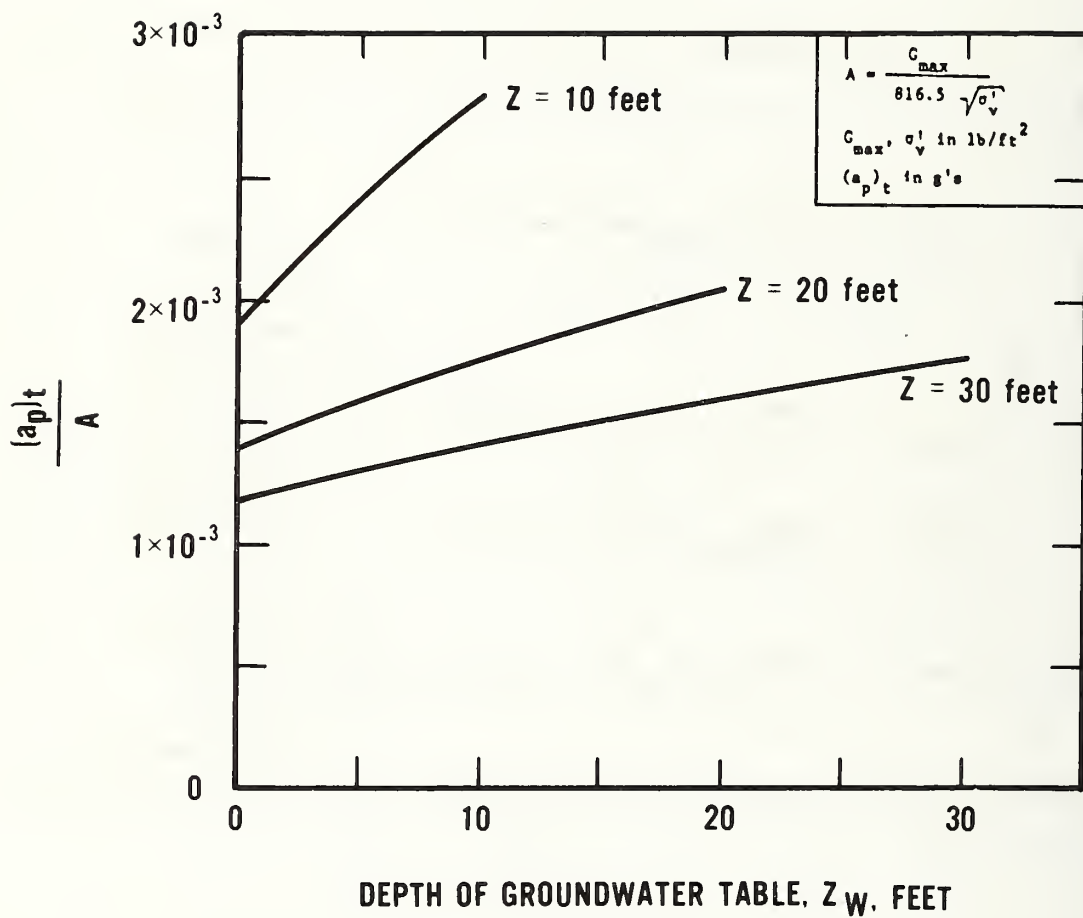


Figure 6.9 Liquefaction chart for threshold peak ground surface acceleration, $(a_p)_t$

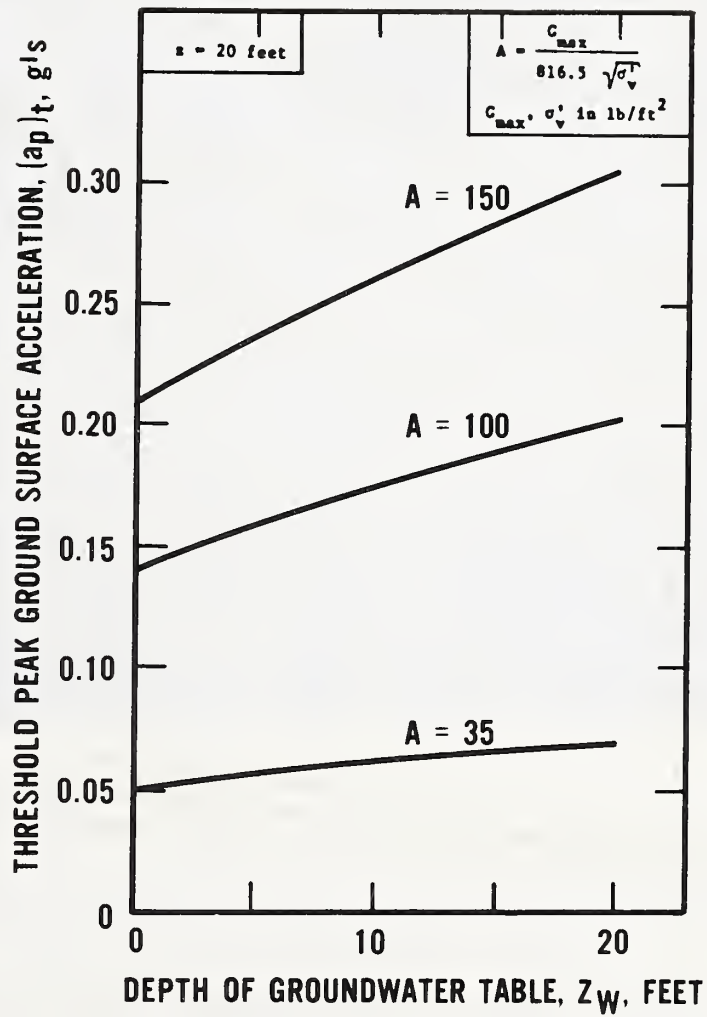


Figure 6.10 Liquefaction chart for threshold peak ground surface acceleration $(a_p)_t$, at $z=20$ feet

FACING PAGE: Sand boils in rice field near Old Kitakami River. The sand boils were caused by liquefaction during the Miyagi-ken-oki, Japan, June 12, 1978, earthquake.

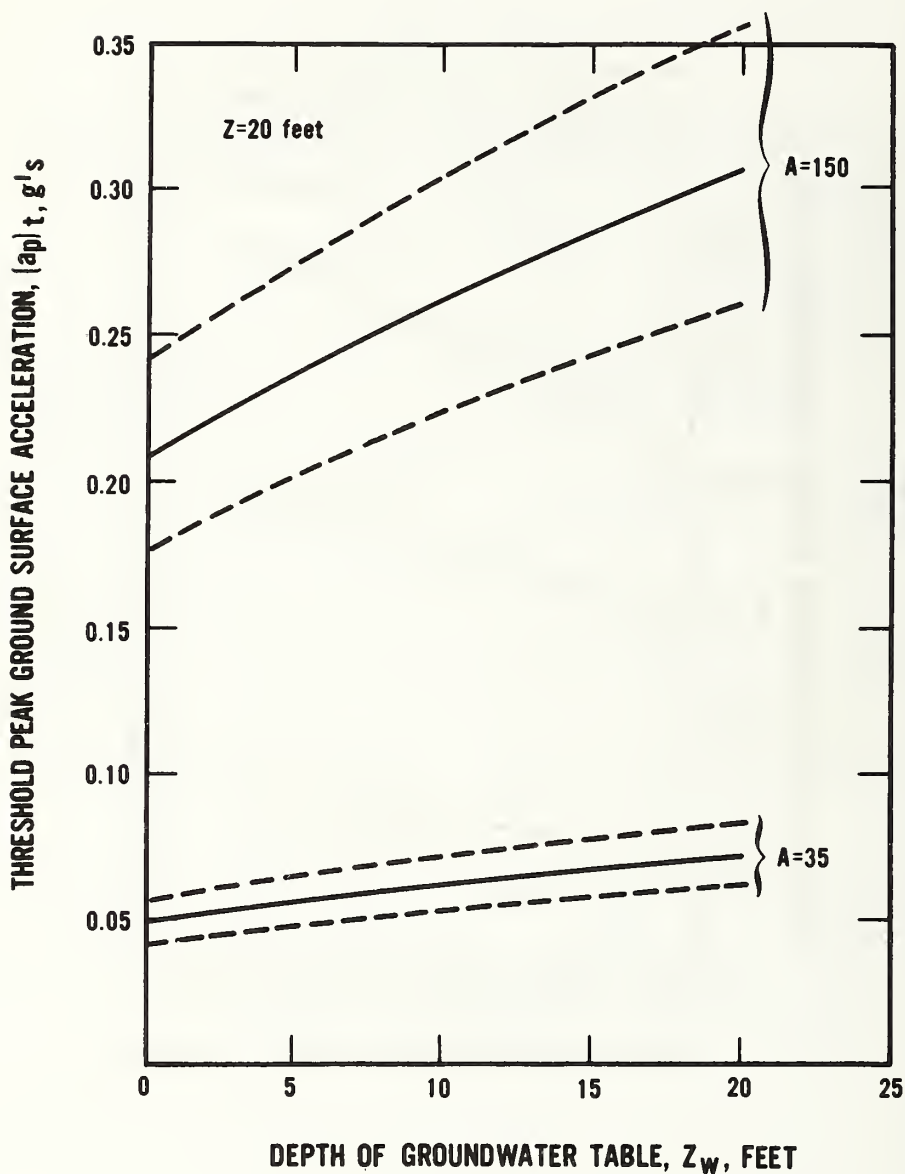


Figure 6.11 Lower and upper values of $(a_p)_t$ to account for scatter in $(G/G_{\max})\gamma_t$ and r_d at $z=20$ ft



7. SUMMARY AND FINDINGS

We have reached the following conclusions from the work presented in this report, on methods for predicting pore pressure buildup and liquefaction potential of saturated sands at level sites during earthquake:

- 1) Data from cyclic stress-controlled tests on sands accumulated in the last few years demonstrate that a number of factors besides relative density influence the value of the cyclic strength. These factors include fabric, overconsolidation, prior seismic straining and time under pressure. The findings raise serious doubts about the present practice of using stress-controlled cyclic tests on disturbed samples reconstituted to the estimated field density.

- 2) Cyclic test results have demonstrated that there is a predictable correlation between cyclic shear strain and the pore water pressure buildup of saturated sands. An example of this correlation is presented in figure 5.33. Also, more consistent results are obtained if strain-controlled rather than stress-controlled tests are conducted. In particular, fabric, which has a large influence on cyclic strength, does not influence significantly the pore water pressure developed during strain-controlled tests. It is suggested that the influence of relative density and of the other factors listed in point (1), on the cyclic strength, is due to a large extent to differences in stiffness between specimens in both compression and extension, which, in turn, induce very different shear strains during stress-controlled tests. This would explain why strain-controlled tests give more consistent results than stress-controlled tests.
- 3) Results of strain-controlled tests on normally consolidated dry and saturated sands by several investigations, using a number of testing techniques, have consistently suggested the existence of a threshold cyclic shear strain, $\gamma_t \approx 10^{-2}$ percent. For strains below this threshold, there is neither densification nor prestraining of dry sands and there is no pore water pressure buildup in saturated sands. An analytical model of the sand constituted by a simple cubic array of quartz spheres predicts similar values of γ_t ($\gamma_t = 1 \times 10^{-2}$ to 4×10^{-2} percent for the range of confining pressures of practical interest). A series of undrained cyclic strain-controlled triaxial tests on saturated Monterey No. 0 sand reported herein measured a value $\gamma_t = 1.1 \times 10^{-2}$ percent. The experimental data in figures 5.18 and 5.19 indicate that this value of γ_t for the sand tested is independent of relative density and of confining pressure for the range between about 500 psf and 2,000 psf. This proof of the existence of γ_t , as well as its constant value are powerful arguments in favor of a strain approach to liquefaction.
- 4) Based on the conclusions above, a cyclic strain approach to liquefaction is proposed. The basic equation of the suggested method (eq. 3.5) requires estimating both the seismic strain induced in the sand layer and the effective shear modulus of the layer during the earthquake. The proposed method is based on measuring the shear modulus in situ at small strains, G_{max} , using geophysical techniques, and on performing cyclic strain-controlled tests in the laboratory to determine: (i) the modulus reduction values, G/G_{max} , (ii) the value of γ_t , and (iii) the pore water pressure buildup Δu , versus cyclic strain γ and number of cycles n .
- 5) A series of 12 undrained strain-controlled cyclic triaxial tests on saturated Monterey No. 0 sand specimens was performed. The tests included nondestructive, high precision measurements at very small strains ($\gamma \approx 10^{-3}$ percent) using an improved technique recently developed by the second author (Ladd), which allowed the measurement of G_{max} and γ_t for the sand specimens. In addition to G_{max} and γ_t , the values of G/G_{max} and Δu needed for the cyclic strain approach were also measured. The results of this test program are presented in chapter 5 where the influence of relative density and confining pressure on G_{max} and γ_t , and of cyclic strain and number of straining cycles on G/G_{max} and Δu are presented and discussed in detail.

The results are also compared with similar data obtained by other researchers on Monterey No. 0 sand and other sands, with good agreement.

- 6) Two outcomes are possible when applying the proposed strain approach to a specific site under a given design peak surface acceleration, a_p . In the first outcome, which will occur for a low value of a_p and/or a stiff sand layer (G_{\max} large), $\gamma_c \lesssim \gamma_t \approx 10^{-2}$ percent, the application of the method is straightforward with very small uncertainty, and the method predicts that the risk of liquefaction is negligible. In the second outcome, which will occur for a high value of a_p and/or a flexible sand layer (G_{\max} small), the seismic strain, $\gamma_c > \gamma_t \approx 10^{-2}$ percent, and there is risk of liquefaction. In this case, the uncertainty in the application of the method will increase as γ_c increases above γ_t , due to the uncertainty in the value of G/G_{\max} .
- 7) Finally, a simplified cyclic strain approach to liquefaction is proposed, aimed at determining, for a given site and depth of the sand, the value of the surface peak acceleration inducing the threshold strain in the layer. This is called the threshold peak ground surface acceleration $(a_p)_t$. If the design acceleration, $a_p < (a_p)_t$, the danger of liquefaction can be discarded. If $a_p > (a_p)_t$, further studies are needed. Simplified charts were developed and are presented in chapter 6 to compute $(a_p)_t$ for a given site. The use of these charts require knowing G_{\max} , the depth of the layer, the overburden pressure and the depth to groundwater table. These charts are consistent with the historic experience of seismic liquefaction, and are recommended for preliminary site-specific evaluations. These charts, shown in figures 6.9 through 6.11, indicate that $(a_p)_t$ may be as low as 0.04g for a site with low G_{\max} and shallow water table, and as high as 0.20g or 0.30g for a stiff site having a high measured G_{\max} and a deep water table.



8. ACKNOWLEDGMENT

The authors gratefully acknowledge the contributions by Mr. Paul Dutko and his associates at Woodward-Clyde Consultants, Clifton, NJ, in carrying out the laboratory testing program presented in this report. The contribution of Mr. Gregory Thomas at Rensselaer Polytechnic Institute, who plotted the laboratory results shown in chapter 5, is also gratefully acknowledged. The authors also want to thank Dr. Rune Dyvik and Captain William Pierce at Rensselaer Institute, who reviewed the manuscript and made useful suggestions. A special note of thanks to Mrs. Brenda Thompson and Ms. Ulesia Gray of the Word Processing Center of CBT for the typing and performing the many revisions of this manuscript.

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APPENDIX

Calculations of Cyclic Triaxial Tests Results

From the measured peak axial loads and axial deformations within a given cycle, cyclic deviator stresses and axial strains are computed using the specimen dimensions after consolidation. No corrections were made for the affect of the rubber membrane.

The shear strain amplitude is calculated from the axial strain amplitude using the following equation:

$$\underline{+\gamma} = \underline{+\epsilon} (1+\nu) = \frac{\Delta L_{PP}}{2H_c} \times (1+\nu) = \underline{+} 1.5\epsilon$$

where:

- $\underline{+\gamma}$ = shear strain amplitude (in/in)
- $\underline{+\epsilon}$ = axial strain amplitude (in/in)
- ΔL_{PP} = peak-to-peak axial deformation measured within a given loading cycle using the oscillograph recorder
- H_c = height of specimen after consolidation
- ν = Poisson's ratio; a value of 0.5 was used in all tests.

The shear modulus is calculated using the following equation:

$$G = \frac{E}{2(1+\nu)} = \frac{p_{pp} \times H_c}{3A_c \times L_{pp}}$$

where:

- G = shear modulus
- E = Young's modulus
- p_{pp} = peak-to-peak axial load measured within a given loading cycle using the oscillograph recorder
- A_c = area of specimen after consolidation

Calculated values of shear strain amplitude and shear modulus were also corrected for sample setup compliance using the following equations:

$$\underline{+\gamma}_c = \underline{+\gamma} \times CF$$

$$G_c = G / CF$$

where:

- $\underline{+\gamma}_c$ = shear strain amplitude corrected for equipment compliance
- G_c = shear modulus corrected for equipment compliance
- CF = correction factor for equipment compliance obtained from a curve such as that presented in figure 5.2.

The data presented in figure 5.2 represent the results of a series of special tests in which each test was individually corrected for equipment compressibility. This correction consisted of correcting each recorded value of ΔL_{pp} by subtracting away the peak-to-peak axial deformation of a steel cylinder grouted into the cell in the same manner as the test specimens and at a confining pressure and peak-to-peak axial load similar to that which was recorded when ΔL_{pp} was determined.

During the cell calibration and from test to test, the same stones, platens, etc., are used. In addition, these items were indexed in such a manner that they are in the same position from test-to-test.

U.S. DEPT. OF COMM.		1. PUBLICATION OR REPORT NO. NBS BSS 138		2. Performing Organ. Report No.		3. Publication Date July 1982	
4. TITLE AND SUBTITLE Prediction of Pore Water Pressure Buildup and Liquefaction of Sands During Earthquakes by the Cyclic Strain Method							
5. AUTHOR(S) R. Dobry, R.S. Ladd, F.Y. Yokel, R.M. Chung, and D. Powell							
6. PERFORMING ORGANIZATION (If joint or other than NBS, see instructions) NATIONAL BUREAU OF STANDARDS DEPARTMENT OF COMMERCE WASHINGTON, D.C. 20234						7. Contract/Grant No.	
						8. Type of Report & Period Covered Final	
9. SPONSORING ORGANIZATION NAME AND COMPLETE ADDRESS (Street, City, State, ZIP) Same as 6.							
10. SUPPLEMENTARY NOTES Library of Congress Catalog Card Number: 82-600561 <input type="checkbox"/> Document describes a computer program; SF-185, FIPS Software Summary, is attached.							
11. ABSTRACT (A 200-word or less factual summary of most significant information. If document includes a significant bibliography or literature survey, mention it here) A cyclic strain approach for evaluating the buildup of excess pore water pressures and the potential for liquefaction of level sandy sites during earthquakes is proposed in this report. This strain approach is based on the premise that, for undrained loading of sand, there is a predictable correlation between cyclic shear strain and excess pore water pressure; also, that there is a threshold shear strain below which there is no sliding at the contacts between sand particles and no pore water pressure buildup can occur. As the result, a sand deposit will not develop excess pore pressures if the induced seismic shear strain is less than the threshold strain. Both theoretical evidence and experimental verification supporting the cyclic strain approach and the existence of the threshold, are presented in the report. Based on all these findings, a specific design method is proposed for predicting if excess pore pressures will develop at a specific site during a design earthquake.							
12. KEY WORDS (Six to twelve entries; alphabetical order; capitalize only proper names; and separate key words by semicolons) cyclic strain; damping ratio; earthquake engineering; laboratory testing; liquefaction; particulate mechanics; particulate model; pore water pressure; sand; seismic loading; shear modulus; shear strain; site stability.							
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						15. Price	



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